

FINITE ELEMENT MODELLING OF A BUILDING FRAME

DEPARTMENT:

UNIVERSITY:

FINITE ELEMENT MODELLING OF A BUILDING FRAME

BATCH

By

NAME

SEAT NO:

DEPARTMENT :

UNIVERSITY:

CERTIFICATE

This is to certify that the following students of batch 2011-2012 have successfully completed the final year project in partial fulfillment of requirements for a Masters Degree in _____ from _____.

PROJECT SUPERVISOR

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NOTATIONS

ACI	American Concrete Institute
C_a	Seismic coefficient
C_t	Numerical coefficient
C_v	Seismic coefficient
C_r	Centre of rigidity
C_m	Centre of mass
D	Dead load
E	Earthquake load
E_c	Modulus of elasticity of concrete
E_s	Modulus of elasticity of steel
f_c'	Compressive strength of concrete
FEM	Finite element method
f_y	Tensile strength of steel
h_n	Height of the building from the base
I	Importance Factor of Building
IMRF	Intermediate Moment Resisting Frame
Kips	Kilo pounds
MDM	Matrix Displacement Method
L	Live load
Pcf	Pounds per cubic foot
Psf	Pounds per square foot
Psi	Pounds per square inch
R	Ductility and over strength factor
T	Fundamental period of structure
UBC-9	Uniform Building Code, 1997
V	Design Base Shear
W	Service dead load+25% of service live load
Z	Seismic Zone Factor

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We also express our deep gratitude to our parents and friends for their help and encouragement.

ABSTRACT

In this project, an eight storey ductile space frame is selected. It is analyzed by Matrix Displacement Method (MDM) and Portal Frame Method for gravity and seismic analysis respectively, as defined in the books of Structural Analysis as well as used by Professional Engineers.

In the later part of the project, the same frame is analyzed by using Finite Element Method (FEM).

At the end, the results of the two methods are compared. Conclusion is;

“Selected building frame have been found balanced in respect of end moments and forces by using all the methods used individually. However difference is found, in comparison; this may be because MDM and Portal Frame Method does not consider variation of displacement/deflection along length of a member whereas FEM incorporates all possible deformations at every section of the member as well as at each joint of the frame.”

Reader of this project can understand the philosophy, technique and usage of each method as well as the possible differences that can appear in the results of classical methods when compared with the finite element method.

DEDICATION

The project is dedicated to our parents and our supervisor for helping us out during the completion of the entire project.

CHAPTER NO. 1

INTRODUCTION

1.1 GENERAL

Classical methods of structural analysis involves solution of simultaneous equations which is always a tedious and difficult task; matrix operation helps in making ease in solution of equations; things have extended in last four decades and Finite Element Method have evolved, somewhat extension of Matrix Method of Structural Analysis.

CK Wang described a Matrix Method of Analysis in his book “Intermediate Structural Analysis”^[1].

Daryl L. Logan described Finite Element Method in his book “A First Course of Finite Element Method”.^[2]

Both these books are widely in use of engineering students as well as professional structure Engineers.

In this project an effort has been made to see the difference in the analysis made by Matrix Method and that of Finite Element Method (Described by CK Wang and Logan respectively).

A model building frame is selected and analyzed by using both methods; single line diagram of frame is considered during analysis. The diaphragm effect of floor slabs are not considered in this project.

1.2 OBJECTIVES

- To analyse a given building frame subjected to Earthquake Loads by Portal Frame Method.
- To analyse a given building frame subjected to Gravity by Matrix Displacement Method.
- To analyse the same frame by using FEM.
- To compare the two results.

1.3 LIMITATIONS

- Reinforced concrete building frame.
- UBC-1997 is used for determination of seismic forces.
- Portal Frame Method is used for frame Analysis subjected to Earthquake lateral forces.

1.4 PROCEDURE

- Portal frame analysis.
- Matrix displacement analysis for gravity loads.
- Superposition of Gravity and Earthquake end Moments.
- Finite Element Analysis.
- Comparison of the calculated values.

CHAPTER NO. 2

BASIC DATA FOR ANALYSIS

2.1 MULTISTORIED BUILDING

Taking into consideration the technique of analysis the multistoried buildings are classified as:

- A high-rise structure whose height ranges between 75 feet (23m) and 491 feet (150m).
- A Skyscraper whose height is greater than 492 feet (150m).

2.2 STRUCTURAL LOADS

The types of loads specified by ACI-318 are given under.

2.2.1 GRAVITY LOADS

2.2.1.1 DEAD LOADS

Dead loads consist of the weight of all materials and fixed equipment incorporated into the building or other structure.

2.2.1.2 LIVE LOAD

Live loads are those loads produced by the use and occupancy of the building or other structure like construction load, or environmental loads such as wind load, snow load, rain load, earthquake load or flood load.

Occupancy Live Loads prescribed by American National Standard Institute (ANSI), is used in this project. **See Table 5, Appendix D.**

2.2.2 LATERAL LOADS

Lateral loads on the super structure of a building frame are generally considered due to the blowing wind and earthquake. In this project lateral earthquake forces are calculated by using UBC-97.

2.3 BUILDING DESCRIPTION

The main features of building are stated below:

- a) No. of stories = Ground+8

- b) No. of levels below ground = Zero
- c) Storey height from ground to 4th floor is 16'-0" and 4th floor to roof is 14'-0"

Plan and elevation attached in Appendix A.

2.3.1 MATERIAL PROPERTIES

$$f_c = 4000 \text{ psi}$$

$$f_y = 60000 \text{ psi}$$

$$E_c = 57000 \sqrt{f_c}$$

$$E_s = 29 \times 10^6 \text{ psi}$$

2.3.2 BUILDING FRAMING SYSTEM

Beam-Column Ductile Building Frame System is used.

2.3.3 DIMENSIONS OF ELEMENTS

Table 2.1: Dimensions of Elements

Slab	Beam	Column	Masonry
6" thick	8" x 24"	18" x 18"	13'-6" height
Length and Breadth calculated by Tributary areas		24" x 24"	11'-6" height

2.3.4 DEAD LOAD

Fig 2.1 shows integral elements of typical slab section that creates the dead load.

i. SLAB LOAD

Dead Load of Slab include

- Self-Weight
- CC Plaster
- Finishes
- Partition

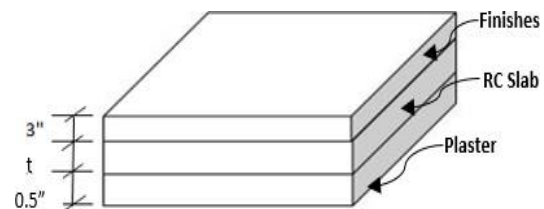


Figure 2.1: Integral Slab Element

Self-Weight Of Slab

Considering the Weight of Slab for 1 Square feet of Area

$$\text{Volume} = \frac{t}{12} \times \frac{12 \times 12}{144} = 0.08333t \text{ ft}^3 \quad \text{where,}$$

$$\gamma_c = 150 \text{ pcf}$$

- t is the thickness of Slab

$$W_{\text{self-Weight}} = V \times \gamma_c$$

$$W_{\text{self-Weight}} = 0.0833t \times 150$$

$$W_{\text{self-Weight}} = \mathbf{12.5t \text{ lb/ft}^2}$$

CC Plaster

$$\text{Volume} = \frac{0.5}{12} \times \frac{12 \times 12}{144} = 0.0416 \text{ ft}^3$$

$$\gamma_c = 145 \text{ pcf}$$

$$W_{\text{CC Plaster}} = V \times \gamma_c$$

$$W_{\text{CC Plaster}} = 0.0416 \times 145$$

$$W_{\text{CC Plaster}} = \mathbf{6.04 \text{ lb/ft}^2}$$

Finishes

$$\text{Volume} = \frac{3}{12} \times \frac{12 \times 12}{144} = 0.25 \text{ ft}^3$$

$$\gamma_c = 145 \text{ pcf}$$

$$W_{\text{Finishes}} = V \times \gamma_c$$

$$W_{\text{Finishes}} = 0.25 \times 145$$

$$W_{\text{Finishes}} = \mathbf{36.25 \text{ lb/ft}^2}$$

Partition

From Standard ACI Codes:

$$W_{\text{Partitions}} = \mathbf{30 \text{ lb/ft}^2}$$

Total Weight of Slab

$$W_{\text{slab}} = W_{\text{Partitions}} + W_{\text{Finishes}} + W_{\text{CC Plaster}} + W_{\text{self-Weight}}$$

$$W_{\text{slab}} = 30 + 36.25 + 6.04 + 12.5t$$

$$W_{\text{slab}} = 72.29 + 12.5t$$

$$\text{For } t = 6''$$

$$W_{\text{slab}} = 72.29 + 12.5(6/12)$$

$$W_{\text{slab}} = \mathbf{147.29 \text{ lb/ft}^2}$$

ii. BEAM LOAD

Considering the Weight of beam for 1 feet of length,

$$\text{Volume} = 1 \times \frac{8}{12} \times \frac{24}{12} = 1.333 \text{ ft}^3$$

$$\begin{aligned}\gamma_c &= 150 \text{ pcf} \\ W_{\text{Beam}} &= V \times \gamma_c \\ W_{\text{Beam}} &= 1.3333 \times 150 \\ W_{\text{Beam}} &= 200 \text{ lb/ft} \\ W_{\text{Beam}} &= 0.2 \text{ K/ft}\end{aligned}$$

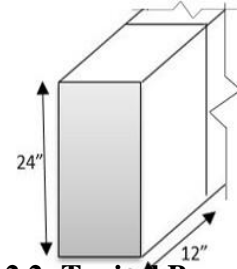


Figure 2.2: Typical Beam Section

iii. COLUMN LOAD

C1

$$\begin{aligned}\text{Volume} &= h \times \frac{18}{12} \times \frac{18}{12} = 0.444h \text{ ft}^3 \\ \gamma_c &= 150 \text{ pcf} \\ W_{c1} &= V \times \gamma_c \\ W_{c1} &= 0.444h \times 150 \\ W_{c1} &= 337.5h \text{ lb.} \\ W_{c1} &= 0.34h \text{ Kips}\end{aligned}$$

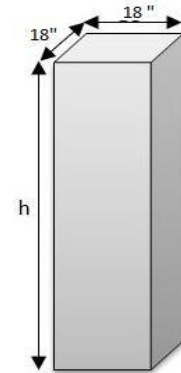


Figure 2.3: Typical Column

C2

$$\begin{aligned}\text{Volume} &= h \times \frac{24}{12} \times \frac{24}{12} = 4h \text{ ft}^3 \\ \gamma_c &= 150 \text{ pcf} \\ W_{c1} &= V \times \gamma_c \\ W_{c1} &= 4h \times 150 \\ W_{c1} &= 600h \text{ lb.} \\ W_{c1} &= 0.6h \text{ Kips}\end{aligned}$$

Section (C1)

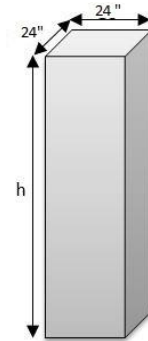


Figure 2.4: Typical Column

Section (C2)

iv. MASONRY LOAD

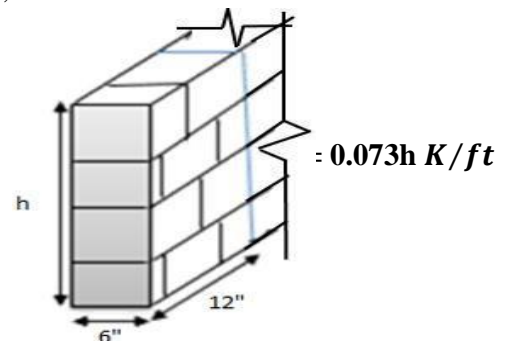
Considering the Weight of Masonry for 1 feet of length,

$$\text{Volume} = 1 \times \frac{6}{12} \times h = 0.5h \text{ ft}^3$$

Where,

- h is the height of Masonry Wall

$$\begin{aligned}\gamma_c &= 145 \text{ pcf} \\ W_{\text{Masonry}} &= V \times \gamma_c \\ W_{\text{Masonry}} &= 0.5h \times 145 \\ W_{\text{Masonry}} &= 72.5h\end{aligned}$$



**Figure 2.5: Typical
Masonry Wall**

2.3.5 LIVE LOAD

Live load= 70 psf (Table 5, Appendix D)

2.3.6 WEIGHT OF BUILDING

Total load of the building is calculated manually consisting of dead and live load as shown in the table below:

Table 2.2: Weight of Building

Total Load For Floor 1				Commulative Load			
D.L		L.L		D.L		L.L	
Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)
46.927	56.3124	8.84	14.144	349.059	418.3842	70.72	113.132
74.23	89.076	16.45	26.32	557.158	668.473	131.6	210.56
74.23	89.076	16.45	26.32	557.158	668.473	131.6	210.56
46.927	56.3124	8.84	14.144	349.059	418.3842	70.72	113.132
75.67	90.804	16.56	26.496	567.568	680.927	132.48	211.938
121.2	145.44	30.8	49.28	917.03	1100.39	246.4	394.24
121.2	145.44	30.8	49.28	917.03	1100.39	246.4	394.24
75.67	90.804	16.56	26.496	567.568	680.927	132.48	211.938
75.67	90.804	16.56	26.496	567.568	680.927	132.48	211.938
121.2	145.44	30.8	49.28	917.03	1100.39	246.4	394.24
121.2	145.44	30.8	49.28	917.03	1100.39	246.4	394.24
75.67	90.804	16.56	26.496	567.568	680.927	132.48	211.938
46.927	56.3124	8.84	14.144	349.059	418.3842	70.72	113.132
74.23	89.076	16.45	26.32	557.158	668.433	131.6	210.56
74.23	89.076	16.45	26.32	557.158	668.433	131.6	210.56
46.927	56.3124	8.84	14.144	349.059	418.3842	70.72	113.132
1272.108	1526.5296	290.6	464.96	9563.26	11472.6168	2324.8	3719.48

2.4 SEISMIC DESIGN REQUIREMENTS

Seismic design parameters are taken from UBC-97.

2.4.1 BASE SHEAR

It is an estimate of the maximum expected lateral force that will occur due to seismic ground motion at the base of the structure.

$$\text{Base Shear can be calculated as, } V = \frac{C_v \times I}{R \times T} \times W \quad (\text{Eq. 2.1})$$

2.4.1.1 BASE SHEAR CALCULATION

Summary of the base shear calculation is shown under.

Table 2.3: Base Shear Calculation

Seismic Zone	2B	-	-
Soil Profile	S_c	-	-
Seismic Zone Factor	Z	0.2	UBC1997,Table 16-I
Seismic importance factor	I	1	UBC1997,Table 16-K
Structural system factor (Moment Resisting Concrete Frame)	R	8.5	UBC1997,Table 16-N
Seismic Coefficient	C_v	0.32	UBC1997,Table 16-R
Seismic coefficient for time period	C_t	0.03	For Concrete moment Frames
Height of Building in ft.	h_n	120	-
Building Period in Seconds	T=C_txh_n^{3/4}	1.088	Eq. 2.7
Weight of building in Kips	W	10108.4	-
Base Shear in Kips	V=(C_vI/RT)xW	353.794	UBC (Eq.30.4)

Note: All the tables of UBC-1997 are attached in appendix D.

2.4.2 STOREY FORCES

Static Base Shear Force is distributed along the height of building at each story level using the relation given under.

$$F_x = \frac{(V-F_t)(W_x \times h_x)}{\sum(W_x \times h_x)} \quad \text{UBC-97, Eq.30-15} \quad \text{(Eq. 2.3)}$$

Where,

V = Base shear

F_t = Extra force at the top

W_x = Portion of total weight acting on each floor

h_x = Height of each floor

Table 2.4: Storey force

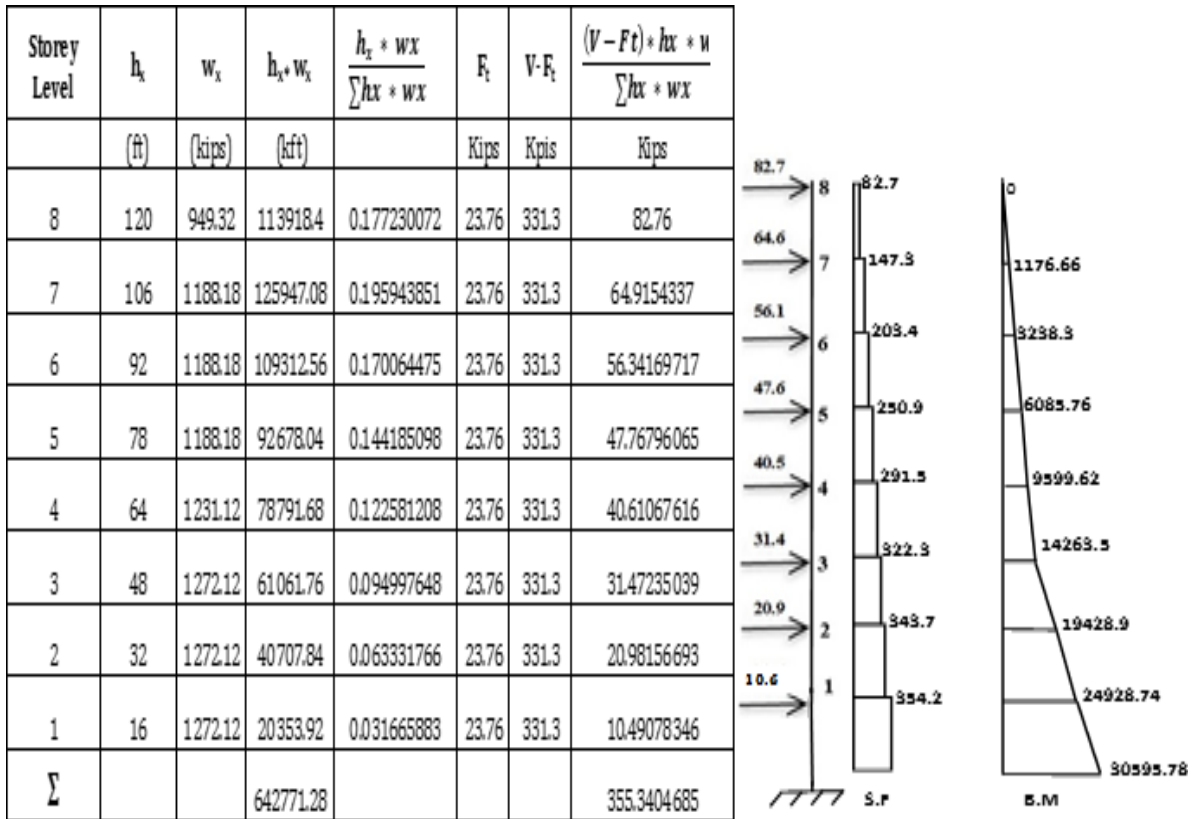


Figure 2.6: SF and BM at Each Storey

2.5 TORSION CHECK

To check whether the building is under action of torsion with respect to the vertical axis of the building frame, the location of centre of mass and centre of rigidity has been calculated; calculation is given under.

2.5.1 CENTRE OF MASS

The point where the entire weight of a body is concentrated such that if the body is supported at this point, it will remain in equilibrium in any position. It is calculated as under,

$$COM = \frac{\Sigma(\text{Moment of Area})}{\Sigma \text{Area}} \quad (\text{Eq. 2.4})$$

$$X_m = 33 \text{ ft}$$

$$Y_m = 30 \text{ ft}$$

2.5.2 CENTRE OF RIGIDITY

Resistance of the floor and of the building subjected to external lateral loads is created at the center of rigidity. In other words the total stiffness of the floor as well as of the building concentrates at the Centre of rigidity. It is calculated by the following formula;

$$COR = \frac{\Sigma(\text{Moment of } I)}{\Sigma(I)} \quad (\text{Eq. 2.5})$$

Where; I is the moment of inertia of columns

$$X_r = 33 \text{ ft}$$

$$Y_r = 30 \text{ ft}$$

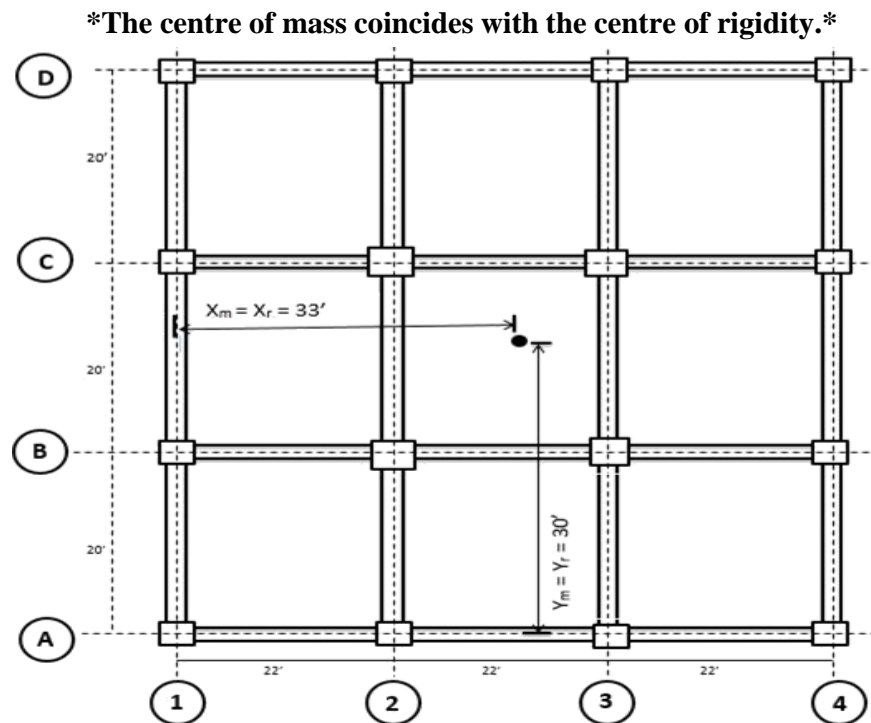


Figure 2.7: Location of Center of Rigidity and Center of Mass

CHAPTER NO. 3

THEORY OF ANALYSIS

The techniques of analysis used in this project for given building frame are;

- 1) Matrix Displacement Method described by CK Wang in his book, “Intermediate Structural Analysis”.
- 2) Finite Element Method described by Daryl L. Logan in his book, “A First Course in Finite Element Method”.

3.1 APPROACH OF THE MATRIX DISPLACEMENT METHOD

Matrix Displacement Method can be applied for analysis by any one of the following approaches.

A. FIRST PRINCIPLE APPROACH

- 1) Displacement matrix, [B]
- 2) Static matrix, [A]
- 3) Element stiffness matrix, [S]
- 4) Global matrix, $[K] = [A] \times [S] \times [B] = [ASB]$
- 5) Inverse of Global matrix, $[K]^{-1}$
- 6) Load matrix, [P]
- 7) Fixed end moment matrix, $[F_0]$
- 8) Joint displacement matrix, $[X] = [K]^{-1} [P]$
- 9) Force matrix, $[F] = [S] \times [B] \times [X]$
- 10) End forces, $[F^*] = [F] + [F_0]$
- 11) Member displacement matrix, $[e] = [B] \times [X]$

B. DIRECT STIFFNESS APPROACH

- 1) Local stiffness matrix of an element, [k]
- 2) Transformation of local matrices to global matrix, [K]
- 3) Inverse of global matrix, $[K]^{-1}$
- 4) Fixed end moment matrix, $[F_0]$
- 5) Load matrix, [P]
- 6) Joint displacement matrix, $[X] = [K]^{-1} [P]$

- 7) Member displacement matrix, [e]
- 8) Element stiffness matrix, [S]
- 9) Force matrix, [F]=[S]×[e]
- 10) End forces, [F*]=[F]+[F_o]

Direct stiffness approach is used for analysis in this project

3.1.1 DIRECT STIFFNESS APPROACH

1) LOCAL STIFFNESS MATRIX OF AN ELEMENT

CK Wang Considered a flexural member having four degrees of freedom is shown under.

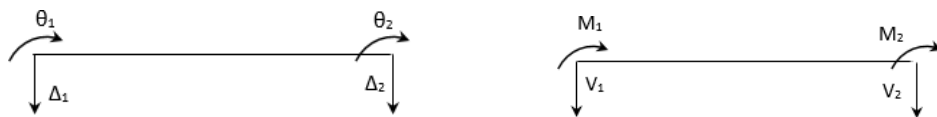


Figure 3.1: Degree of Freedom of a member

Standard local stiffness matrix for a flexural member is given under.

Figure 3.2: Typical Local Stiffness Matrix for Flexural Member

	θ_1	θ_2	Δ_1	Δ_2
M_1	$4EI/L$	$2EI/L$	$6EI/L^2$	$-6EI/L^2$
M_2	$2EI/L$	$4EI/L$	$6EI/L^2$	$-6EI/L^2$
V_1	$6EI/L^2$	$6EI/L^2$	$12EI/L^3$	$-12EI/L^3$
V_2	$-6EI/L^2$	$-6EI/L^2$	$-12EI/L^3$	$12EI/L^3$

2) TRANSFORMATION TO GLOBAL STIFFNESS MATRIX

The Global stiffness matrix for the whole structure is determined through transformation of local matrices.

3) LOAD MATRIX

Load matrix is obtained by considering the load applied directly to the joint and by converting the span load to joint loads through fixed end moment calculation.

4) FIXED END MOMENT MATRIX

The matrix is developed by determining the fixed end moments at the joints of the members.

5) MEMBER DISPLACEMENT MATRIX

The matrix is developed by considering the joint displacement at the ends of each member.




6) MEMBER STIFFNESS MATRIX

The stiffness matrix expresses the forces in members and it is a square matrix.

$$S = \frac{EI}{L}$$

Calculation of each step is shown in Appendix C.

3.1.2 CONVENTIONS OF MATRIX DISPLACEMENT METHOD

	Considered Positive
	Considered Positive
	Considered Positive
L	Local degree of freedom
G	Global degree of freedom
K	Global stiffness matrix
K	Local stiffness matrix

3.2 FINITE ELEMENT METHOD

The finite element method is a numerical method for solving problems of engineering and mathematical physics. Problems involving complicated geometrics, loadings and material properties, require solution of a series of ordinary or partial differential equations, that need a cumbersome calculations and sometimes solution may not be achieved as desired. Hence there is need to rely on numerical methods, such as the finite element method, for acceptable solutions.

3.2.1 APPROACH OF THE FINITE ELEMENT METHOD

Typically, for the structural stress-analysis problem, determination of end displacements and end forces due to applied loads is the core issue.

There are two general approaches associated with the finite element method. One approach, called the force, or flexibility method, uses internal forces as the unknown of the problem. The second approach, called the displacement, or stiffness method, assumes the displacements of the

nodes as the unknowns of the problem. Therefore, the fundamental approach of FEM is to formulate equations of “Compatibility of Deformation” and “Equilibrium of Forces” at ends (nodes) of a structural member.

3.2.1.1 PROCEDURE

Procedure for Analysis through Finite Element Method, defined by Logan, adopted in this project, can be summarised as,

1. Divide the member in to finite elements with predefined interconnected nodes.
2. Global degree of freedom
3. Local degree of freedom
4. Load matrix (with respect to global axis)
5. Element global stiffness matrix. [k]

Element stiffness matrix with respect to global axes is given by following matrix.

Figure 3.3: Typical Element Stiffness Matrix

	\hat{d}_{ix}	\hat{d}_{iy}	$\hat{\phi}_i$	\hat{d}_{jx}	\hat{d}_{jy}	$\hat{\phi}_j$
\hat{d}_{ix}	$AC^2 + \frac{12I}{L^2} S^2$	$(A - \frac{12I}{L^2}) CS$	$\frac{6I}{L} S$	$-(A - \frac{12I}{L^2}) CS$	$(A - \frac{12I}{L^2}) CS$	$-\frac{6I}{L} S$
\hat{d}_{iy}	$(A - \frac{12I}{L^2}) CS$	$AS^2 + \frac{12I}{L^2} C^2$	$\frac{6I}{L} C$	$-(A - \frac{12I}{L^2}) CS$	$-(A - \frac{12I}{L^2}) CS$	$\frac{6I}{L} C$
$\hat{\phi}_i$	$-\frac{6I}{L} S$	$\frac{6I}{L} C$	$4I$	$\frac{6I}{L} S$	$-\frac{6I}{L} S$	$2I$
\hat{d}_{jx}	$-(A - \frac{12I}{L^2}) CS$	$(A - \frac{12I}{L^2}) CS$	$\frac{6I}{L} S$	$AC^2 + \frac{12I}{L^2} S^2$	$(A - \frac{12I}{L^2}) CS$	$\frac{6I}{L} S$
\hat{d}_{jy}	$(A - \frac{12I}{L^2}) CS$	$-(A - \frac{12I}{L^2}) CS$	$\frac{6I}{L} C$	$(A - \frac{12I}{L^2}) CS$	$AS^2 + \frac{12I}{L^2} C^2$	$-\frac{6I}{L} C$
$\hat{\phi}_j$	$-\frac{6I}{L} S$	$\frac{6I}{L} C$	$2I$	$\frac{6I}{L} S$	$-\frac{6I}{L} C$	$4I$

$\times E/L$

Where;

A= Area of Member I= Moment of Inertia of Member
 L= Span length of Member C= Cos θ S= Sin θ

6. Assembly of all defined element to obtain the global or total Stiffness Matrix [K]
7. Force-Displacement Relationship.

Force – displacement relationship is given by following equation

$$F = K \cdot d$$

or

$$d = K^{-1} \cdot F$$

8. Solve for the Displacements
9. Element local stiffness matrix $[\hat{k}]$

Figure 3.4: Typical Element Local Stiffness Matrix

\hat{d}_{ix}	\hat{d}_{iy}	$\hat{\Phi}_i$	\hat{d}_{jx}	\hat{d}_{jy}	$\hat{\Phi}_j$	
C_1	0	0	$-C_1$	0	0	\hat{d}_{ix}
0	$12C_2$	$6C_2L$	0	$-12C_2$	$-6C_2L$	\hat{d}_{iy}
0	$6C_2L$	$4C_2L^2$	0	$-6C_2L$	$-4C_2L^2$	$\hat{\Phi}_i$
$-C_1$	0	0	C_1	0	0	\hat{d}_{jx}
0	$-12C_2$	$-6C_2L$	0	$12C_2$	$6C_2L$	\hat{d}_{jy}
0	$-6C_2L$	$-4C_2L^2$	0	$6C_2L$	$4C_2L^2$	$\hat{\Phi}_j$

Where;

$$C_1 = \frac{AE}{L} \quad ; \quad C_2 = \frac{EI}{L^3}$$

10. Element local forces $[\hat{f}]$

$\hat{f} \quad \hat{f}$

$$f = k \cdot [T d]$$

where;



T= Transformation matrix

Figure 3.5: Transformation Matrix

C	S	0	0	0	0
	C	0	0	0	0
0	0	1	0	0	0
0	0	0	C	S	0
0	0	0		C	0
0	0	0	0	0	1

11. Free Body Diagram.

3.2.2 CONVENTIONS OF FINITE ELEMENT METHOD

 Considered Positive
 Considered Positive

K Global stiffness matrix
^

CHAPTER NO. 4 SIMULATION

4.1 GENERAL

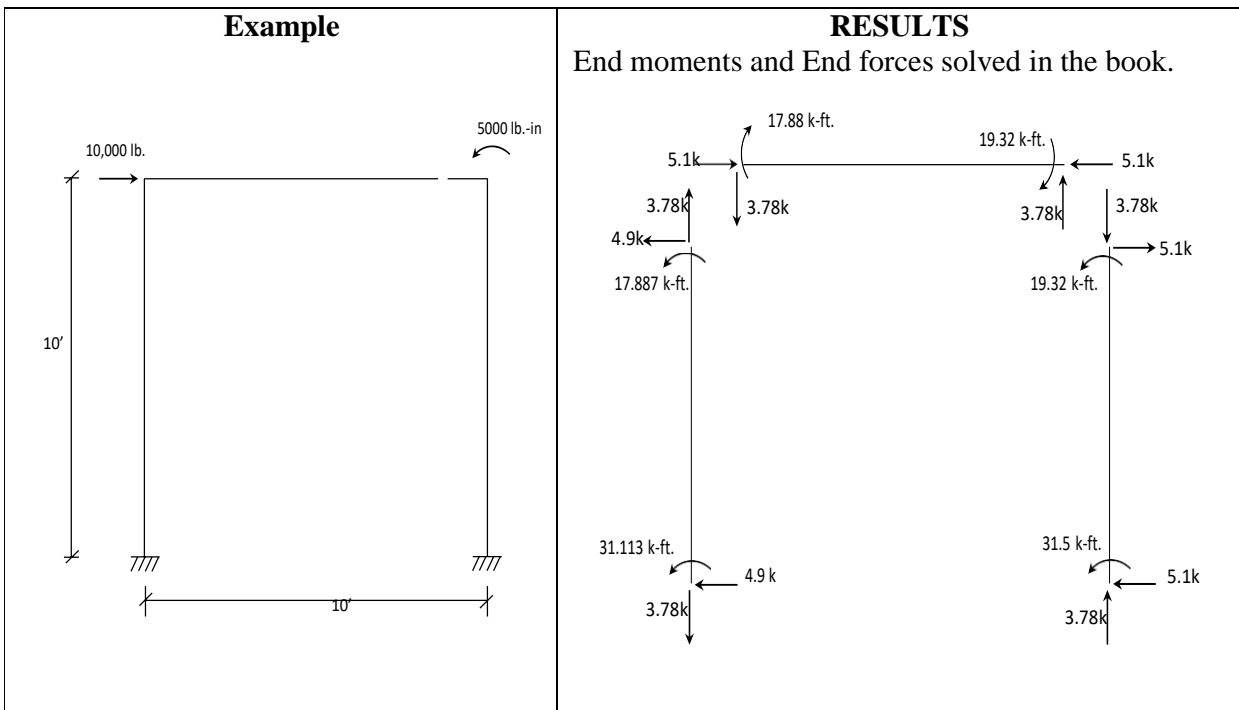
Prior to start of work on the given building frame model, two solved examples are selected.

1. An **example 5.1** of the Finite Element Method is taken from the book of Daryl L. Logan and is re-analyzed by Matrix Displacement Method described by CK Wang.
2. An **example 12.3.4** of Matrix Displacement Method is taken from the book of CK Wang and is re-analyzed by Finite Element Method described by Daryl L. Logan.

4.1.1 SINGLE STOREY FRAME SYSTEM

a. Example (5.1), from Daryl L. Logan

Single Storey frame **Example: 5.1** selected from the book “A First Course in Finite Element Method” by Daryl L. Logan is given under.



4.1.1.1 REANALYSIS BY MATRIX DISPLACEMENT METHOD

The above example is solved using Matrix Displacement Method the Steps involved for solution are;

1) LOCAL STIFFNESS MATRIX

$$K_1 = \begin{matrix} & \text{Element 1} \\ & \begin{matrix} \text{L1} & \text{L2(G1)} & \text{L3} & \text{L4(G3)} \end{matrix} \\ \begin{matrix} \text{L1} \\ \text{L2(G1)} \\ \text{L3} \\ \text{L4(G3)} \end{matrix} & \begin{bmatrix} 0.8 & 0.4 & 0.12 & -0.12 \\ 0.4 & 0.8 & 0.12 & -0.12 \\ 0.12 & 0.12 & 0.024 & -0.024 \\ -0.12 & -0.12 & -0.024 & 0.024 \end{bmatrix} \end{matrix} \times EI$$

$$K_2 = \begin{matrix} & \text{Element 2} \\ & \begin{matrix} \text{L1(G1)} & \text{L2(G2)} & \text{L3} & \text{L4} \end{matrix} \\ \begin{matrix} \text{L1(G1)} \\ \text{L2(G2)} \\ \text{L3} \\ \text{L4} \end{matrix} & \begin{bmatrix} 0.4 & 0.2 & 0.06 & -0.06 \\ 0.2 & 0.4 & 0.06 & -0.06 \\ 0.06 & 0.06 & 0.012 & -0.012 \\ -0.06 & -0.06 & -0.012 & 0.012 \end{bmatrix} \end{matrix} \times EI$$

$$K_3 = \begin{matrix} & \text{Element 3} \\ & \begin{matrix} \text{L1} & \text{L2(G2)} & \text{L3} & \text{L4(G3)} \end{matrix} \\ \begin{matrix} \text{L1} \\ \text{L2(G2)} \\ \text{L3} \\ \text{L4(G3)} \end{matrix} & \begin{bmatrix} 0.8 & 0.4 & 0.12 & -0.12 \\ 0.4 & 0.8 & 0.12 & -0.12 \\ 0.12 & 0.12 & 0.024 & -0.024 \\ -0.12 & -0.12 & -0.024 & 0.024 \end{bmatrix} \end{matrix} \times EI$$

2) GLOBAL STIFFNESS MATRIX

$$K = \begin{matrix} & \begin{matrix} \text{G1} & \text{G2} & \text{G3} \end{matrix} \\ \begin{matrix} \text{G1} \\ \text{G2} \\ \text{G3} \end{matrix} & \begin{bmatrix} 1.2 & 0.2 & -0.12 \\ 0.2 & 1.2 & -0.12 \\ -0.12 & -0.12 & 0.048 \end{bmatrix} \end{matrix} \times EI$$

3) INVERSE OF GLOBAL MATRIX [K⁻¹]

$$K^{-1} = \begin{array}{c|ccc} & G1 & G2 & G3 \\ \hline G1 & 1.125 & 0.125 & 3.125 \\ G2 & 0.125 & 1.125 & 3.125 \\ G3 & 3.125 & 3.125 & 36.45833 \end{array} \times 1/EI$$

4) LOAD MATRIX [P]

$$P = \begin{array}{c|c} P_1 & 0 \\ P_2 & -0.4167 \\ P_3 & 10 \end{array} \begin{array}{l} \text{Kip} \\ \text{Kft} \\ \text{Kip} \end{array}$$

5) DEFORMATION MATRIX [B]

$$[e] = [B][X]$$

$$B = \begin{array}{c|ccc} & 0 & 0 & -0.1 \\ & 1 & 0 & -0.1 \\ & 1 & 0 & 0 \\ & 0 & 1 & 0 \\ & 0 & 1 & -0.1 \\ & 0 & 0 & -0.1 \end{array}$$

6) JOINT ROTATION [X]

$$X = \begin{array}{c|c} X_1 & 3.12E+01 \\ X_2 & 3.08E+01 \\ X_3 & 3.63E+02 \end{array} \times 1/EI \begin{array}{l} \text{Radian} \\ \text{Radian} \\ \text{Inches} \end{array}$$

7) FORCE MATRIX [F*]

$$F = \begin{array}{c|c} F_1 & -31.1146 \\ F_2 & -18.6354 \\ F_3 & 18.6354 \\ F_4 & 18.5521 \\ F_5 & -18.9688 \\ F_6 & -31.2813 \end{array}$$

Note: All Values are in K-ft

8) FREE BODY DAIGRAM

The end forces and moments for the frame re-analysed by Matrix displacement method is shown under.

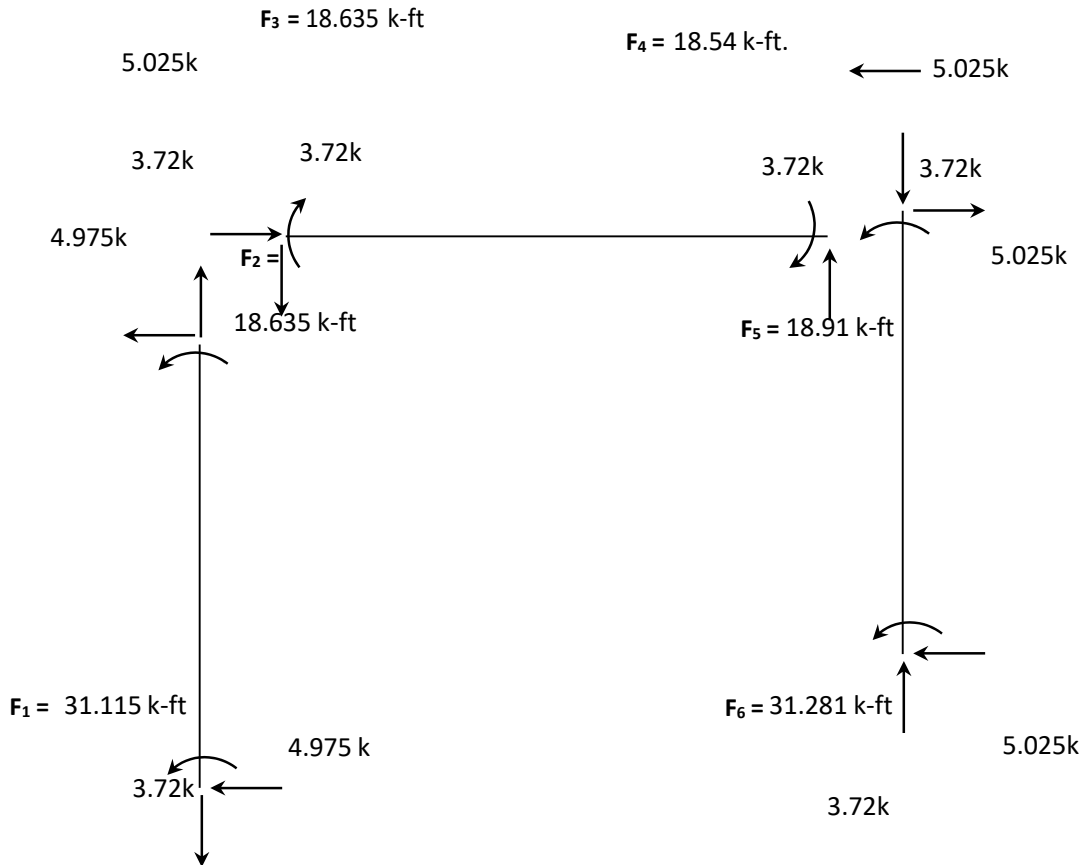


Figure 4.1: Results from Matrix Displacement Method

4.1.1.2 COMPARISON OF RESULTS

Comparison b/w FEM and MDM												
Joints	Fx				Fy				Moment			
	MDM	FEM	Difference	%age accuracy	MDM	FEM	Difference	%age accuracy	MDM	FEM	Difference	%age accuracy
A	-4.95	-4.9	-0.05	98.97959184	-3.72	-3.78	0.06	98.41269841	-31.115	-31.113	-0.002	99.99357182
B ₁	4.95	4.9	0.05	98.97959184	3.72	3.78	-0.06	98.41269841	-18.635	-17.887	-0.748	95.81819198
B ₂	5.025	5.1	-0.075	98.52941176	-3.72	-3.78	0.06	98.41269841	18.635	17.88	0.755	95.77740492
C ₁	-5.025	-5.1	0.075	98.52941176	3.72	3.78	-0.06	98.41269841	18.52	19.92	-1.4	92.97188755
C ₂	5.025	5.1	-0.075	98.52941176	-3.72	-3.78	0.06	98.41269841	-18.961	-19.32	0.359	98.14182195

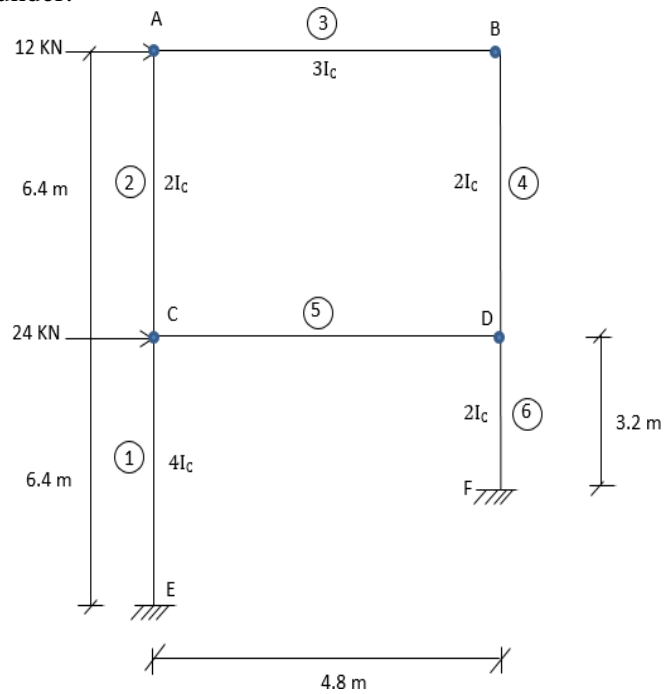
D	-5.025	-5.1	0.075	98.52941176	3.72	3.78	-0.06	98.41269841	-31.2813	-31.5667	0.2853667	99.09598733
---	--------	------	-------	-------------	------	------	-------	-------------	----------	----------	-----------	-------------

Note: All 'F' values in Kips and 'M' values in kip-feet.

4.1.2 DOUBLE STOREY FRAME SYSTEM

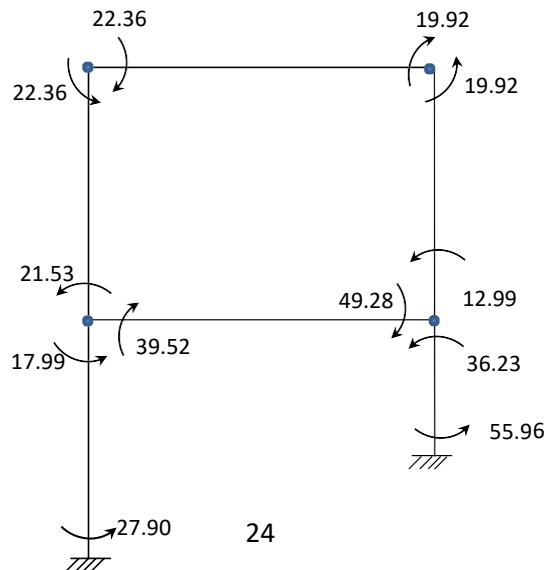
b. Example (12.3.4), from CK Wang

A double Storey frame system selected from the book “Intermediate Structures” by CK Wang is given under.



RESULTS

Solution of example reproduced under. (All Results are in kN-m)



4.1.2.1 REANALYSIS BY FINITE ELEMENT METHOD

The double Storey Frame is solved by using Finite Element Method the Steps involved for solution are;

1) GLOBAL DISPLACEMENT

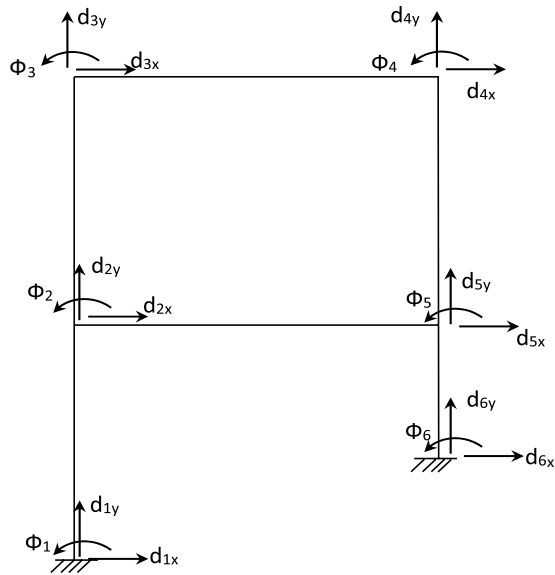


Figure 4.2: Global displacements

2) LOCAL DISPLACEMENT

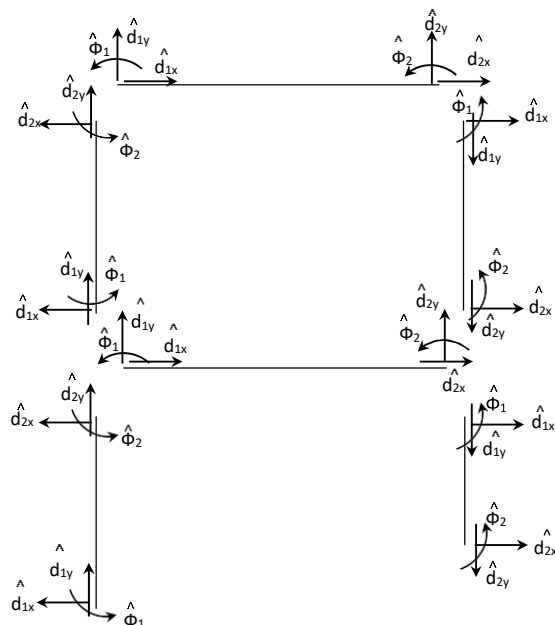


Figure 4.3: Local displacements

3) LOAD MATRIX

F_{2X}	=	24
F_{2Y}	=	0
M_2	=	0
F_{3X}	=	12
F_{3Y}	=	0
M_3	=	0
F_{4X}	=	0
F_{4Y}	=	0
M_4	=	0
F_{5X}	=	0
F_{5Y}	=	0
M_5	=	0

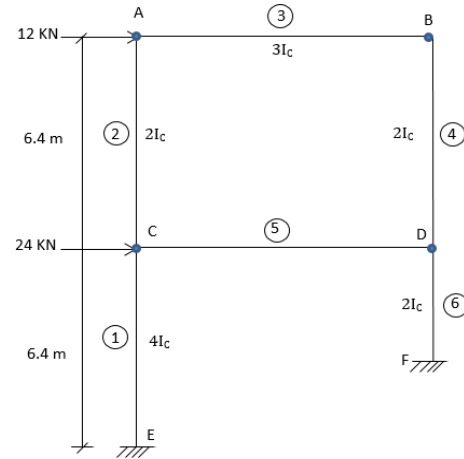


Figure 4.4: Load Diagram

Note: All 'F' values are in Kips and 'M' values in kip-feet.

4) ELEMENT STIFFNESS MATRIX

Element 1						
	1	1	1	2	2	2
	dix	diy	Φ_i	djx	djx	Φ_j
K =	2812500	0	0	-2812500	0	0
	0	24719.24	79101.56	0	-24719.2	79101.56
	0	79101.56	337500	0	-79101.6	168750
	-2812500	0	0	2812500	0	0
	0	-24719.2	-79101.6	0	24719.24	-79101.6
	0	79101.56	168750	0	-79101.6	337500

Element 2						
	2	2	2	3	3	3
	dix	diy	Φ_i	djx	djx	Φ_j
K =	2812500	0	0	-2812500	0	0
	0	12359.62	39550.78	0	-12359.6	39550.78
	0	39550.78	168750	0	-39550.8	84375
	-2812500	0	0	2812500	0	0
	0	-12359.6	-39550.8	0	12359.62	-39550.8
	0	39550.78	84375	0	-39550.8	168750

Element 3						
3	3	3	4	4	4	
dix	diy	Φ_i	djx	djx	Φ_j	
3750000	0	0	-3750000	0	0	dix 3
0	43945.31	105468.8	0	-43945.3	105468.8	diy 3
0	105468.8	337500	0	-105469	168750	Φ_i 3
-3750000	0	0	3750000	0	0	djx 4
0	-43945.3	-105469	0	43945.31	-105469	djx 4
0	105468.8	168750	0	-105469	337500	Φ_j 4

Element 4						
4	4	4	5	5	5	
dix	diy	Φ_i	djx	djx	Φ_j	
2812500	0	0	-2812500	0	0	dix 4
0	12359.62	39550.78	0	-12359.6	39550.78	diy 4
0	39550.78	168750	0	-39550.8	84375	Φ_i 4
-2812500	0	0	2812500	0	0	djx 5
0	-12359.6	-39550.8	0	12359.62	-39550.8	djx 5
0	39550.78	84375	0	-39550.8	168750	Φ_j 5

Element 5						
2	2	2	5	5	5	
dix	diy	Φ_i	djx	djx	Φ_j	
3750000	0	0	-3750000	0	0	dix 2
0	43945.31	105468.8	0	-43945.3	105468.8	diy 2
0	105468.8	337500	0	-105469	168750	Φ_i 2
-3750000	0	0	3750000	0	0	djx 5
0	-43945.3	-105469	0	43945.31	-105469	djx 5
0	105468.8	168750	0	-105469	337500	Φ_j 5

Element 6						
5	5	5	6	6	6	
dix	diy	Φ_i	djx	djx	Φ_j	
5625000	0	0	-5625000	0	0	dix 5
0	98876.95	158203.1	0	-98877	158203.1	diy 5
0	158203.1	337500	0	-158203	168750	Φ_i 5
-5625000	0	0	5625000	0	0	djx 6
0	-98877	-158203	0	98876.95	-158203	djx 6
0	158203.1	168750	0	-158203	337500	Φ_j 6

5) MODIFIED GLOBAL ELEMENT STIFFNESS MATRIX

The transformed global matrix of 18*18 is reduced to 12*12 after applying boundary conditions and is shown below.

[K] =

	2	2	2	3	3	3	4	4	4	4	5	5	5		
	dix	diy	Φi	djx	djx	Φj	dix	diy	Φi	djx	djx	Φj			
	3787078.857	0	39550.78125	-12359.61914	0	-39550.78125	0	0	0	-3750000	0	0	0	2	dix
	0	5668945.313	105468.75	0	-2812500	0	0	0	0	0	-43945.3125	105468.75	0	2	diy
	39550.78125	105468.75	843750	39550.78125	0	84375	0	0	0	0	-105468.75	168750	0	2	Φi
	-12359.61914	0	39550.78125	3762359.619	0	39550.78125	-3750000	0	0	0	0	0	0	3	djx
	0	-2812500	0	0	2856445.313	105468.75	0	-43945.3125	105468.75	0	0	0	0	3	djx
	-39550.78125	0	84375	39550.78125	105468.75	506250	0	-105468.75	168750	0	0	0	0	3	Φj
	0	0	0	-3750000	0	0	3762359.619	0	-39550.78125	-12359.61914	0	-39550.78125	0	4	dix
	0	0	0	0	-43945.3125	-105468.75	0	2856445.313	-105468.75	0	-2812500	0	0	4	diy
	0	0	0	0	105468.75	168750	-39550.78125	-105468.75	506250	39550.78125	0	84375	0	4	Φi
	-3750000	0	0	0	0	0	-12359.61914	0	39550.78125	3861236.572	0	-118652.3438	0	5	djx
	0	-43945.3125	-105468.75	0	0	0	0	-2812500	0	0	8481445.313	-105468.75	0	5	djx
	0	105468.75	168750	0	0	0	-39550.78125	0	84375	-118652.3438	-105468.75	843750	0	5	Φj

6) FORCE – DISPLACEMENT RELATIONSHIP

“Force Displacement” relationship is given as,

$$F = k \cdot d$$

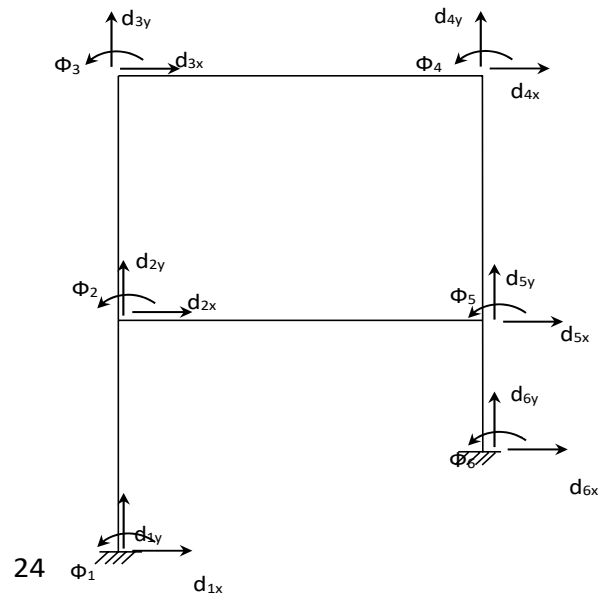
or

$$d = K^{-1} \cdot F$$

DISPLACEMENT MATRIX

[D] =

0	d1x
0	d1y
0	Φ1
0.000682	d2x
-1.7E-06	d2y
-0.00016	Φ2
0.00219	d3x
-1.5E-06	d3y
-0.00013	Φ3
0.002189	d4x
6.12E-07	d4y
0.000126	Φ4
0.000674	d5x
8.58E-07	d5y
0.000218	Φ5
0	d6x
0	d6y
0	Φ6



Global Displacements

Note: All 'd' values are in feet and 'ϑ' values in radians.

7) ELEMENT LOCAL FORCES

From the global displacements the local forces in elements are obtained by the following equation

$$\hat{f} = \hat{k} \cdot \hat{T} \cdot d$$

$$f_1 =$$

ELEMENT 1		
4.824104	fix	1
3.820342	fiy	1
26.12018	mi	1
-4.8241	fjx	2
-3.82034	fjx	2
-1.66999	mj	2

$$f_2 =$$

ELEMENT 2		
-0.690032	fix	2
6.9066325	fiy	2
20.727985	mi	2
0.6900323	fjx	3
-6.906632	fjx	3
23.474463	mj	3

$$f_3 =$$

ELEMENT 3		
5.093368	fix	3
-0.69003	fiy	3
-23.4745	mi	3
-5.09337	fjx	4
0.690032	fjx	4
20.16231	mj	4

$$f_4 =$$

ELEMENT 4		
-0.69003	fix	4
-5.09337	fiy	4
-20.1623	mi	4
0.690032	fjx	5
5.093368	fjx	5
-12.4352	mj	5

$$f_5 =$$

ELEMENT 5		
27.08629	fix	2
5.5141364	fiy	2
-19.058	mi	2
-27.08629	fjx	5
-5.514136	fjx	5
45.525853	mj	5

$$f_6 =$$

ELEMENT 6		
4.824104	fix	5
-32.1797	fiy	5
-33.0906	mi	5
-4.8241	fjx	6
32.17966	fjx	6
-69.8843	mj	6

Note: All 'F' values in Kips and 'M' values in kip-feet.

8) RESULTS FROM FEM

All units are in KN-m.

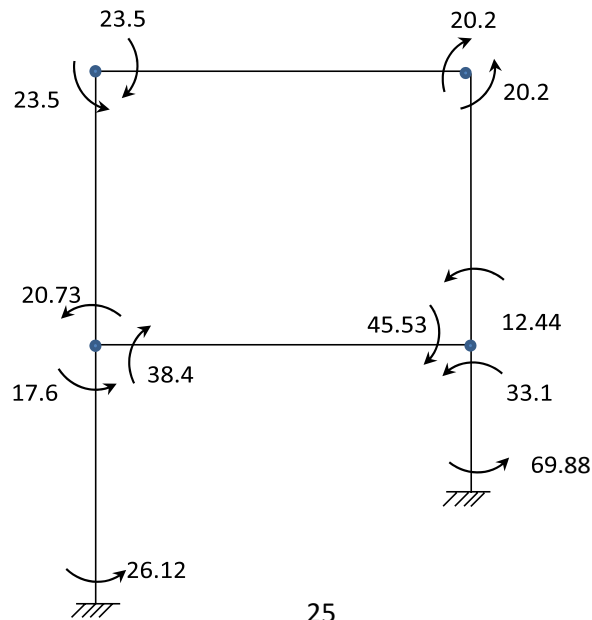


Figure 4.5: Results from FEM

4.1.2.2 COMPARISON OF RESULTS

Comparison Between FEM and MDM				
S.No	Moment			
	MDM	FEM	Difference	%age accuracy
MEMBER 1				
i) Joint E	-27.9	-26.12	-1.78	93.18529862
ii) Joint C	-17.99	-17.6	-0.39	97.78409091
MEMBER 2				
i) Joint C	-21.53	-20.73	-0.8	96.14085866
ii) Joint A	-22.36	-23.5	1.14	95.14893617
MEMBER 3				
i) Joint A	22.36	23.5	-1.14	95.14893617
ii) Joint B	19.92	20.2	-0.28	98.61386139
MEMBER 4				
i) Joint B	-19.92	-20.2	0.28	98.61386139
ii) Joint D	-12.99	-12.44	-0.55	95.57877814
MEMBER 5				
i) Joint C	39.52	38.4	1.12	97.08333333
ii) Joint D	49.28	45.53	3.75	91.7636723
MEMBER 6				
i) Joint D	-36.23	-33.1	-3.13	90.54380665
ii) Joint F	-55.96	-69.88	13.92	80.08013738

Note: All values are in kip-feet.

CHAPTER NO. 5

FRAME ANALYSIS

5.1 ANALYSIS THROUGH CLASSICAL METHOD

5.1.1 EARTHQUAKE ANALYSIS

5.1.1.1 PORTAL FRAME METHOD

Through portal frame method, end moments and shear forces of Beams and Columns are calculated. Assumptions for portal frame method are:

- i) Column shear in interior column is always doubled of that of exterior column
- ii) Point of contra-flexure lies at mid span of Columns and Beams.

The output for frame A is shown under.

a) SHEAR FORCE

The shear force in column is determined using storey shear and is transferred to the beams using the moments.

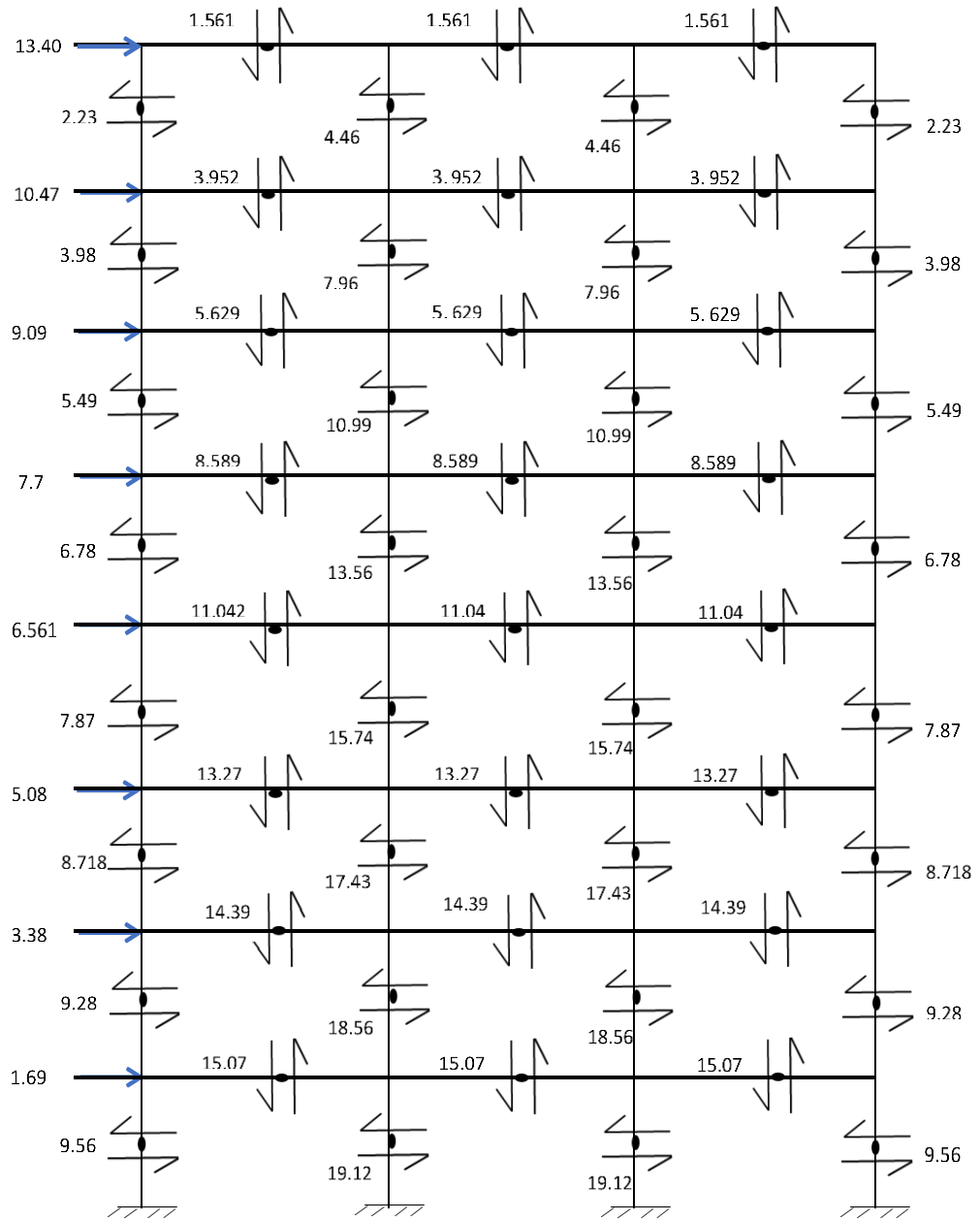


Figure 5.1: Shear Distribution (kips)

b) END MOMENTS

The end moment is shown under.

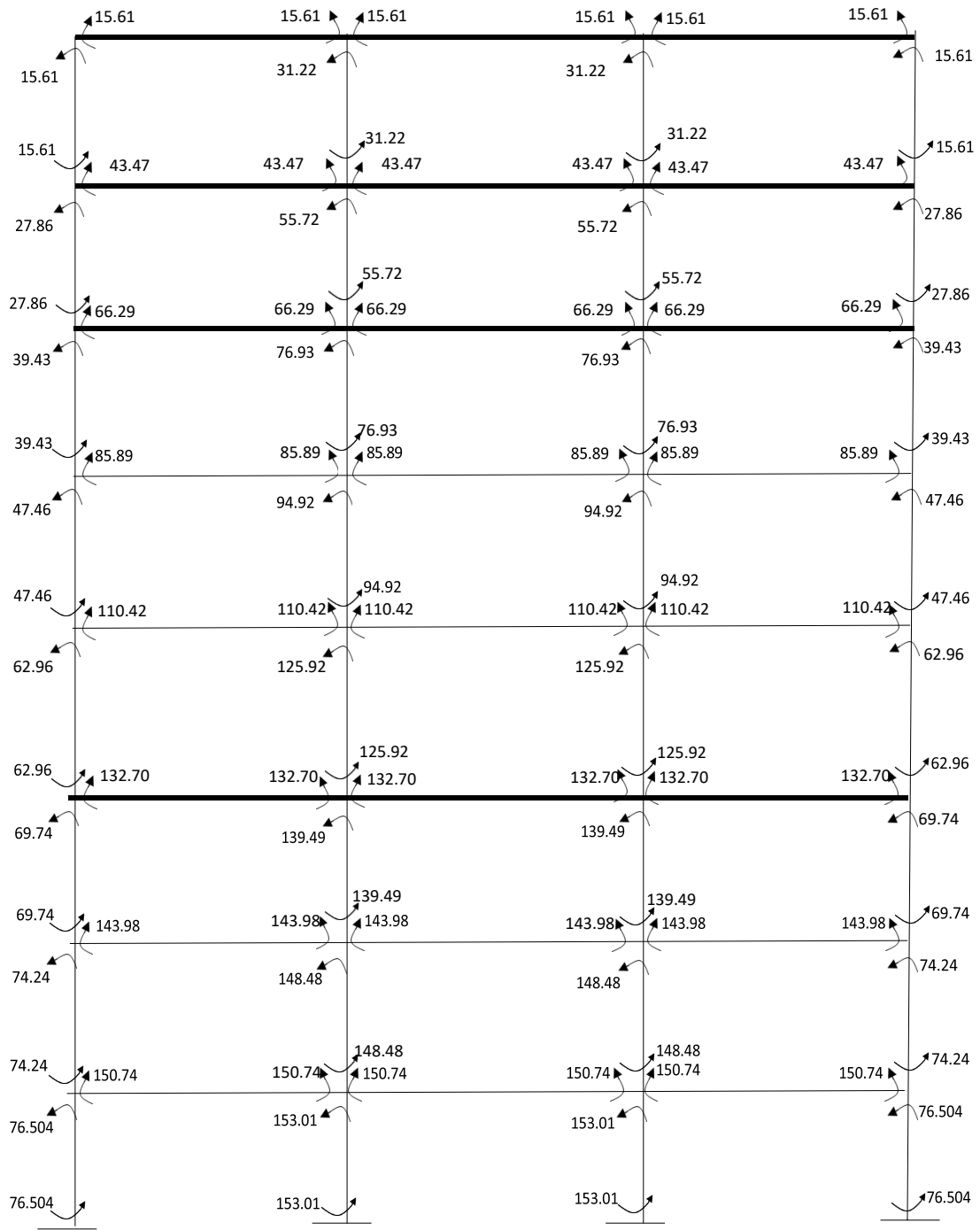


Figure 5.2: End Moments (k-ft)

5.1.2 GRAVITY ANALYSIS

The approach of work through Gravity Analysis for the given building frame is given under.

a) LOAD FROM SLAB TO BEAM:

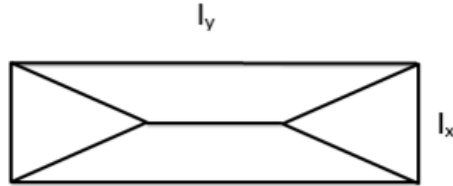


Figure 5.3: Typical Two Way Slab

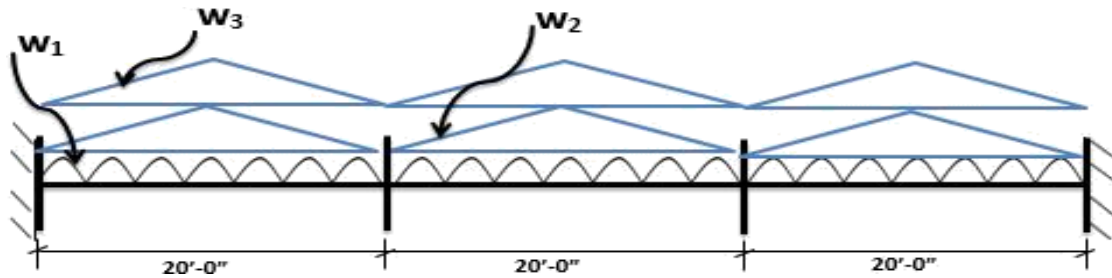


Figure 5.4: Load from Slab to Beam

w_1 = Self Weight Of beam,

$w_2 = w_3$ = Factored load coming from slab.

b) LOAD TRANSFORMATION TO UDL:

Trapezoidal and triangular loading is transformed to UDL by using the following relationships.

$$\text{For Short Span Beam: } \frac{1}{3} W_u * l_x \quad (\text{Eq. 5.1})$$

$$\text{For Long Span Beam: } \frac{1}{2} W_u * l_x \left(1 - \frac{1}{3} k^2\right) \quad (\text{Eq. 5.2})$$

Where;

W_u = factored load on slab

$l_x = 20$ ft

$k = l_y / l_x$

Frame on Grid A:

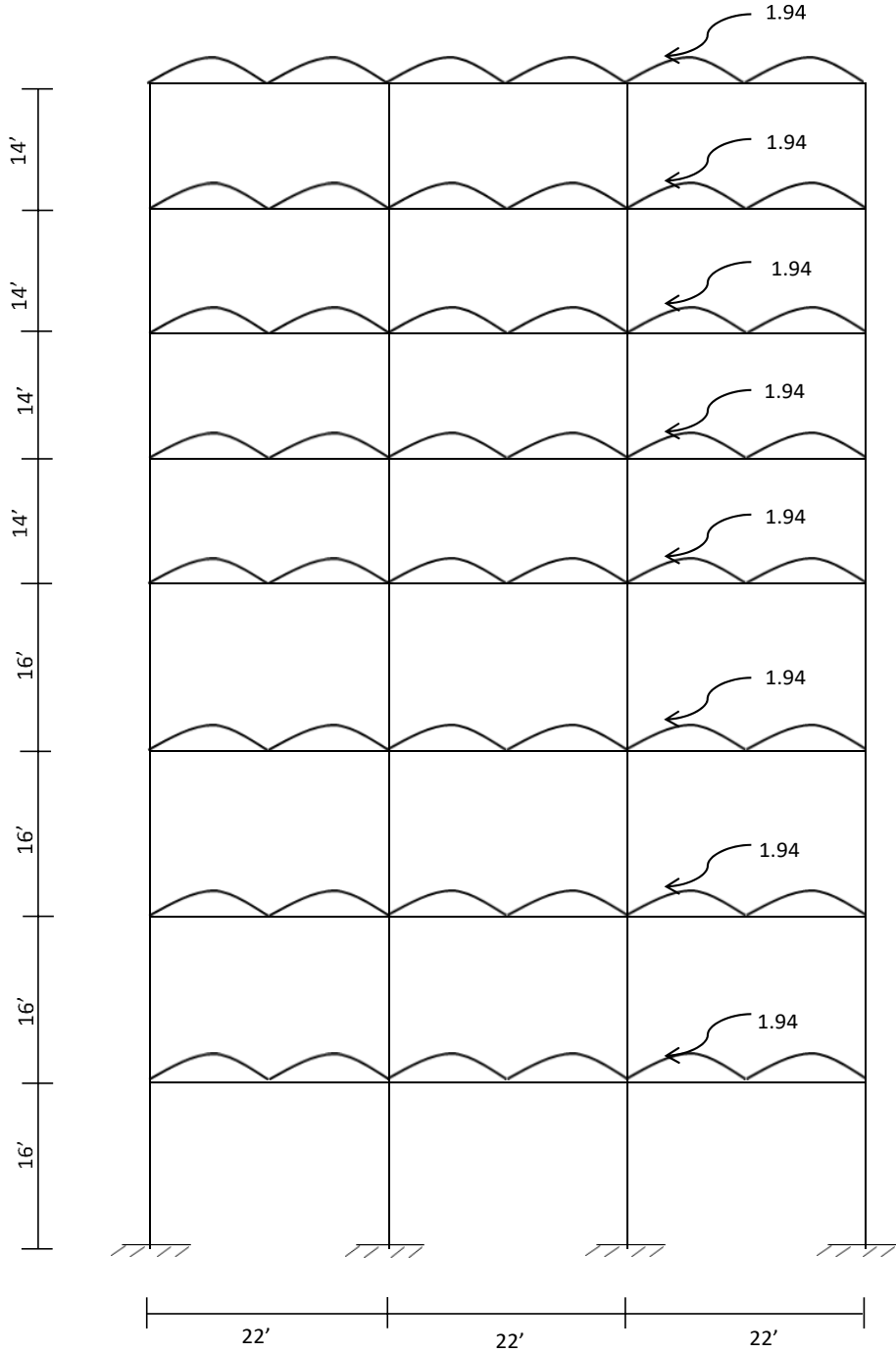


Figure 5.5: UDL (K/ft) on frame at Grid A

c) **FIXED END MOMENTS**

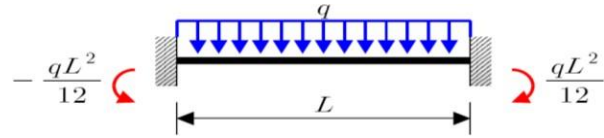


Figure 5.6: Typical Fixed End Moment Condition

by Using Formula mentioned above the Fixed End Moments are:

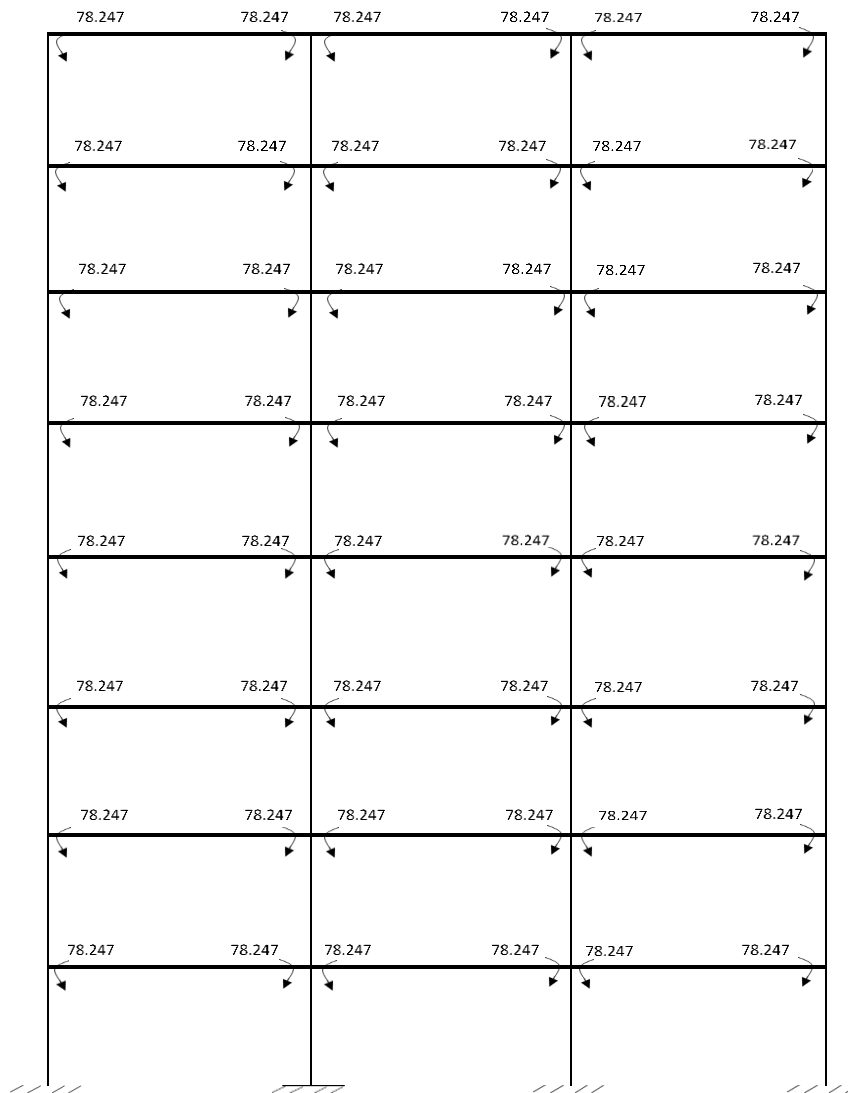


Figure 5.7: Fixed End Moment (k-ft) on Frame at Grid A

5.1.2.1 MATRIX DISPLACEMENT METHOD

a) LOCAL STIFFNESS MATRIX OF AN ELEMENT [k]

The local matrices of elements 13, 37, 41 are shown below. The following matrices will govern for the rest of the elements.

BEAM

ELEMENT 13

- When $L = 22'-0''$
- Inertia $I = 9216 \text{ in}^4$

$[k] = E \times$

	L1 (G17)	L2 (G18)	L3	L4
L1 (G17)	139.64	69.8182	0.7934	-0.793
L2 (G18)	69.818	139.636	0.7934	-0.793
L3	0.7934	0.79339	0.006	-0.006
L4	-0.793	-0.7934	-0.006	0.006

COLUMN

ELEMENT 37

- When $L = 14'-0''$
- Inertia $I = 8750.6 \text{ in}^4$

$[k] = E \times$

	L1 (G17)	L2 (G13)	L3 (G37)	L4 (G36)
L1 (G17)	208.3474	104.1737	1.860245	-1.86024
L2 (G13)	104.1737	208.3474	1.860245	-1.86024
L3 (G37)	1.860245	1.860245	0.022146	-0.02215
L4 (G36)	-1.86024	-1.86024	-0.02215	0.022146

ELEMENT 41

- When $L = 16'-0''$
- Inertia $I = 8750.6 \text{ in}^4$

$$\mathbf{K} = E \times$$

	L1 (G21)	L2 (G17)	L3 (G38)	L4 (G37)
L1 (G36)	182.3	91.152	1.4243	-1.424
L2 (G17)	91.152	182.304	1.4243	-1.424
L3 (G38)	1.4243	1.42425	0.0148	-0.015
L4 (G37)	-1.424	-1.4243	-0.015	0.0148

b) GLOBAL STIFFNESS MATRIX [K]

The transformed global matrix of 36×36 is reduced to 32×32 after applying boundary conditions and is shown below.

c) INVERSE OF GLOBAL MATRIX $[K]^{-1}$

The inverse of the global matrix is as under.

d) FIXED END MOMENT MATRIX [F_o]

To transfer the load of span on node fixed end moments are calculated and are shown under.

F _{o1} = -938.964
F _{o2} = 938.964
F _{o3} = -938.964
F _{o4} = 938.964
F _{o5} = -938.964
F _{o6} = 938.964
F _{o7} = -938.964
F _{o8} = 938.964
F _{o9} = -938.964
F _{o10} = 938.964
F _{o11} = -938.964
F _{o12} = 938.964
F _{o13} = -938.964
F _{o14} = 938.964
F _{o15} = -938.964
F _{o16} = 938.964
F _{o17} = -938.964
F _{o18} = 938.964
F _{o19} = -938.964
F _{o20} = 938.964
F _{o21} = -938.964
F _{o22} = 938.964
F _{o23} = -938.964
F _{o24} = 938.964
F _{o25} = -938.964
F _{o26} = 938.964
F _{o27} = -938.964
F _{o28} = 938.964

F _{o29} = -938.964
F _{o30} = 938.964
F _{o31} = -938.964
F _{o32} = 938.964
F _{o33} = -938.964
F _{o34} = 938.964
F _{o35} = -938.964
F _{o36} = 938.964
F _{o37} = -938.964
F _{o38} = 938.964
F _{o39} = -938.964
F _{o40} = 938.964
F _{o41} = -938.964
F _{o42} = 938.964
F _{o43} = -938.964
F _{o44} = 938.964
F _{o45} = -938.964
F _{o46} = 938.964
F _{o47} = -938.964
F _{o48} = 938.964
F _{o49} = 0
F _{o50} = 0
F _{o51} = 0
F _{o52} = 0
F _{o53} = 0
F _{o54} = 0
F _{o55} = 0
F _{o56} = 0

F _{o57} = 0
F _{o58} = 0
F _{o59} = 0
F _{o60} = 0
F _{o61} = 0
F _{o62} = 0
F _{o63} = 0
F _{o64} = 0
F _{o65} = 0
F _{o66} = 0
F _{o67} = 0
F _{o68} = 0
F _{o69} = 0
F _{o70} = 0
F _{o71} = 0
F _{o72} = 0
F _{o73} = 0
F _{o74} = 0
F _{o75} = 0
F _{o76} = 0
F _{o77} = 0
F _{o78} = 0
F _{o79} = 0
F _{o80} = 0
F _{o81} = 0
F _{o82} = 0
F _{o83} = 0
F _{o84} = 0

F _{o85} = 0
F _{o86} = 0
F _{o87} = 0
F _{o88} = 0
F _{o89} = 0
F _{o90} = 0
F _{o91} = 0
F _{o92} = 0
F _{o93} = 0
F _{o94} = 0
F _{o95} = 0
F _{o96} = 0
F _{o97} = 0
F _{o98} = 0
F _{o99} = 0
F _{o100} = 0
F _{o101} = 0
F _{o102} = 0
F _{o103} = 0
F _{o104} = 0
F _{o105} = 0
F _{o106} = 0
F _{o107} = 0
F _{o108} = 0
F _{o109} = 0
F _{o110} = 0
F _{o111} = 0
F _{o112} = 0

Note: All values in k-in.

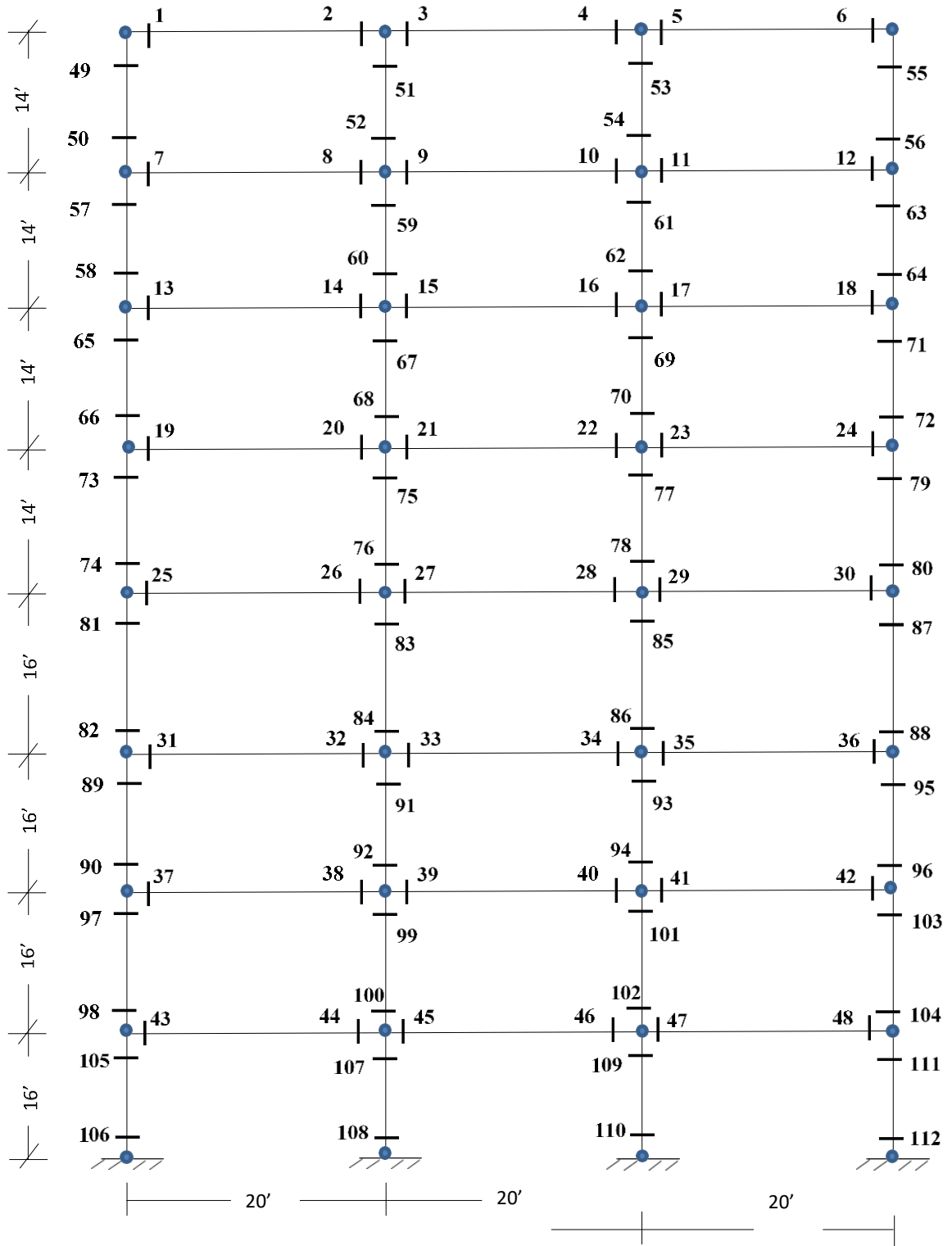


Figure 5.8: Location of Fixed end moment

e) LOAD MATRIX [P]

The load matrix is obtained by considering the loads at the node of the member and is shown below.

$P_1 = 938.964$
$P_2 = 0$
$P_3 = 0$
$P_4 = -938.964$
$P_5 = 938.964$
$P_6 = 0$
$P_7 = 0$
$P_8 = -938.964$
$P_9 = 938.964$
$P_{10} = 0$
$P_{11} = 0$
$P_{12} = -938.964$
$P_{13} = 938.964$
$P_{14} = 0$
$P_{15} = 0$
$P_{16} = -938.964$
$P_{17} = 938.964$
$P_{18} = 0$
$P_{19} = 0$
$P_{20} = -938.964$
$P_{21} = 938.964$
$P_{22} = 0$
$P_{23} = 0$
$P_{24} = -938.964$
$P_{25} = 938.964$
$P_{26} = 0$
$P_{27} = 0$
$P_{28} = -938.964$
$P_{29} = 938.964$
$P_{30} = 0$
$P_{31} = 0$
$P_{32} = -938.964$

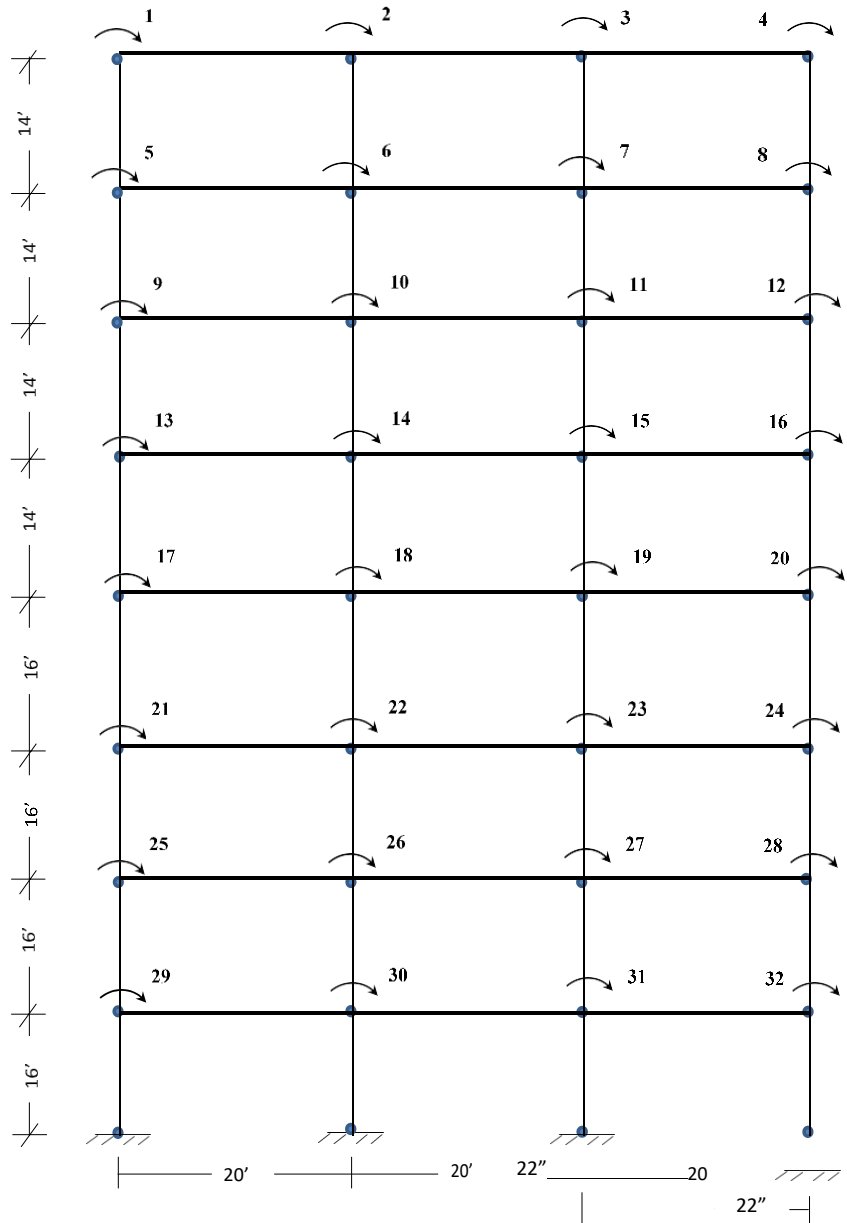


Figure 5.9: Location of Loads

Note: All values in k-in.

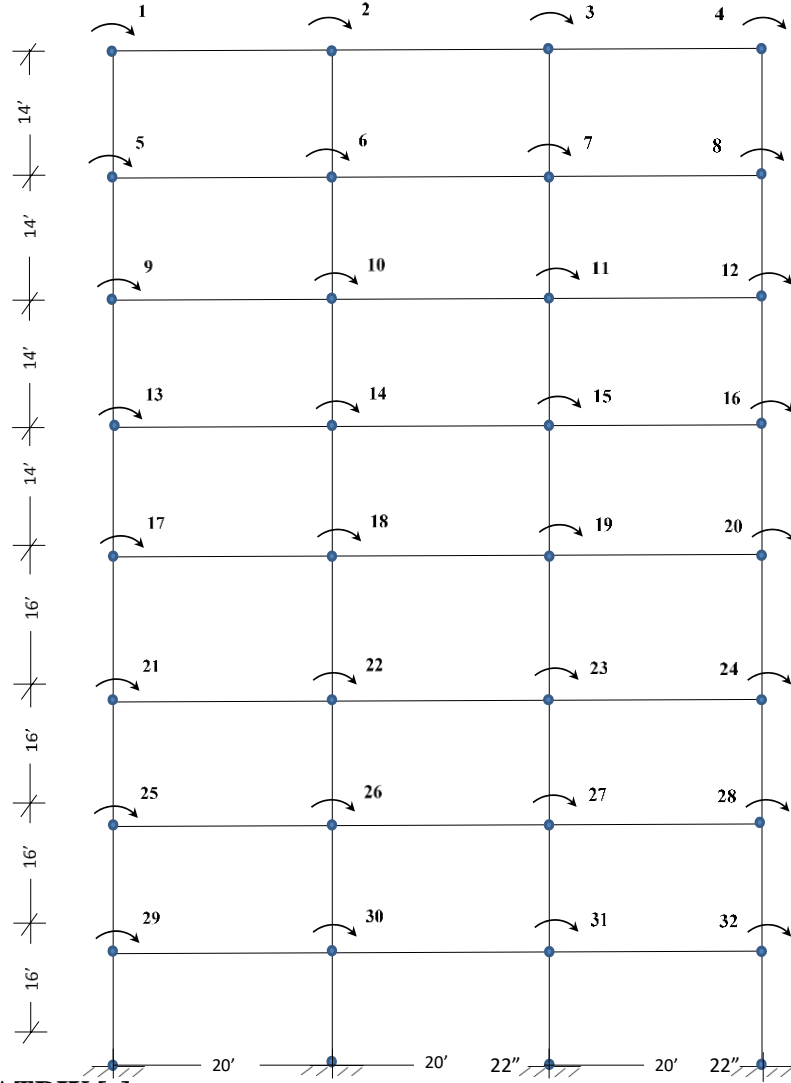
$$X_1 = 2.519983711$$

X_2	=	-0.563209697
X_3	=	0.563267227
X_4	=	-2.520158463
X_5	=	0.973116893
X_6	=	0.006664175
X_7	=	-0.00679737
X_8	=	-0.972571708
X_9	=	1.29214033
X_{10}	=	-0.128946098
X_{11}	=	0.129502298
X_{12}	=	-1.29478781
X_{13}	=	1.226182599
X_{14}	=	-0.097993909
X_{15}	=	0.095812827
X_{16}	=	-1.212961957
X_{17}	=	1.238655195
X_{18}	=	-0.102385148
X_{19}	=	0.109001564
X_{20}	=	-1.3051494
X_{21}	=	1.418229442
X_{22}	=	-0.138513178
X_{23}	=	0.136351511
X_{24}	=	-1.40546451
X_{25}	=	1.32300525
X_{26}	=	-0.109918612
X_{27}	=	0.110450217
X_{28}	=	-1.325469728
X_{29}	=	1.648300313
X_{30}	=	-0.183000924
X_{31}	=	0.182887917

f) JOINT DISPLACEMENT MATRIX [X]

$$[X] = [K]^{-1}[P]$$

Note:
All values in radians.



g) MEMBER DISPLACEMENT MATRIX [e]

Figure 5.10: Location of Joint displacements

The displacement matrix is obtained by considering the joint rotation of the member.

e_1	=	2.519984
e_2	=	-0.56321
e_3	=	-0.56321
e_4	=	0.563267
e_5	=	0.563267
e_6	=	-2.52016

e_7	=	0.973117
e_8	=	0.006664
e_9	=	0.006664
e_{10}	=	-0.0068
e_{11}	=	-0.0068
e_{12}	=	-0.97257

e_{13}	=	1.29214
e_{14}	=	-0.12895
e_{15}	=	-0.12895
e_{16}	=	0.129502
e_{17}	=	0.129502
e_{18}	=	-1.29479

e_{19}	=	1.226183
e_{20}	=	-0.09799
e_{21}	=	-0.09799
e_{22}	=	0.095813
e_{23}	=	0.095813
e_{24}	=	-1.21296

$e_{25} = 1.238655$	$e_{47} = 0.182888$	$e_{69} = 0.129502$	$e_{91} = -0.13851$
$e_{26} = -0.10239$	$e_{48} = -1.64784$	$e_{70} = 0.095813$	$e_{92} = -0.10992$
$e_{27} = -0.10239$	$e_{49} = 2.519984$	$e_{71} = -1.29479$	$e_{93} = 0.136352$
$e_{28} = 0.109002$	$e_{50} = 0.973117$	$e_{72} = -1.21296$	$e_{94} = 0.11045$
$e_{29} = 0.109002$	$e_{51} = -0.56321$	$e_{73} = 1.226183$	$e_{95} = -1.40546$
$e_{30} = -1.30515$	$e_{52} = 0.006664$	$e_{74} = 1.238655$	$e_{96} = -1.32547$
$e_{31} = 1.418229$	$e_{53} = 0.563267$	$e_{75} = -0.09799$	$e_{97} = 1.323005$
$e_{32} = -0.13851$	$e_{54} = -0.0068$	$e_{76} = -0.10239$	$e_{98} = 1.6483$
$e_{33} = -0.13851$	$e_{55} = -2.52016$	$e_{77} = 0.095813$	$e_{99} = -0.10992$
$e_{34} = 0.136352$	$e_{56} = -0.97257$	$e_{78} = 0.109002$	$e_{100} = -0.183$
$e_{35} = 0.136352$	$e_{57} = 0.973117$	$e_{79} = -1.21296$	$e_{101} = 0.11045$
$e_{36} = -1.40546$	$e_{58} = 1.29214$	$e_{80} = -1.30515$	$e_{102} = 0.182888$
$e_{37} = 1.323005$	$e_{59} = 0.006664$	$e_{81} = 1.238655$	$e_{103} = -1.32547$
$e_{38} = -0.10992$	$e_{60} = -0.12895$	$e_{82} = 1.418229$	$e_{104} = -1.64784$
$e_{39} = -0.10992$	$e_{61} = -0.0068$	$e_{83} = -0.10239$	$e_{105} = 1.6483$
$e_{40} = 0.11045$	$e_{62} = 0.129502$	$e_{84} = -0.13851$	$e_{106} = 0$
$e_{41} = 0.11045$	$e_{63} = -0.97257$	$e_{85} = 0.109002$	$e_{107} = -0.183$
$e_{42} = -1.32547$	$e_{64} = -1.29479$	$e_{86} = 0.136352$	$e_{108} = 0$
$e_{43} = 1.6483$	$e_{65} = 1.29214$	$e_{87} = -1.30515$	$e_{109} = 0.182888$
$e_{44} = -0.183$	$e_{66} = 1.226183$	$e_{88} = -1.40546$	$e_{110} = 0$
$e_{45} = -0.183$	$e_{67} = -0.12895$	$e_{89} = 1.418229$	$e_{111} = -1.64784$
$e_{46} = 0.182888$	$e_{68} = -0.09799$	$e_{90} = 1.323005$	$e_{112} = 0$

Note: All values in radians.

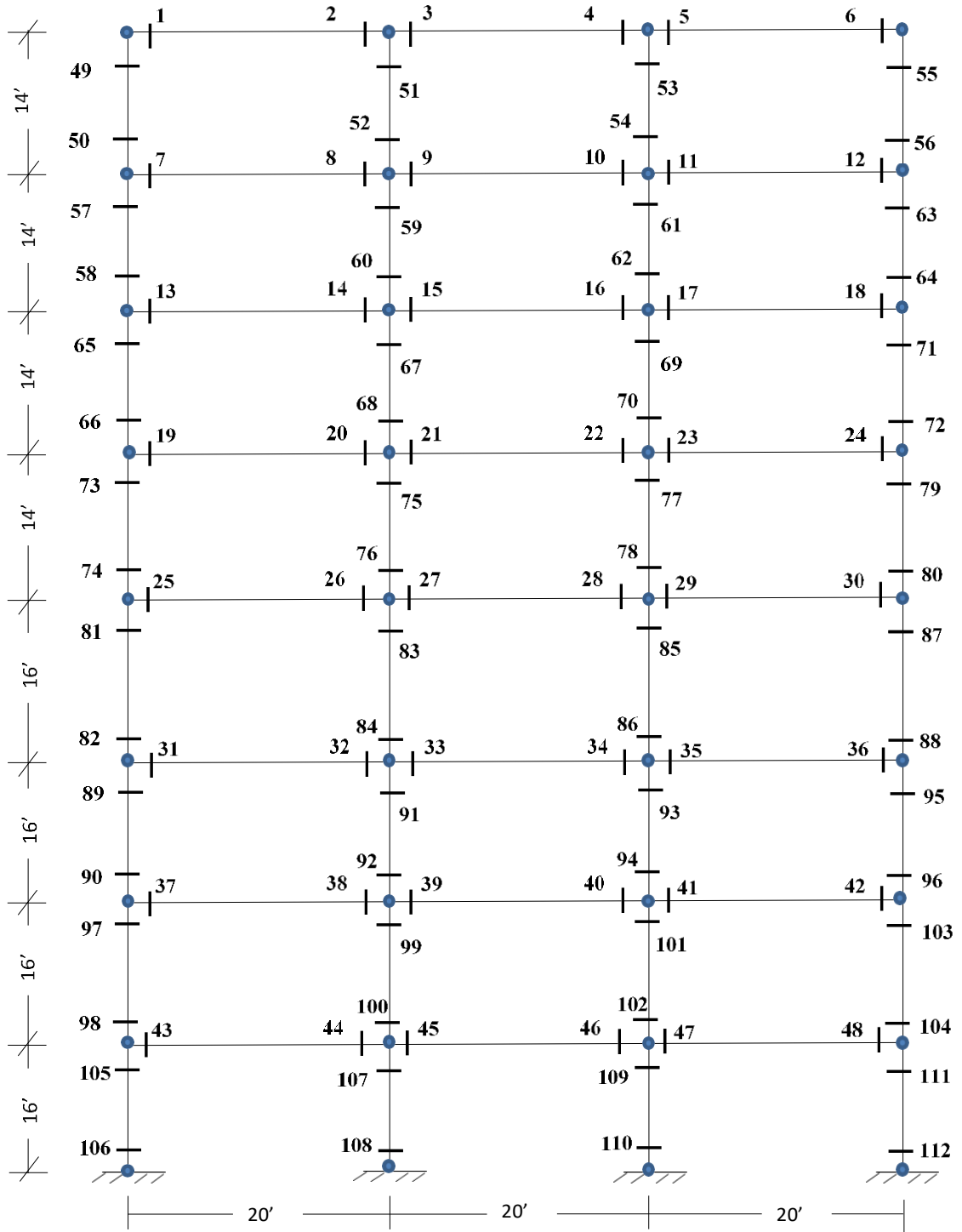


Figure 5.11: Location of member displacements

h) ELEMENT STIFFNESS MATRIX [S]

The stiffness matrix of frame is obtained by using the standard stiffness matrix of an elements.

i) FORCE MATRIX [F]

$$[F] = [S] [e]$$

F ₁ = 312.559
F ₂ = 97.2961
F ₃ = -39.3183
F ₄ = 39.3303
F ₅ = -97.3003
F ₆ = -312.579
F ₇ = 136.348
F ₈ = 68.8718
F ₉ = 0.45598
F ₁₀ = -0.48388
F ₁₁ = -68.8523
F ₁₂ = -136.281
F ₁₃ = 171.427
F ₁₄ = 72.2093
F ₁₅ = -8.96395
F ₁₆ = 9.08045
F ₁₇ = -72.3165
F ₁₈ = -171.758
F ₁₉ = 164.378
F ₂₀ = 71.9263
F ₂₁ = -6.99404
F ₂₂ = 6.5372
F ₂₃ = -71.3078
F ₂₄ = -162.684
F ₂₅ = 165.813
F ₂₆ = 72.184
F ₂₇ = -6.6864
F ₂₈ = 8.07224

F ₂₉ = -75.9026
F ₃₀ = -174.636
F ₃₁ = 188.366
F ₃₂ = 79.6767
F ₃₃ = -9.82166
F ₃₄ = 9.36889
F ₃₅ = -79.0873
F ₃₆ = -186.734
F ₃₇ = 177.065
F ₃₈ = 77.0212
F ₃₉ = -7.6372
F ₄₀ = 7.74855
F ₄₁ = -77.119
F ₄₂ = -177.372
F ₄₃ = 217.386
F ₄₄ = 89.5277
F ₄₅ = -12.7847
F ₄₆ = 12.761
F ₄₇ = -89.5113
F ₄₈ = -217.329
F ₄₉ = 626.22
F ₅₀ = 465.125
F ₅₁ = -116.615
F ₅₂ = -57.2662
F ₅₃ = 116.613
F ₅₄ = 57.2445
F ₅₅ = -626.199
F ₅₆ = -465.029

F ₅₇ = 337.254
F ₅₈ = 370.478
F ₅₉ = -12.0408
F ₆₀ = -26.1636
F ₆₁ = 12.0709
F ₆₂ = 26.2656
F ₆₃ = -337.416
F ₆₄ = -370.972
F ₆₅ = 396.833
F ₆₆ = 389.964
F ₆₇ = -37.063
F ₆₈ = -33.8395
F ₆₉ = 36.9517
F ₇₀ = 33.4432
F ₇₁ = -396.007
F ₇₂ = -387.486
F ₇₃ = 384.393
F ₇₄ = 385.692
F ₇₅ = -31.0734
F ₇₆ = -31.5307
F ₇₇ = 31.3082
F ₇₈ = 32.6817
F ₇₉ = -388.565
F ₈₀ = -398.165
F ₈₁ = 354.981
F ₈₂ = 371.345
F ₈₃ = -31.2817
F ₈₄ = -34.5739

F ₈₅ = 32.2906
F ₈₆ = 34.7828
F ₈₇ = -365.936
F ₈₈ = -375.078
F ₈₉ = 379.031
F ₉₀ = 370.354
F ₉₁ = -35.2604
F ₉₂ = -32.6547
F ₉₃ = 34.9148
F ₉₄ = 32.5546
F ₉₅ = -376.929
F ₉₆ = -369.64
F ₉₇ = 391.319
F ₉₈ = 420.962
F ₉₉ = -36.7086
F ₁₀₀ = -43.3683
F ₁₀₁ = 36.7952
F ₁₀₂ = 43.3961
F ₁₀₃ = -391.726
F ₁₀₄ = -421.102
F ₁₀₅ = 300.403
F ₁₀₆ = 150.201
F ₁₀₇ = -33.3519
F ₁₀₈ = -16.676
F ₁₀₉ = 33.3313
F ₁₁₀ = 16.6657
F ₁₁₁ = -300.319
F ₁₁₂ = -150.159

Note: All values in k-in.

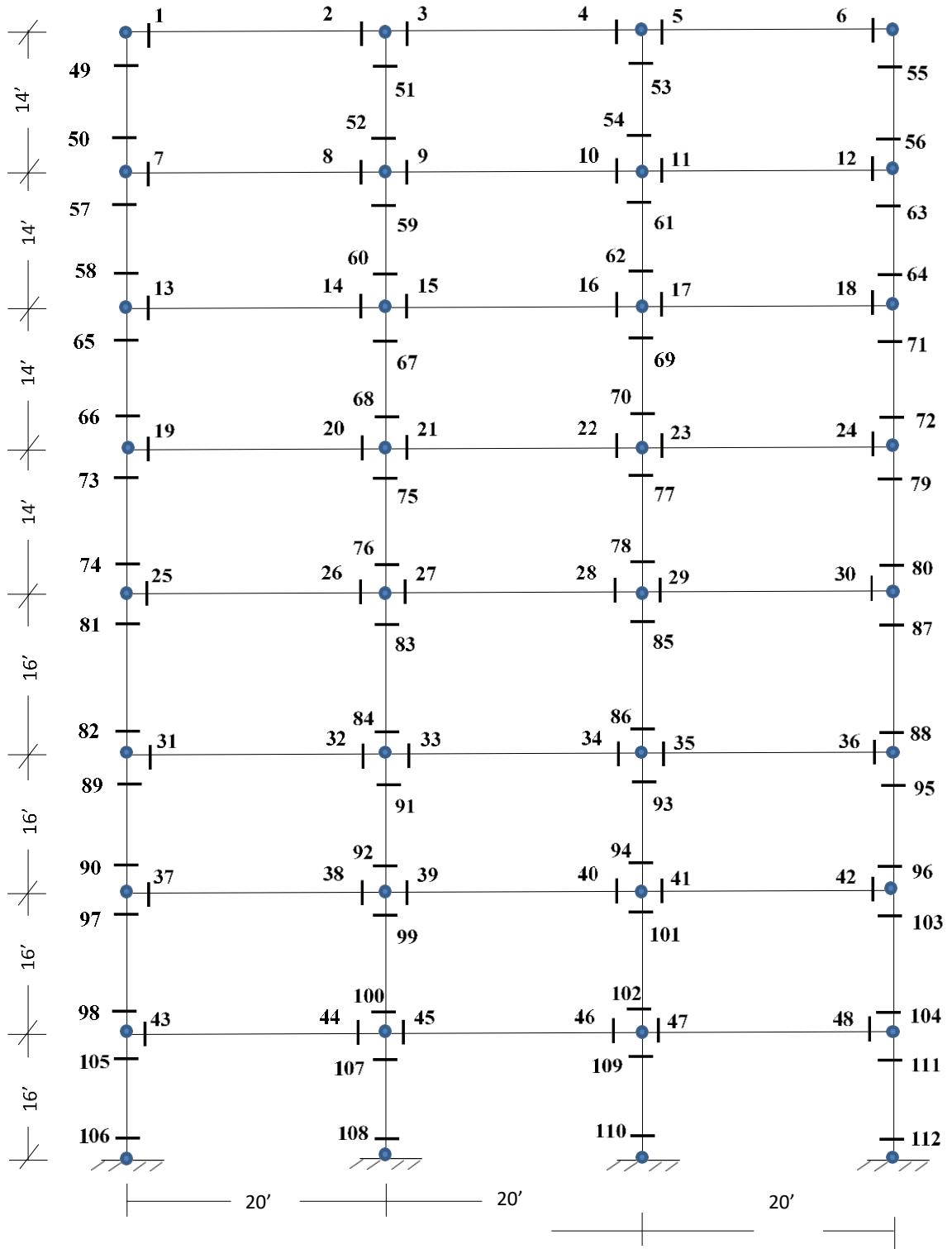


Figure 5.12: Location of Forces

j) END FORCE MATRIX [F*]

$$[F^*] = [F_o] + [F]$$

$F^*_1 = -626.4$
$F^*_2 = 1036.3$
$F^*_3 = -978.28$
$F^*_4 = 978.29$
$F^*_5 = -1036.3$
$F^*_6 = 626.38$
$F^*_7 = -802.62$
$F^*_8 = 1007.8$
$F^*_9 = -938.51$
$F^*_{10} = 938.48$
$F^*_{11} = -1007.8$
$F^*_{12} = 802.68$
$F^*_{13} = -767.54$
$F^*_{14} = 1011.2$
$F^*_{15} = -947.93$
$F^*_{16} = 948.04$
$F^*_{17} = -1011.3$
$F^*_{18} = 767.21$
$F^*_{19} = -774.59$
$F^*_{20} = 1010.9$
$F^*_{21} = -945.96$
$F^*_{22} = 945.5$
$F^*_{23} = -1010.3$
$F^*_{24} = 776.28$
$F^*_{25} = -773.15$
$F^*_{26} = 1011.1$
$F^*_{27} = -945.65$
$F^*_{28} = 947.04$

$F^*_{29} = -1014.9$
$F^*_{30} = 764.33$
$F^*_{31} = -750.6$
$F^*_{32} = 1018.6$
$F^*_{33} = -948.79$
$F^*_{34} = 948.33$
$F^*_{35} = -1018.1$
$F^*_{36} = 752.23$
$F^*_{37} = -761.9$
$F^*_{38} = 1016$
$F^*_{39} = -946.6$
$F^*_{40} = 946.71$
$F^*_{41} = -1016.1$
$F^*_{42} = 761.59$
$F^*_{43} = -721.58$
$F^*_{44} = 1028.5$
$F^*_{45} = -951.75$
$F^*_{46} = 951.73$
$F^*_{47} = -1028.5$
$F^*_{48} = 721.63$
$F^*_{49} = 626.22$
$F^*_{50} = 465.12$
$F^*_{51} = -116.61$
$F^*_{52} = -57.266$
$F^*_{53} = 116.61$
$F^*_{54} = 57.244$
$F^*_{55} = -626.2$
$F^*_{56} = -465.03$

$F^*_{57} = 337.25$
$F^*_{58} = 370.48$
$F^*_{59} = -12.041$
$F^*_{60} = -26.164$
$F^*_{61} = 12.071$
$F^*_{62} = 26.266$
$F^*_{63} = -337.42$
$F^*_{64} = -370.97$
$F^*_{65} = 396.83$
$F^*_{66} = 389.96$
$F^*_{67} = -37.063$
$F^*_{68} = -33.84$
$F^*_{69} = 36.952$
$F^*_{70} = 33.443$
$F^*_{71} = -396.01$
$F^*_{72} = -387.49$
$F^*_{73} = 384.39$
$F^*_{74} = 385.69$
$F^*_{75} = -31.073$
$F^*_{76} = -31.531$
$F^*_{77} = 31.308$
$F^*_{78} = 32.682$
$F^*_{79} = -388.56$
$F^*_{80} = -398.17$
$F^*_{81} = 354.98$
$F^*_{82} = 371.34$
$F^*_{83} = -31.282$
$F^*_{84} = -34.574$

$F^*_{85} = 32.291$
$F^*_{86} = 34.783$
$F^*_{87} = -365.94$
$F^*_{88} = -375.08$
$F^*_{89} = 379.03$
$F^*_{90} = 370.35$
$F^*_{91} = -35.26$
$F^*_{92} = -32.655$
$F^*_{93} = 34.915$
$F^*_{94} = 32.555$
$F^*_{95} = -376.93$
$F^*_{96} = -369.64$
$F^*_{97} = 391.32$
$F^*_{98} = 420.96$
$F^*_{99} = -36.709$
$F^*_{100} = -43.368$
$F^*_{101} = 36.795$
$F^*_{102} = 43.396$
$F^*_{103} = -391.73$
$F^*_{104} = -421.1$
$F^*_{105} = 300.4$
$F^*_{106} = 150.2$
$F^*_{107} = -33.352$
$F^*_{108} = -16.676$
$F^*_{109} = 33.331$
$F^*_{110} = 16.666$
$F^*_{111} = -300.32$
$F^*_{112} = -150.16$

Note: All values in k-in.

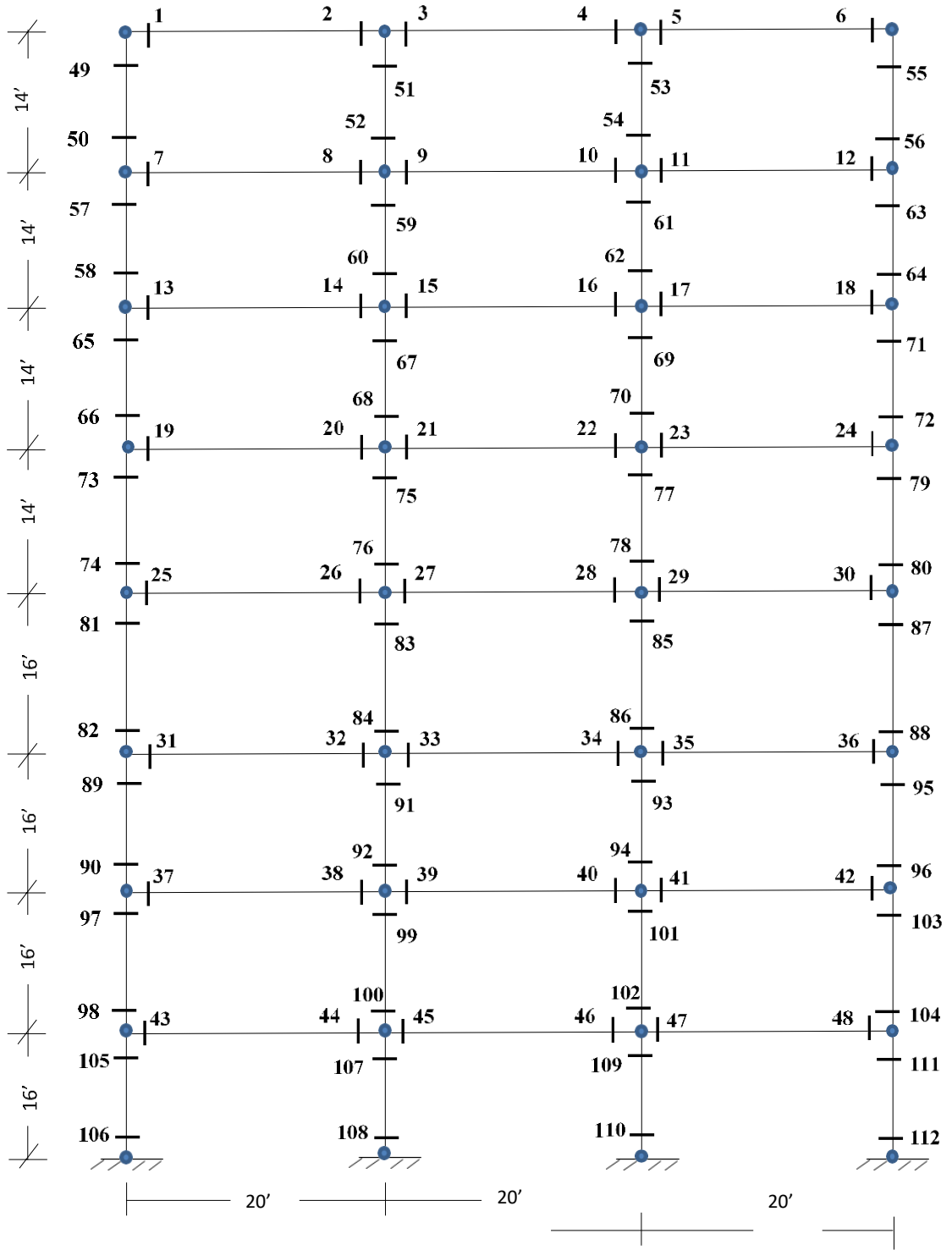


Figure 5.13: Location of End Forces

5.1.3 SUPERPOSITION

Gravity and Seismic moments are superimposed for Comparison.

(See Appendix C)

5.2 ANALYSIS THROUGH FINITE ELEMENT METHOD

The calculations for the frame on Grid A is given under.

a) DISCRETIZATION OF ELEMENT

The structure is divided into finite elements.

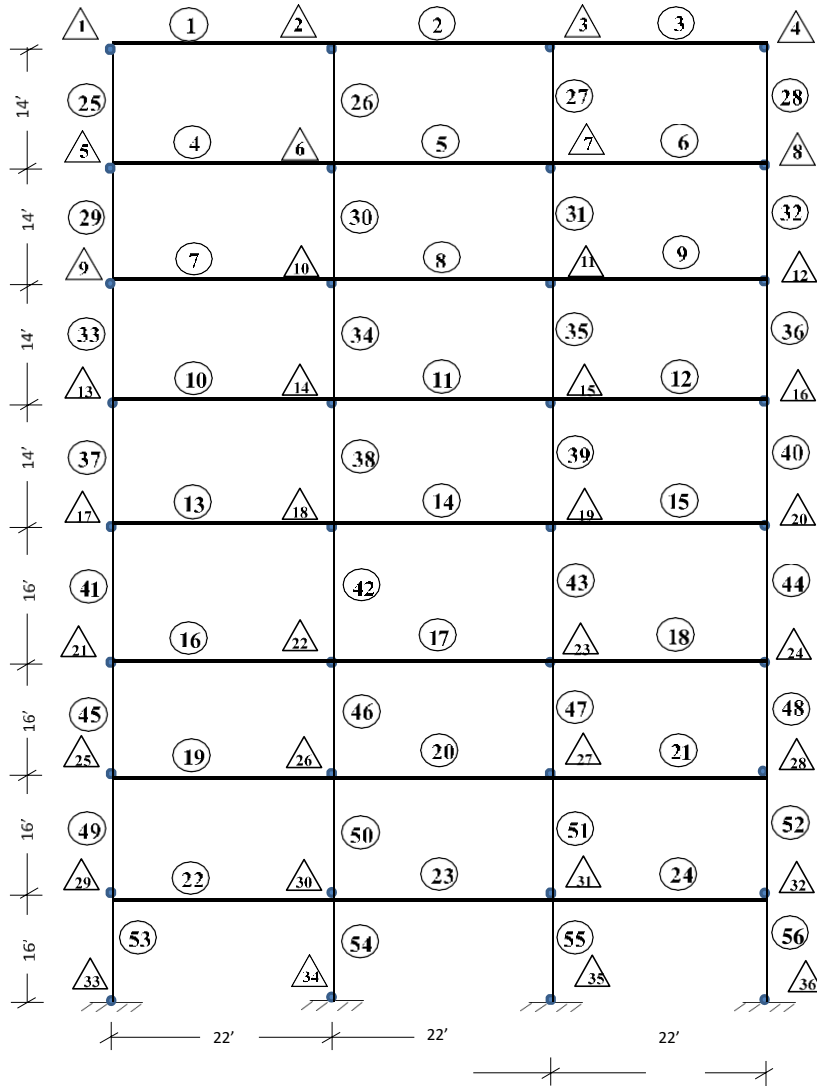
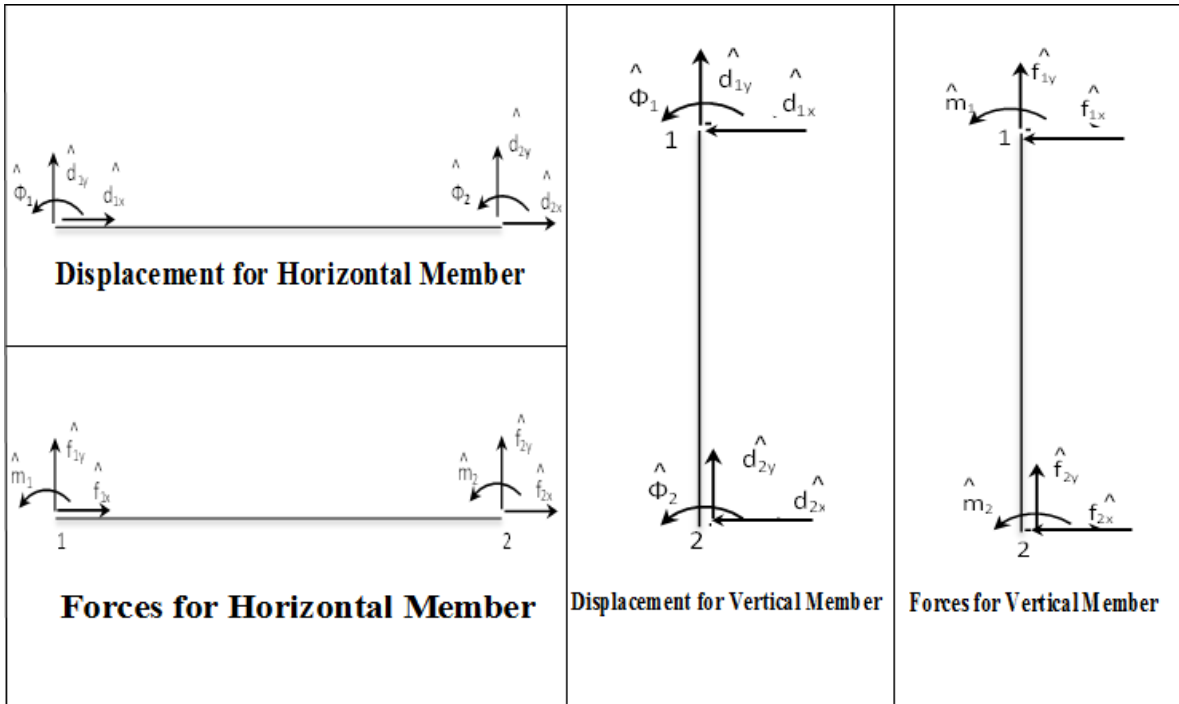


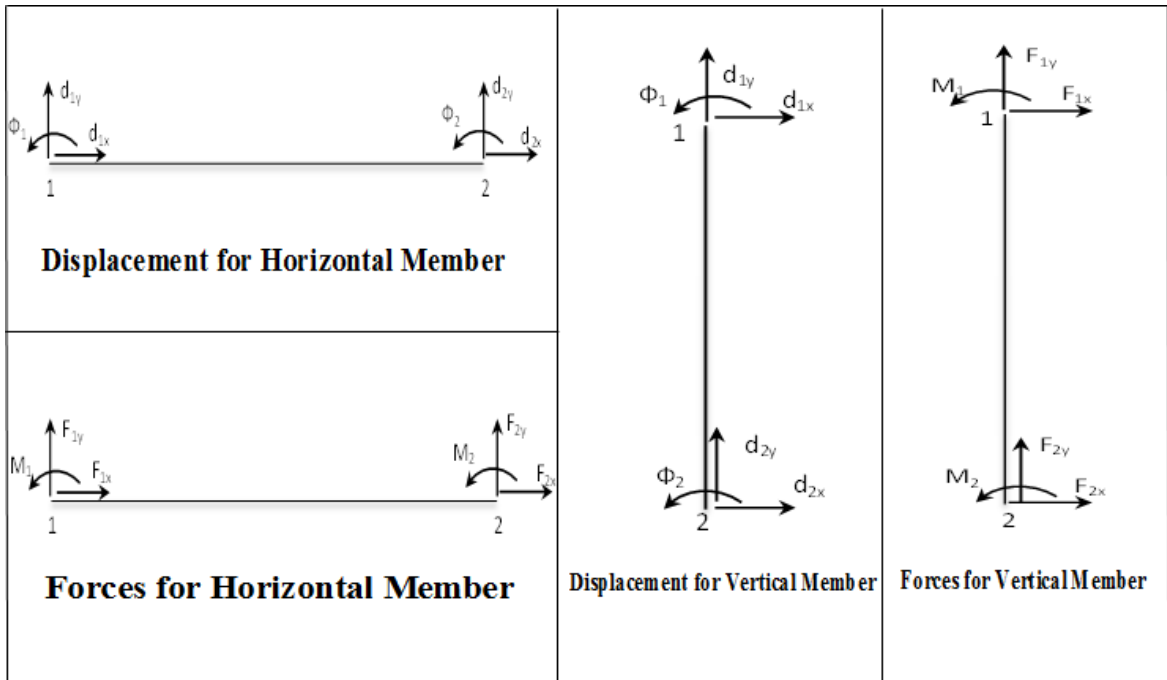
Figure 5.14: Member and Node Location

b) DEGREE OF FREEDOM

The degree of freedom for a flexural member is shown under.



Local Direction



Global Direction

Figure 5.15: Degree of Freedom

c) LOAD MATRIX [P]

The load matrix is obtained by considering the loads at the node of the member and is shown below.

F1x = 13.407
F1y = -21.34
M1 = -938.96
F2x = 0
F2y = -42.68
M2 = 0
F3x = 0
F3y = -42.68
M3 = 0
F4x = 0
F4y = -21.34
M4 = 938.96
F5x = 10.47
F5y = -21.34
M5 = -938.96
F6x = 0
F6y = -42.68
M6 = 0
F7x = 0
F7y = -42.68
M7 = 0
F8x = 0
F8y = -21.34
M8 = 938.96
F9x = 9.09
F9y = -21.34
M9 = -938.96
F10x = 0
F10y = -42.68
M10 = 0
F11x = 0
F11y = -42.68
M11 = 0

F12x = 0
F12y = -21.34
M12 = 938.96
F13x = 7.7
F13y = -21.34
M13 = -938.96
F14x = 0
F14y = -42.68
M14 = 0
F15x = 0
F15y = -42.68
M15 = 0
F16x = 0
F16y = -21.34
M16 = 938.96
F17x = 6.561
F17y = -21.34
M17 = -938.96
F18x = 0
F18y = -42.68
M18 = 0
F19x = 0
F19y = -42.68
M19 = 0
F20x = 0
F20y = -21.34
M20 = 938.96
F21x = 5.08
F21y = -21.34
M21 = -938.96
F22x = 0
F22y = -42.68
M22 = 0

F23x = 0
F23y = -42.68
M23 = 0
F24x = 0
F24y = -21.34
M24 = 938.96
F25x = 3.38
F25y = -21.34
M25 = -938.96
F26x = 0
F26y = -42.68
M26 = 0
F27x = 0
F27y = -42.68
M27 = 0
F28x = 0
F28y = -21.34
M28 = 938.96
F29x = 1.69
F29y = -21.34
M29 = -938.96
F30x = 0
F30y = -42.68
M30 = 0
F31x = 0
F31y = -42.68
M31 = 0
F32x = 0
F32y = -21.34
M32 = 938.96

Note: All 'F' values in Kip and 'M' Values in k-in.

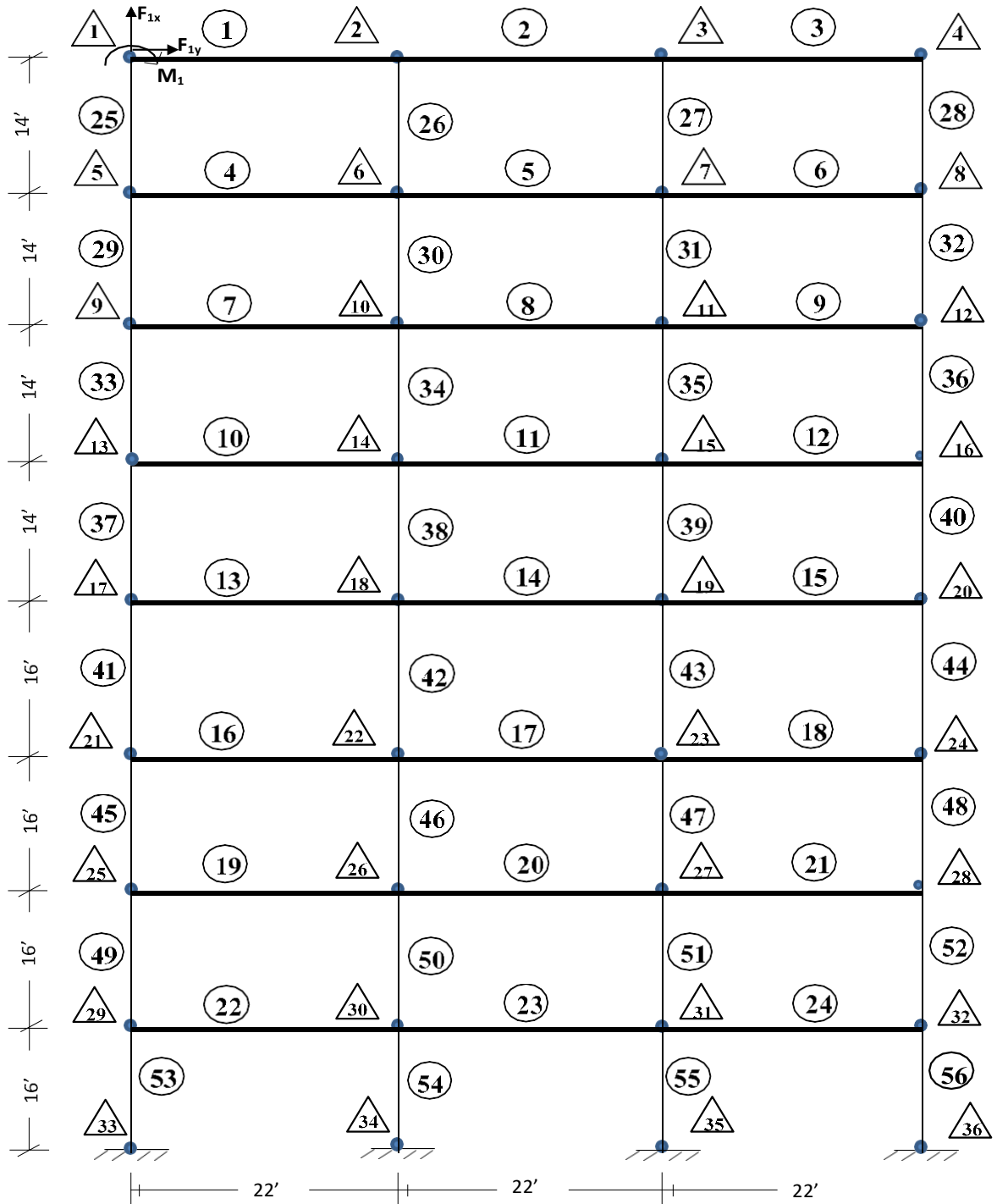


Figure 5.16: Location of Forces

Note: All the loads are acting on the nodes.

d) ELEMENT GLOBAL STIFFNESS MATRIX [k]

The Global matrices of elements 13, 37, 41 are shown below. The following matrices will govern for the rest of the elements.

BEAM

ELEMENT 13

- When $L = 22'-0''$
- Inertia $I = 9216 \text{ in}^4$

	d_{17x}	d_{17y}	ϕ_{17}	d_{18x}	d_{18y}	ϕ_{18}	
$k =$	d_{17x}	3277.2	0	0	-3277.2	0	0
	d_{17y}	0	42.32	5586.12	0	-42.32	5586.12
	ϕ_{17}	0	5586.12	983160	0	-5586.12	491580
	d_{18x}	-3277.2	0	0	3277.2	0	0
	d_{18y}	0	-42.32	-5586.12	0	42.32	-5586.12
	ϕ_{18}	0	5586.12	491580	0	-5586.12	983160

COLUMN

ELEMENT 37

- When $L = 14'-0''$
- Inertia $I = 8750.6 \text{ in}^4$

	d_{17x}	d_{17y}	ϕ_{17}	d_{13x}	d_{13y}	ϕ_{13}	
$k =$	d_{17x}	79.802	0	-6704.08	-79.802	0	-6704.08
	d_{17y}	0	6952.392	0	0	-6952.39	0
	ϕ_{17}	-6704.08	0	7.50E+05	6704.08	0	3.75E+05
	d_{13x}	-79.802	0	6704.08	79.802	0	6704.08
	d_{13y}	0	-6952.39	0	0	6952.392	0
	ϕ_{13}	-6704.08	0	3.75E+05	6704.08	0	7.50E+05

ELEMENT 41

- When $L = 16'-0''$
- Inertia $I = 8750.6 \text{ in}^4$

	d_{21x}	d_{21y}	ϕ_{21}	d_{17x}	d_{17y}	ϕ_{17}	
$k=$	d_{21x}	53.455	0	-5132.89	-53.455	0	-5132.89
	d_{21y}	0	6083.424	0	0	-6083.42	0
	ϕ_{21}	-5132.89	0	6.50E+05	5132.889	0	3.20E+05
	d_{17x}	-53.455	0	5132.889	53.455	0	5132.889
	d_{17y}	0	-6083.42	0	0	6083.424	0
	ϕ_{17}	-5132.89	0	3.20E+05	5132.889	0	6.50E+05

e) TOTAL GLOBAL STIFFNESS MATIX [K]

The transformed global matrix of 108×108 is reduced to 96×96 after applying boundary conditions.

f) INVERSE OF GLOBAL STIFFNESS MATRIX $[K]^{-1}$

g) DISPLACEMENT MATRIX [d]

$$[d] = [K]^{-1} [P]$$

d _{1x}	=	2.64298
d _{1y}	=	-0.08881
ϑ ₁	=	-0.00117
d _{2x}	=	2.637113
d _{2y}	=	-0.24509
ϑ ₂	=	-0.00028
d _{3x}	=	2.63224
d _{3y}	=	-0.2424
ϑ ₃	=	-8.5E-05
d _{4x}	=	2.629171
d _{4y}	=	-0.16426
ϑ ₄	=	0.000464
d _{5x}	=	2.532248
d _{5y}	=	-0.08596
ϑ ₅	=	-0.00101
d _{6x}	=	2.530292
d _{6y}	=	-0.23904
ϑ ₆	=	-0.0005
d _{7x}	=	2.529218
d _{7y}	=	-0.23612
ϑ ₇	=	-0.00026
d _{8x}	=	2.529126
d _{8y}	=	-0.16102
ϑ ₈	=	-0.00016
d _{9x}	=	2.360027
d _{9y}	=	-0.08033
ϑ ₉	=	-0.0013
d _{10x}	=	2.357766
d _{10y}	=	-0.22702
ϑ ₁₀	=	-0.00063
d _{11x}	=	2.356431
d _{11y}	=	-0.22369
ϑ ₁₁	=	-0.00043

d _{12x}	=	2.355885
d _{12y}	=	-0.15392
ϑ ₁₂	=	-0.00036
d _{13x}	=	2.127096
d _{13y}	=	-0.07228
ϑ ₁₃	=	-0.00148
d _{14x}	=	2.125197
d _{14y}	=	-0.20892
ϑ ₁₄	=	-0.00076
d _{15x}	=	2.124117
d _{15y}	=	-0.20514
ϑ ₁₅	=	-0.00058
d _{16x}	=	2.123755
d _{16y}	=	-0.14268
ϑ ₁₆	=	-0.00059
d _{17x}	=	1.83765
d _{17y}	=	-0.06214
ϑ ₁₇	=	-0.00175
d _{18x}	=	1.836572
d _{18y}	=	-0.18464
ϑ ₁₈	=	-0.0009
d _{19x}	=	1.836111
d _{19y}	=	-0.18051
ϑ ₁₉	=	-0.00074
d _{20x}	=	1.835999
d _{20y}	=	-0.12707
ϑ ₂₀	=	-0.00084
d _{21x}	=	1.395208
d _{21y}	=	-0.04857
ϑ ₂₁	=	-0.00199
d _{22x}	=	1.394022
d _{22y}	=	-0.1497
ϑ ₂₂	=	-0.001

d _{23x}	=	1.393406
d _{23y}	=	-0.14551
ϑ ₂₃	=	-0.0009
d _{24x}	=	1.393206
d _{24y}	=	-0.10378
ϑ ₂₄	=	-0.00109
d _{25x}	=	0.903251
d _{25y}	=	-0.03353
ϑ ₂₅	=	-0.00203
d _{26x}	=	0.902473
d _{26y}	=	-0.10739
ϑ ₂₆	=	-0.00104
d _{27x}	=	0.902129
d _{27y}	=	-0.10374
ϑ ₂₇	=	-0.00099
d _{28x}	=	0.901981
d _{28y}	=	-0.07487
ϑ ₂₈	=	-0.00122
d _{29x}	=	0.391056
d _{29y}	=	-0.0173
ϑ ₂₉	=	-0.00204
d _{30x}	=	0.391749
d _{30y}	=	-0.05756
ϑ ₃₀	=	-0.00092
d _{31x}	=	0.392135
d _{31y}	=	-0.05523
ϑ ₃₁	=	-0.00097
d _{32x}	=	0.392142
d _{32y}	=	-0.04023
ϑ ₃₂	=	-0.00119

Note: All 'd' values in inches and 'ϑ' values in radians.

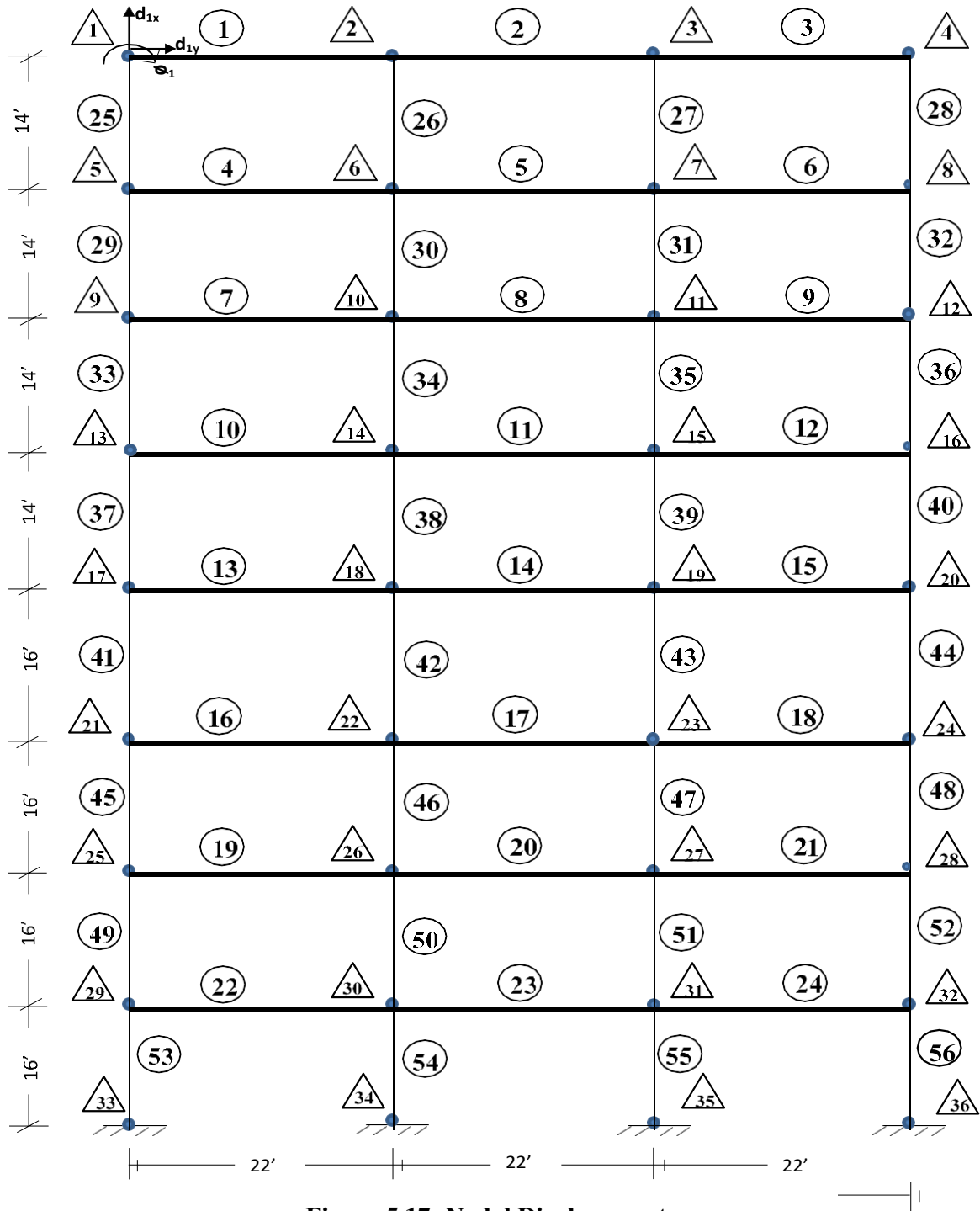


Figure 5.17: Nodal Displacements

Note: The displacements on page # 45 are nodal displacements

h) ELEMENT LOCAL STIFFNESS MATRIX \hat{k}

The local matrices of elements 13, 37 and 41 are shown below. The following matrices will govern for the rest of the elements.

BEAM

ELEMENT 13

- L= 22 ft

$$\hat{k} =$$

COLUMN

ELEMENT 37

- L= 14 ft

d_{17x}^{\wedge}
d_{17y}^{\wedge}
ϕ_{17}^{\wedge}
d_{13x}^{\wedge}
d_{13y}^{\wedge}
ϕ_{13}^{\wedge}

$$\hat{k} =$$

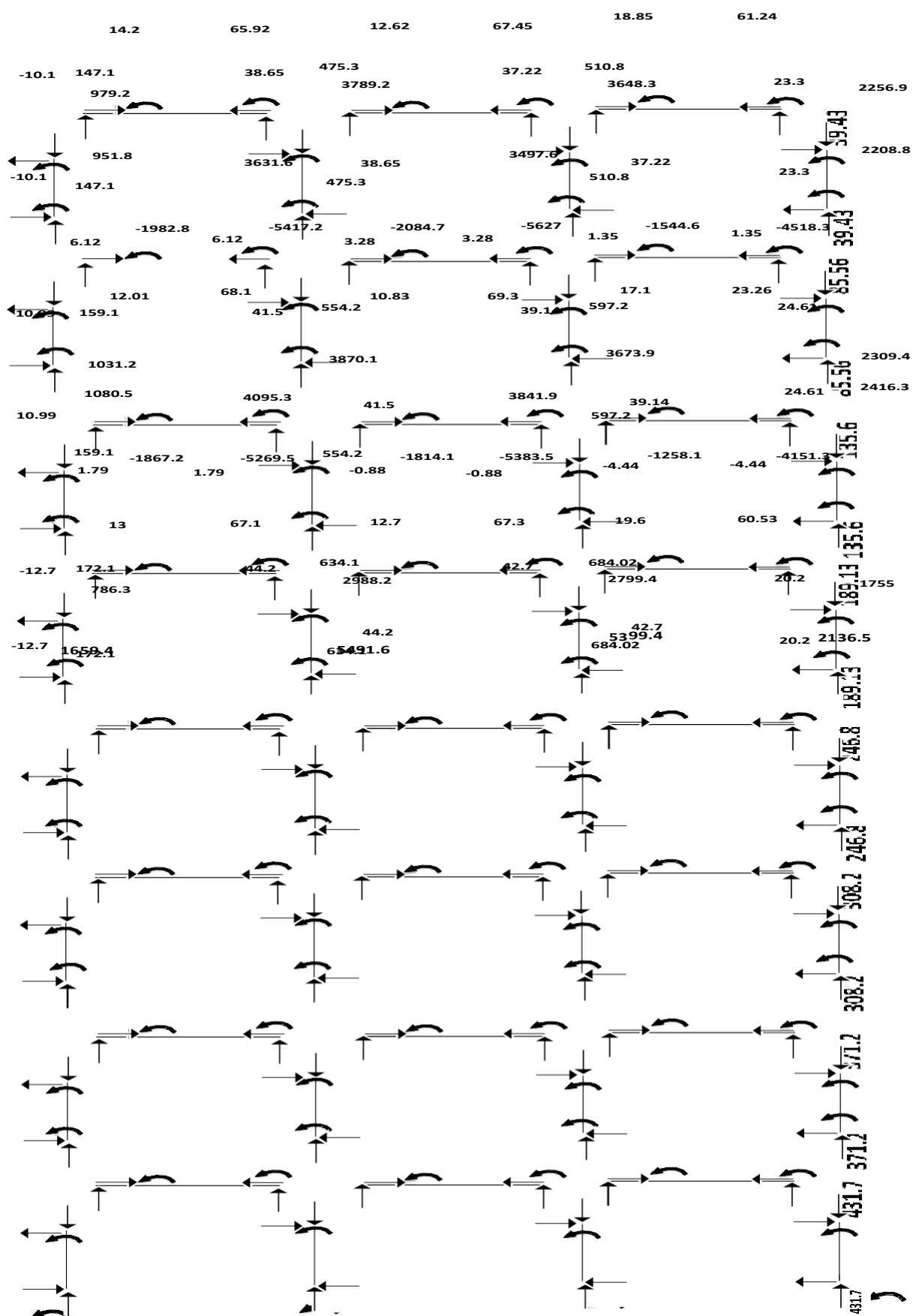
ELEMENT 41

- $L = 16 \text{ ft}$

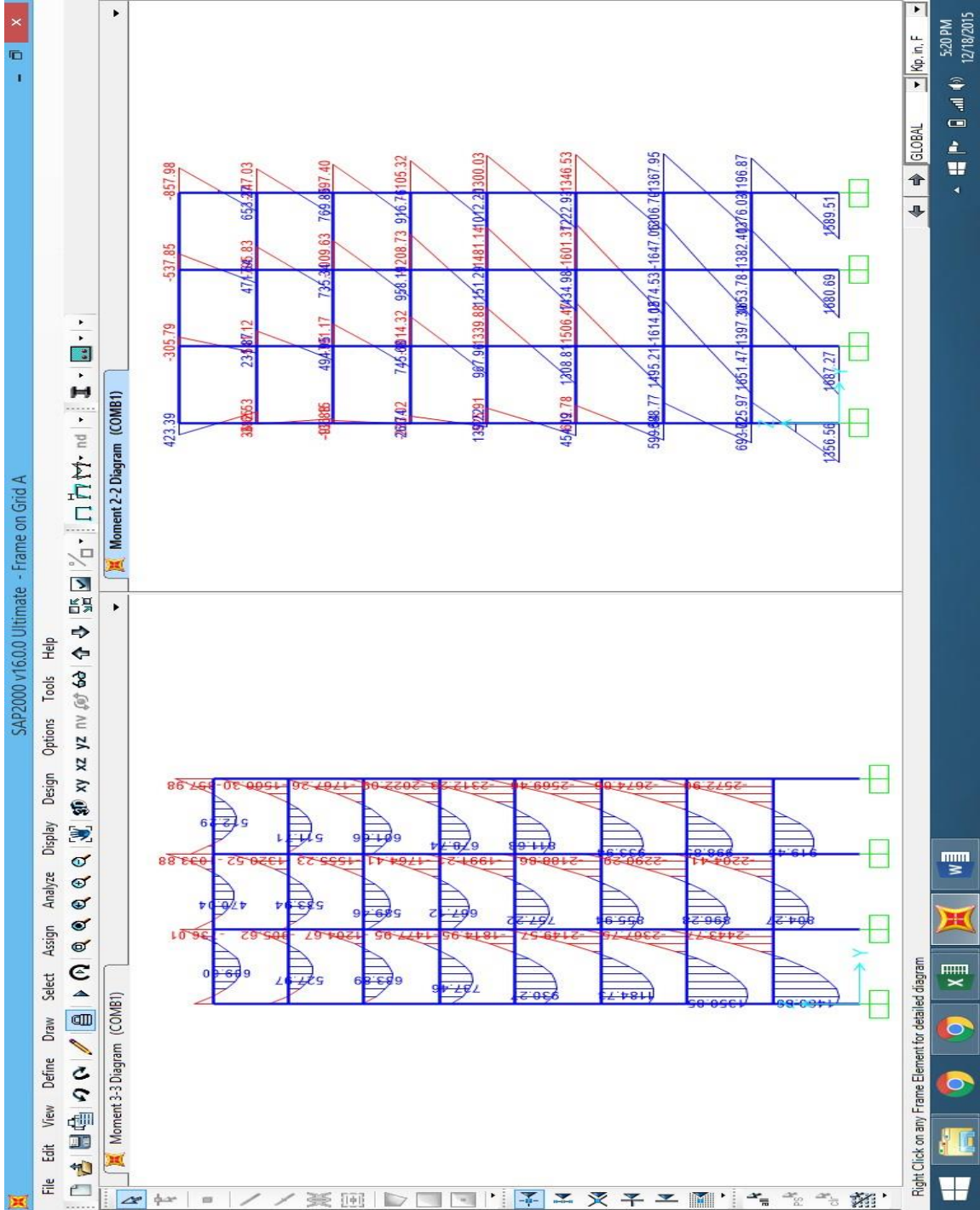
$$\hat{[k]} =$$

i) ELEMENT LOCAL FORCES \hat{f}

	34.5	585.2	34.5	-2380.1	23.10	1119.8	23.10	-2466.8	14.6	1551.8	14.6	-1390.7	
6.51	33.24	33.24	46.84	11.43	81.78	34.94	45.14	8.50	85.79	40.65	39.43	14.6	
6.51	-585.4	-518.1	660.5	11.43	513.1	1260.1	915.12	8.50	85.79	14.6	1062.6	1390.6	
	33.24	502.1	15.99	-2779.6	15.99	81.78	454.4	10	-3050.4	0.85	745.85	0.85	-2410.1
0.69	31.34	64.56	48.7	17.42	160.73	30.21	49.8	33.93	46.15	15.45	1228.7	15.86	
0.69	-132.5	64.56	1241.2	17.42	160.73	1224.7	17.66	169.6	1389.2	15.45	1248.5	17.66	
	16.24	-91.6	16.24	-3382.4	9.19	-131.2	9.19	-3666.3	3.21	245.9	3.21	-2875.6	
2.04	26.88	91.46	53.2	24.5	239.6	25.66	54.42	23.64	254.1	30.08	50	18.66	
2.04	223.6	118.6	1837.5	24.5	1776.3	2272.6	2195.5	23.64	18.66	1507.4	18.66	1507.4	
	91.46	-582.6	15.99	-3915.5	239.6	-671.6	10	-4200.3	0.85	-252.2	0.85	-3356.9	
4.76	31.34	114.5	48.7	29.87	318.24	30.21	49.8	33.93	46.15	21.37	1849.3	463.82	
4.76	336.32	114.5	2268.5	29.87	318.24	2177.2	28.89	338.96	2675.9	21.37	1740.6	338.96	
	10.29	-1168.2	10.29	-4533.1	5.14	-1285.9	5.14	-4821.9	0.16	-806.7	0.16	3847.7	
8.16	18.44	132.9	61.64	35.02	396.8	16.9	63.2	33.88	424.5	22.4	57.67	21.53	
8.16	831.8	736.3	3172.9	35.02	3053.6	3550.3	3450.5	33.88	21.53	2026.8	21.53	2026.8	
	132.9	-1715.6	8.70	-5116.4	396.8	-1845.8	5.06	-5319.3	1.73	-1310.7	1.73	-4283.8	



5.3 SAP2000 ANALYSIS RESULTS



CHAPTER NO. 6

RESULTS

- In the first sample example of frame there are three members and about 90% results of analysis by MDM have been matched with that by FEM.

- In the second sample example of frame there are six members and about 80% results of analysis by MDM have been matched with that by FEM.

- **COMPARISION OF SOFTWARE RESULTS WITH FEM**

1. The directions of end moments calculated manually by finite element method are same as that of obtained by software calculations (SAP2000).

2. The maximum difference among the results of manual analysis through FEM and software analysis (SAP) is 4023.86kip-in, whereas, the minimum and average difference is 41.52kip-in and 1176kip-in, respectively.

3. The reason of difference in result could be, software analysis (SAP) incorporates cross- section of the elements, whereas, manual calculation through FEM do not incorporate cross- section.

- **COMPARISION OF SOFTWARE RESULTS WITH FEM**

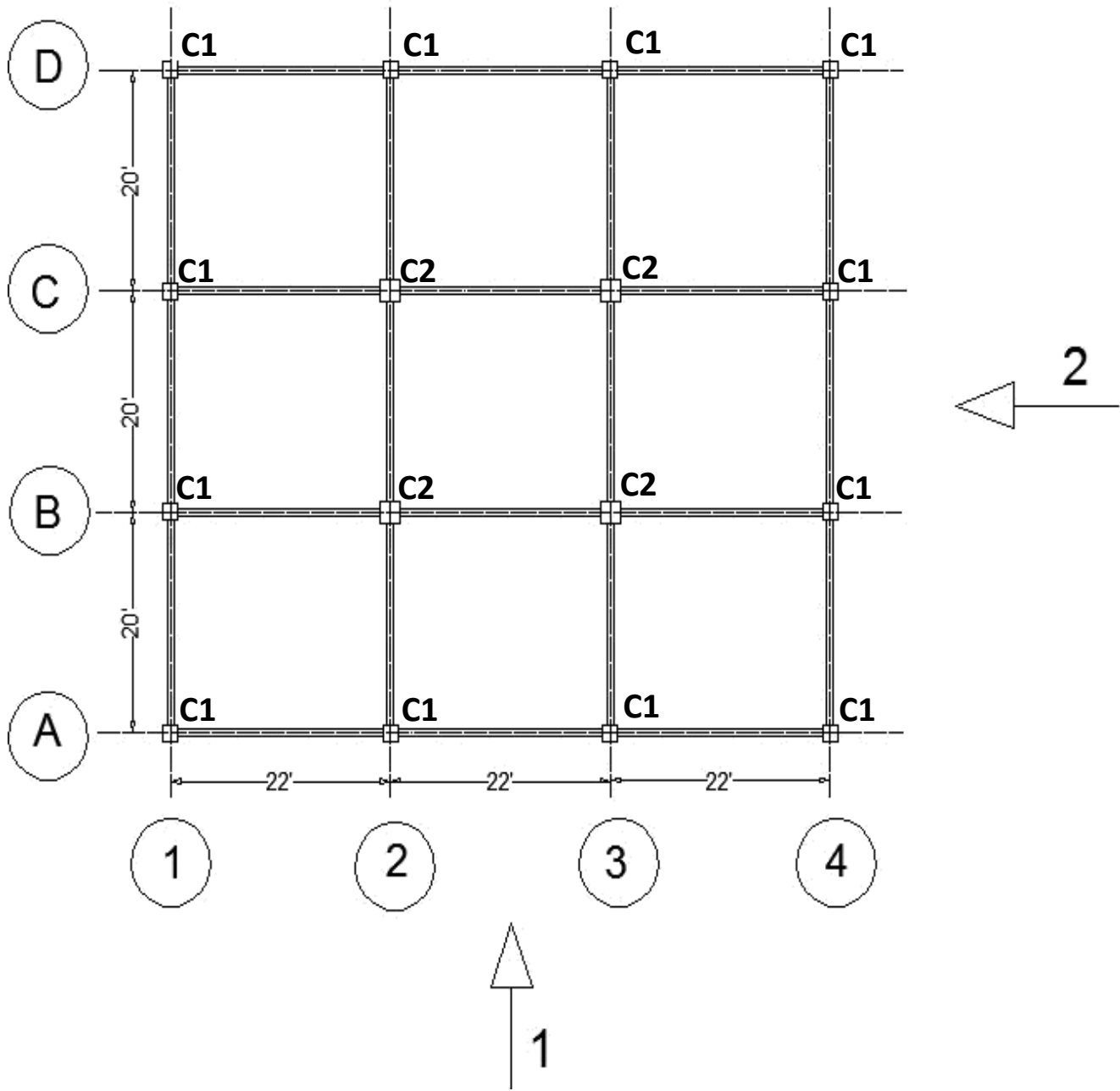
1. The direction of end moments calculated by classical method are different with that of software analysis (SAP2000). The difference in terms of values cannot be measured due to difference in directions.

2. The reason of difference in results could be, the classical method used in this project are portal frame method and matrix displacement method whereas, portal frame method is an approximate method, it has many assumptions regarding point of contra flexure and distribution of horizontal shear. If only matrix displacement method had been used then no such difference would have observed.

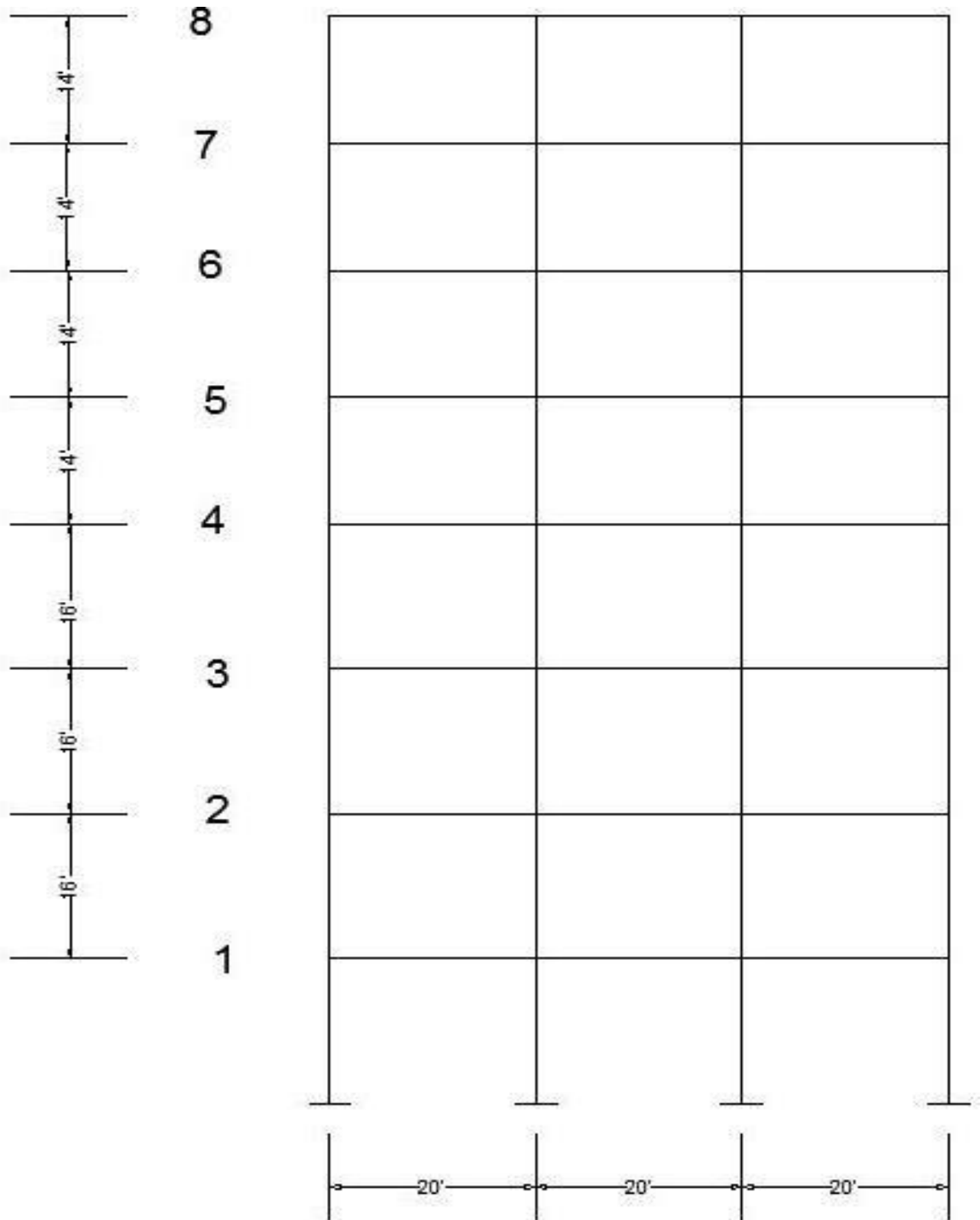
APPENDIX A

DRAWINGS

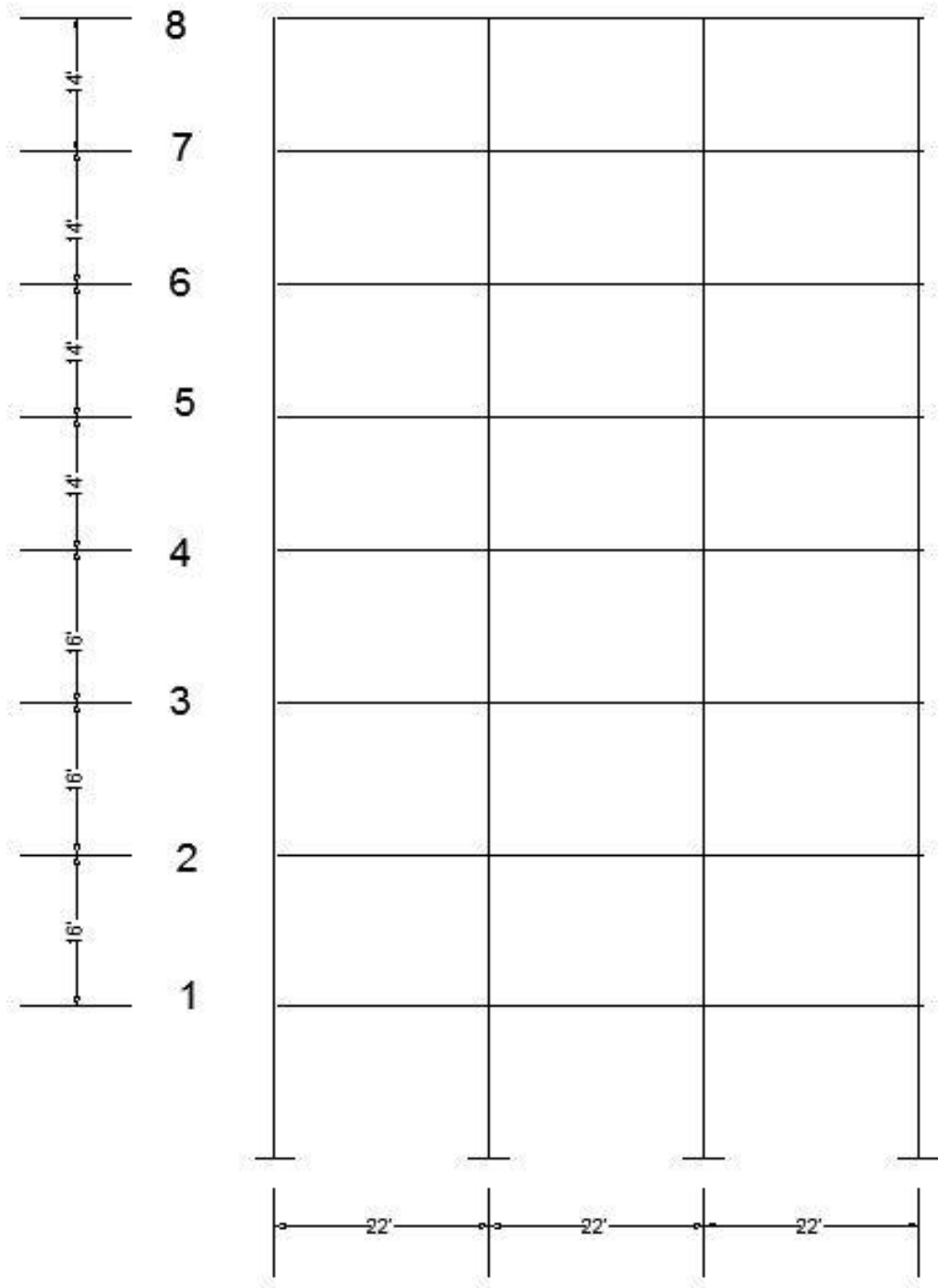
(Plan, Elevations)



PLAN



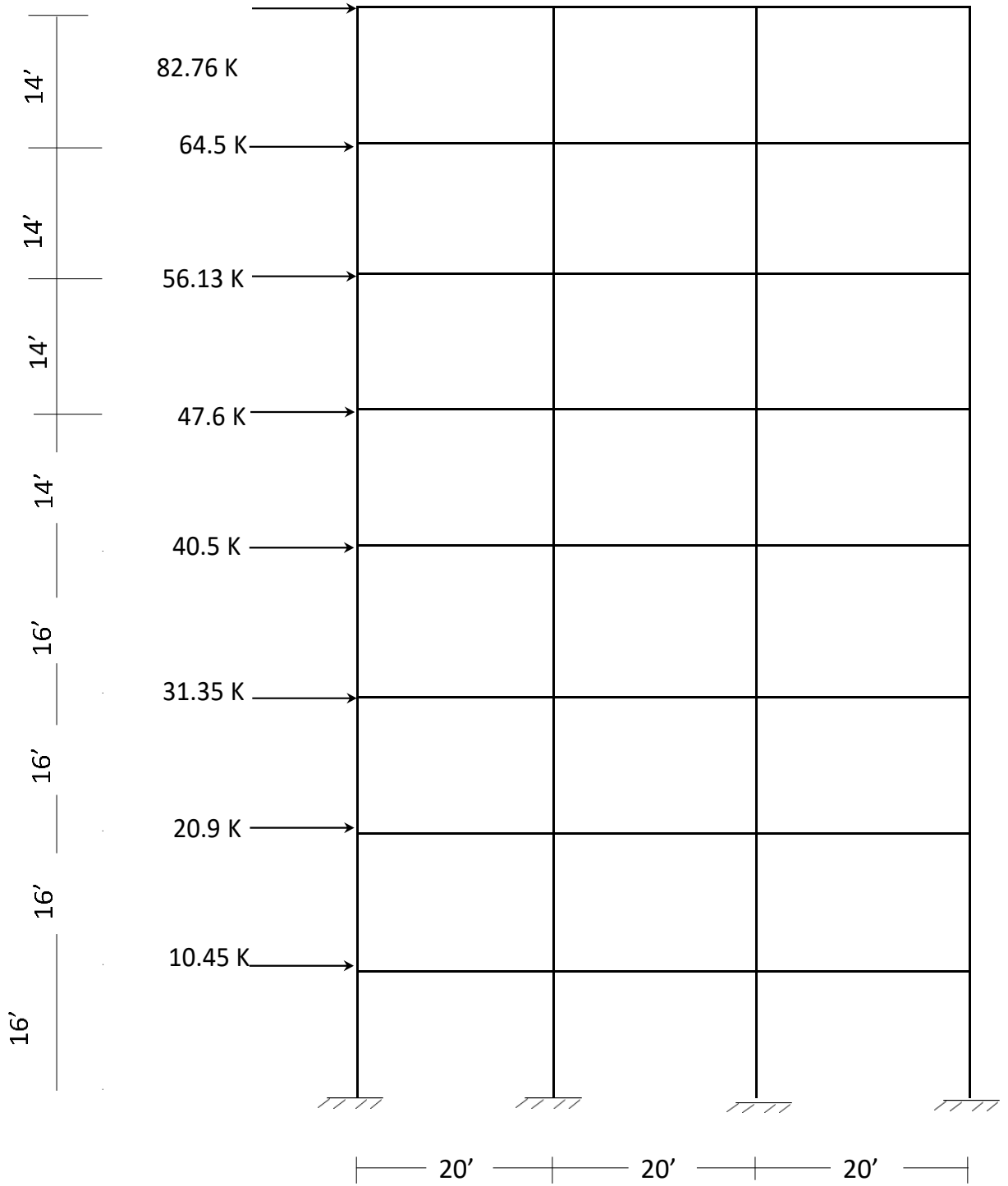
ELEVATION 1



ELEVATION 2

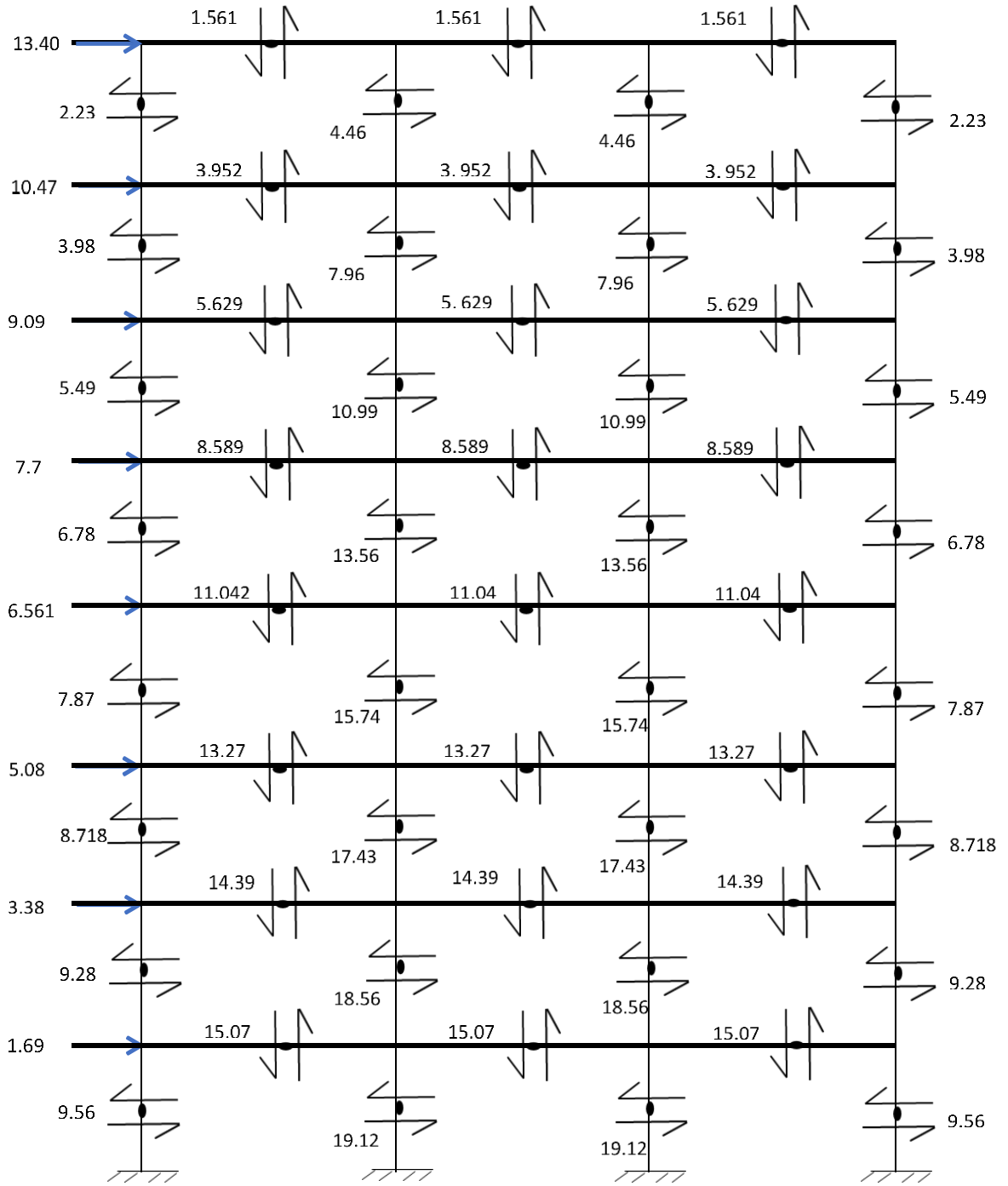
APPENDIX B
EARTHQUAKE ANALYSIS

STOREY FORCES



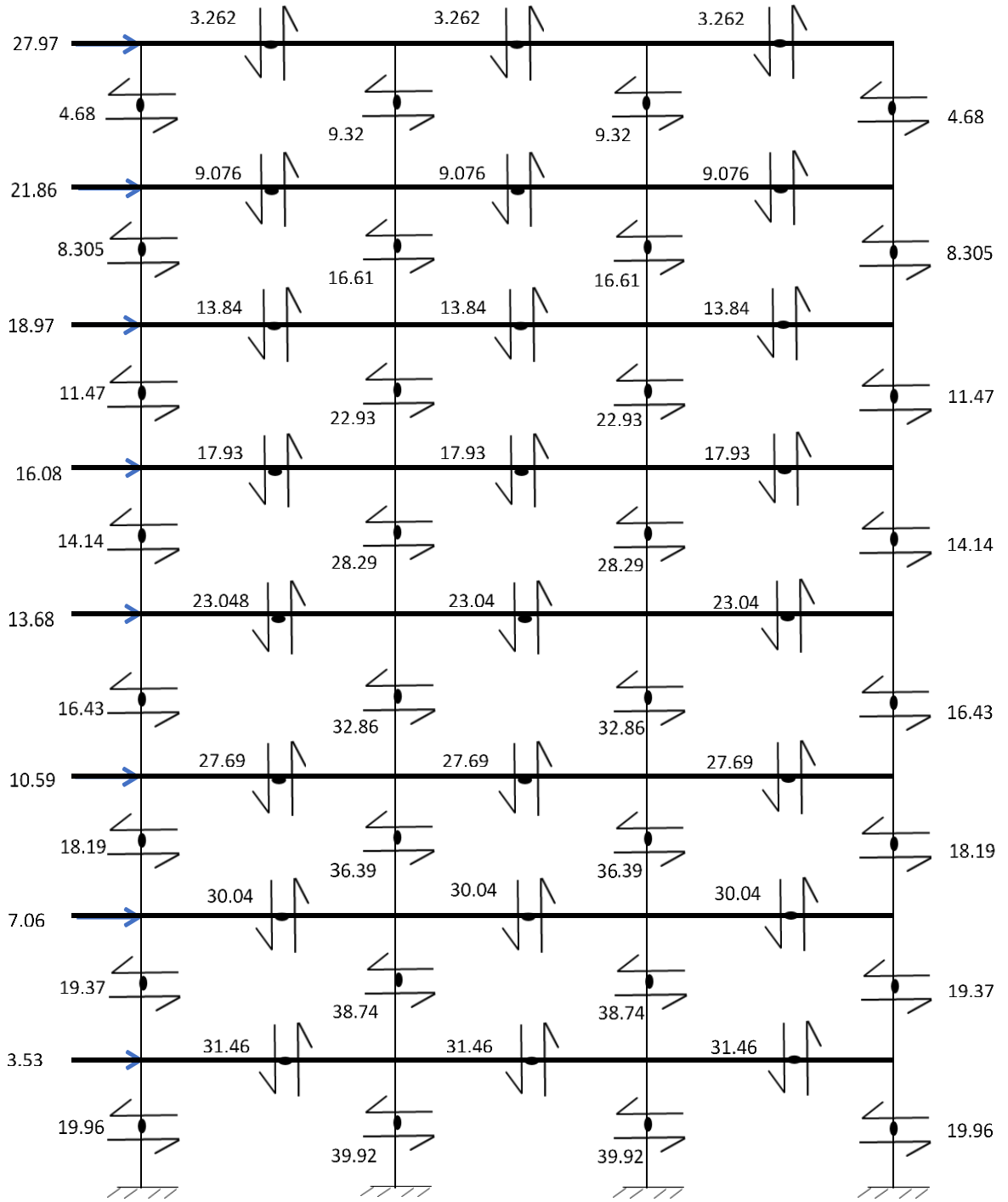
STOREY FORCES

SHEAR DISTRIBUTION



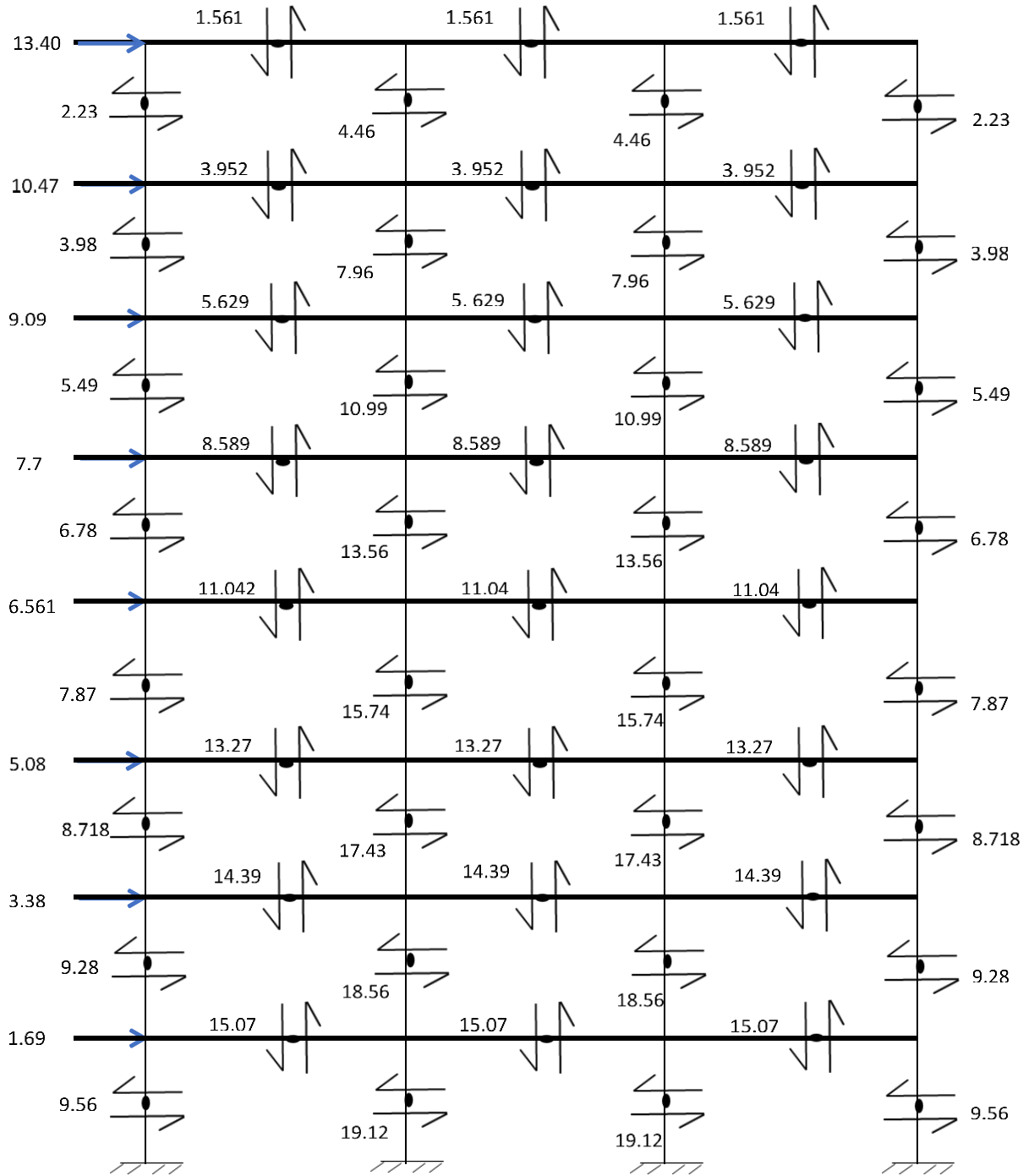
GRID 1&4

Note: All values are in kips.



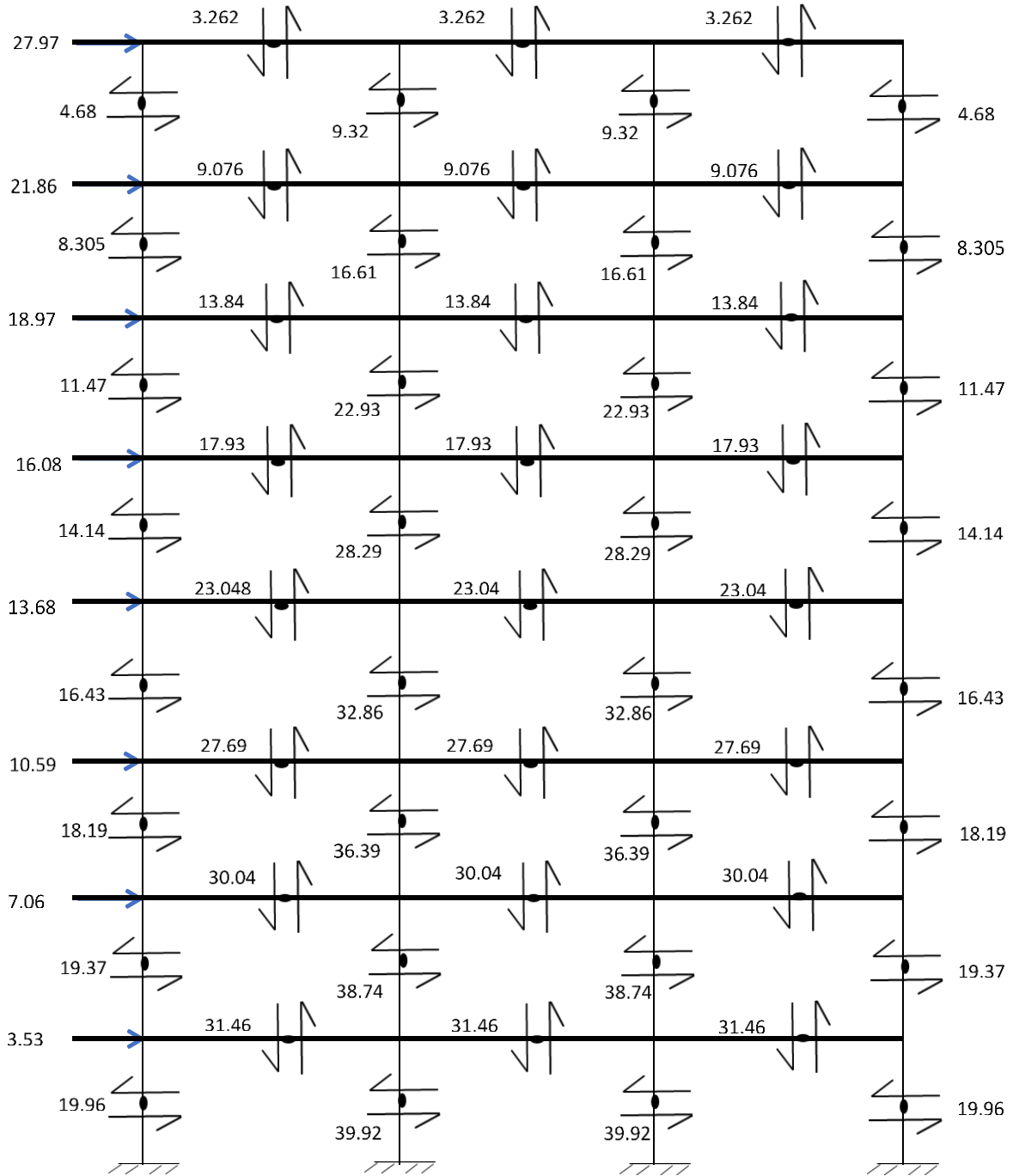
GRID 2&3

Note: All values are in kips.



GRID A&D

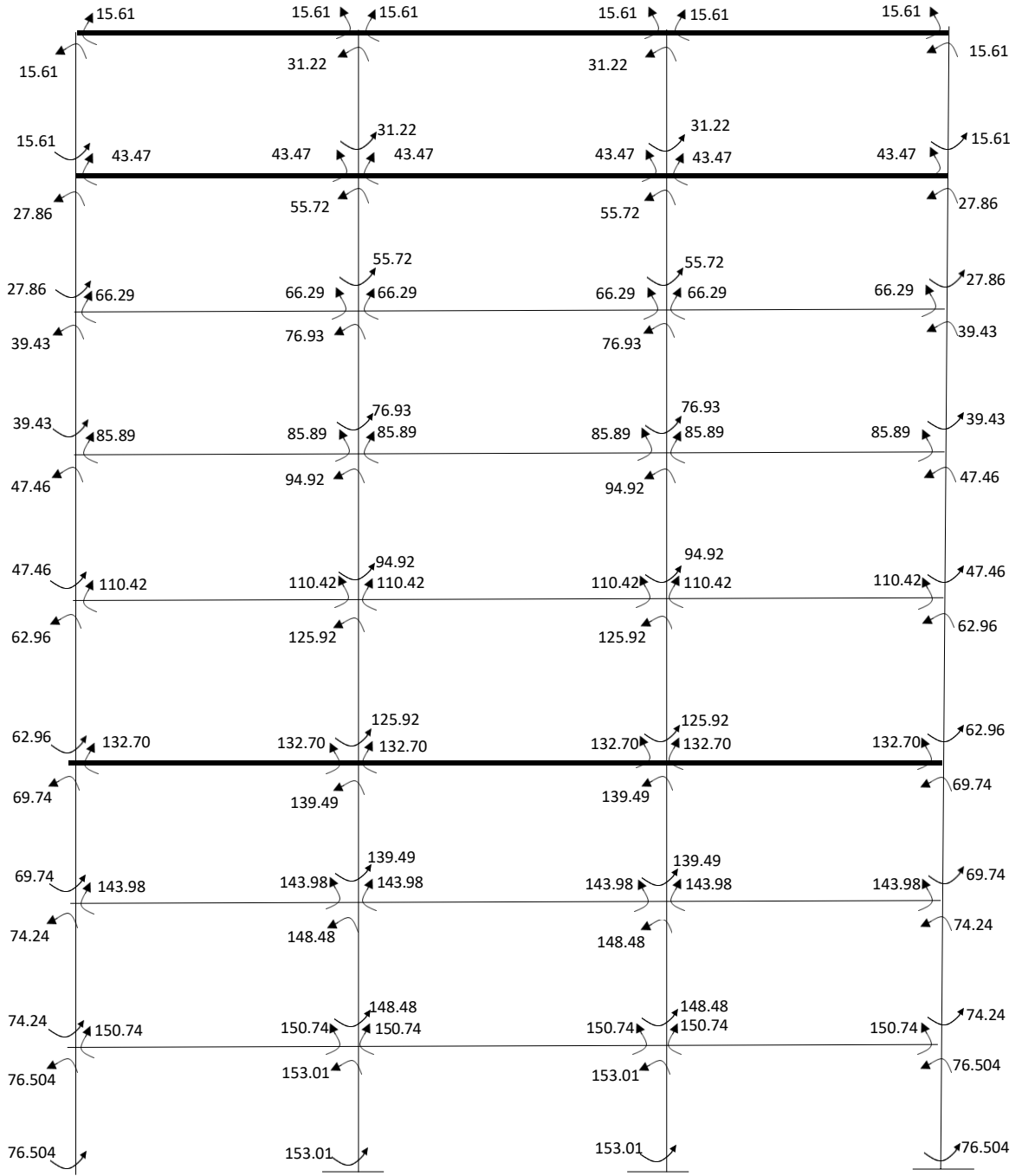
Note: All values are in kips.



GRID B&C

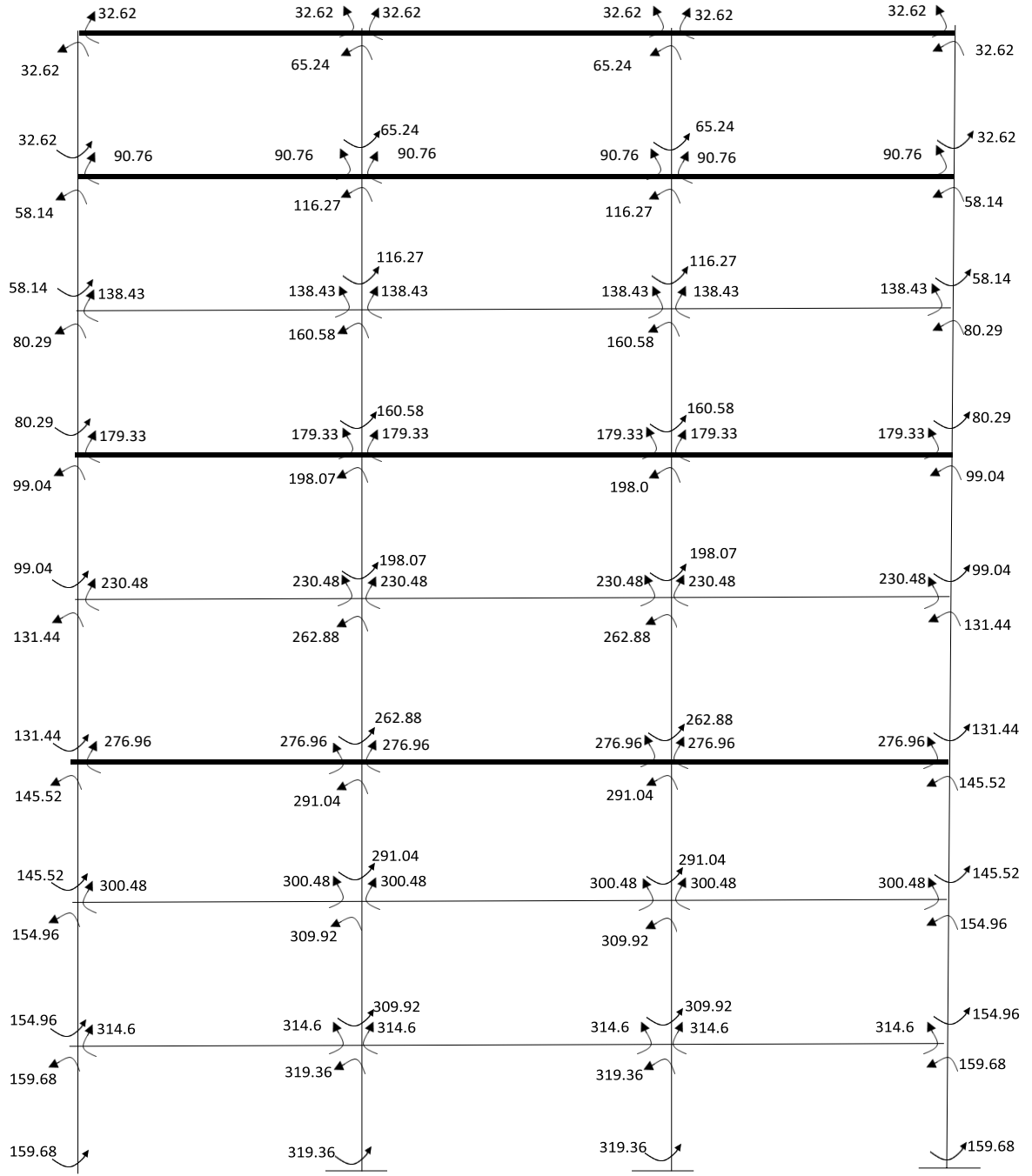
Note: All values are in kips.

END MOMENTS ON BEAMS AND COLUMNS



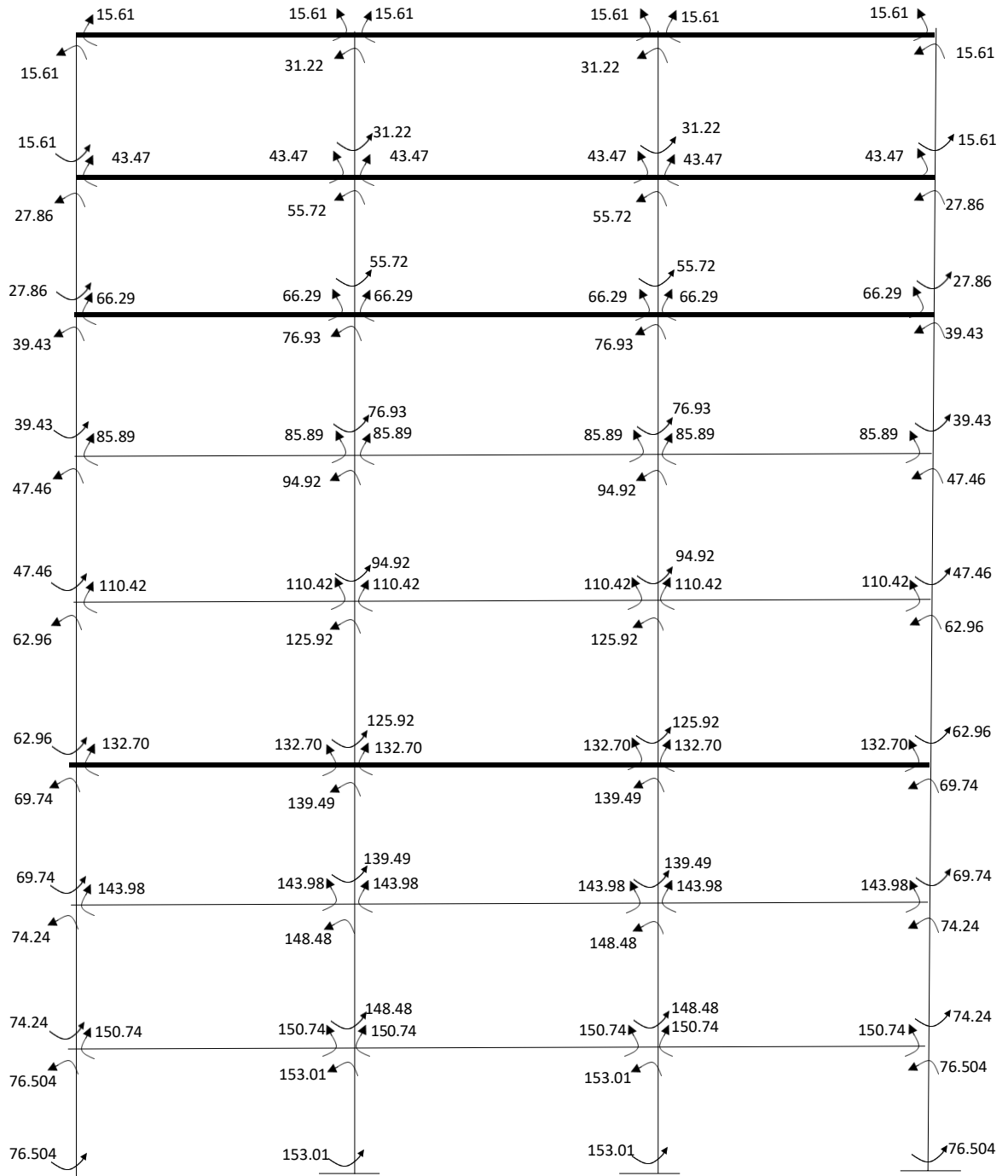
GRID 1&4

Note: All values are in kip-ft.



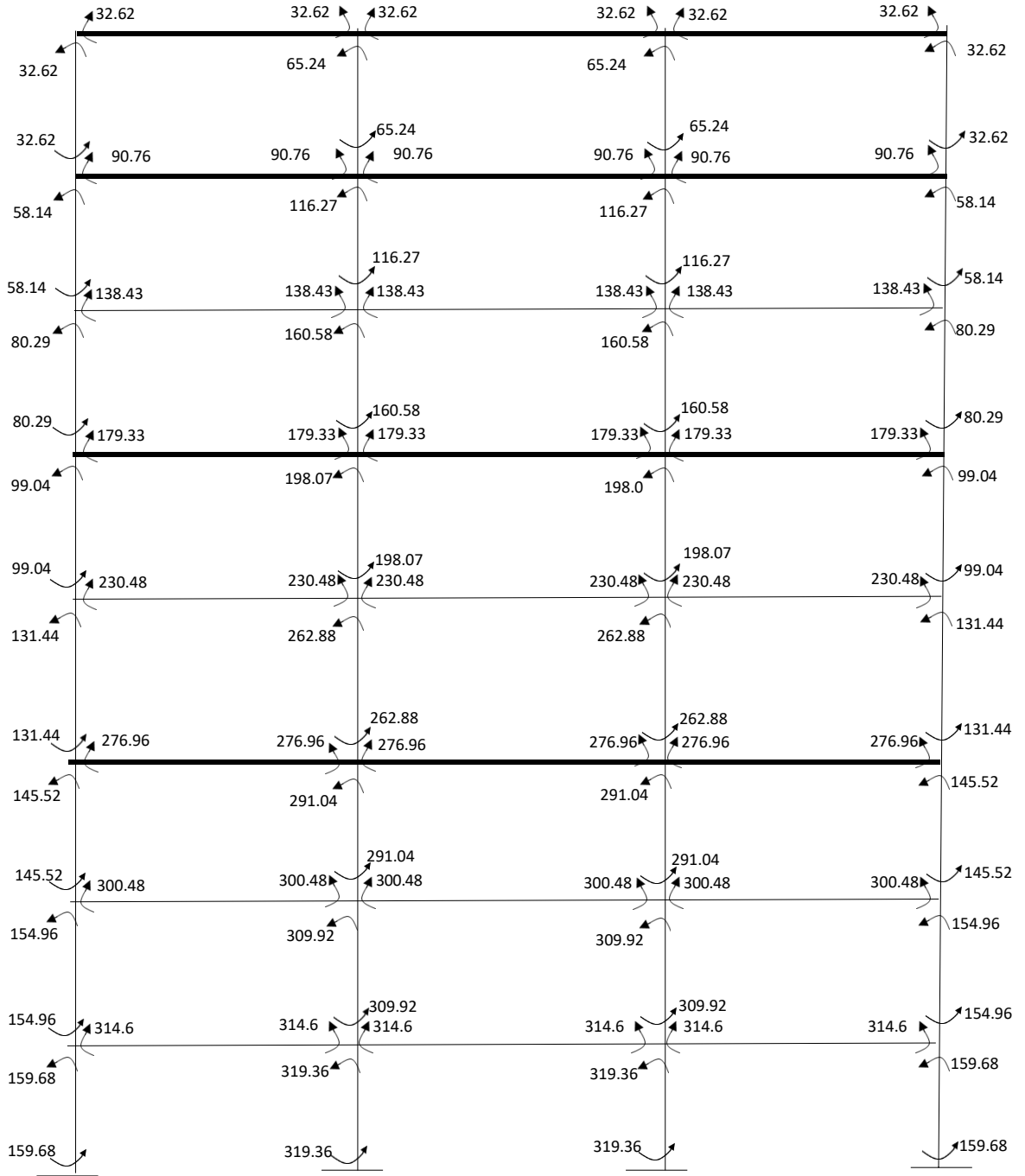
GRID 2&3

Note: All values are in kip-ft.



GRID A&D

Note: All values are in kip-ft.

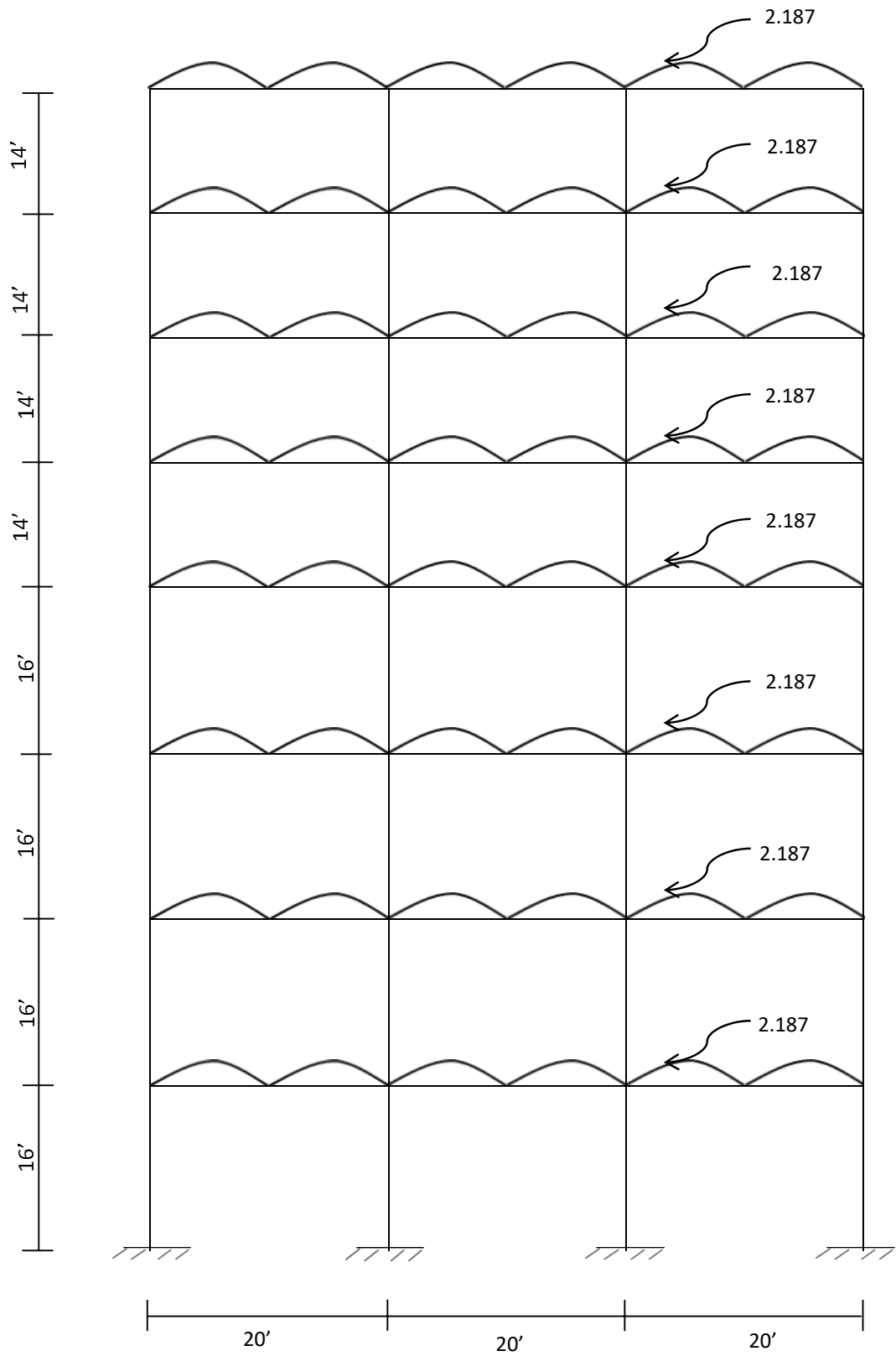


GRID B&C

Note: All values are in kip-ft.

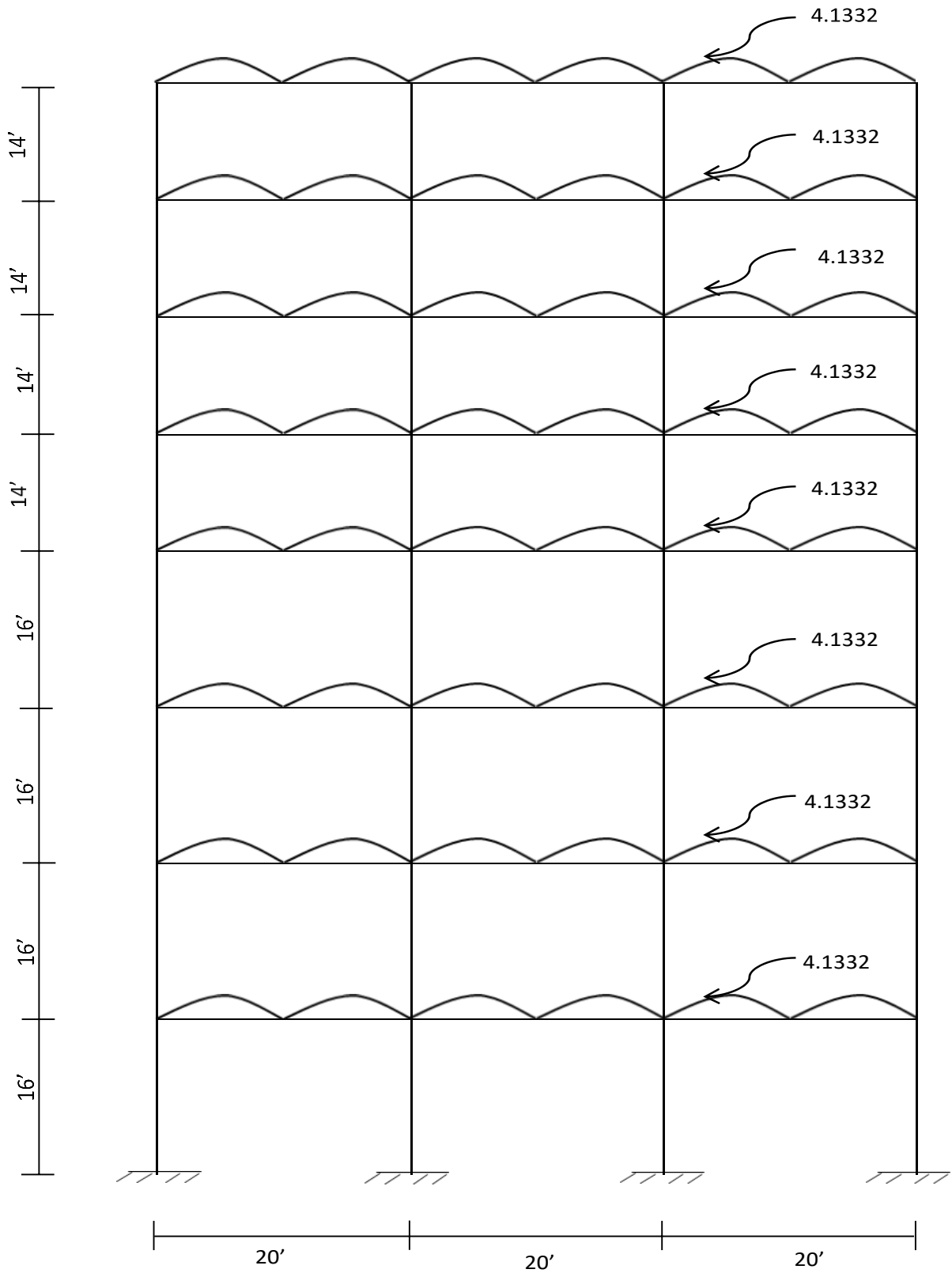
APPENDIX C
GRAVITY ANALYSIS

GRAVITY LOADS



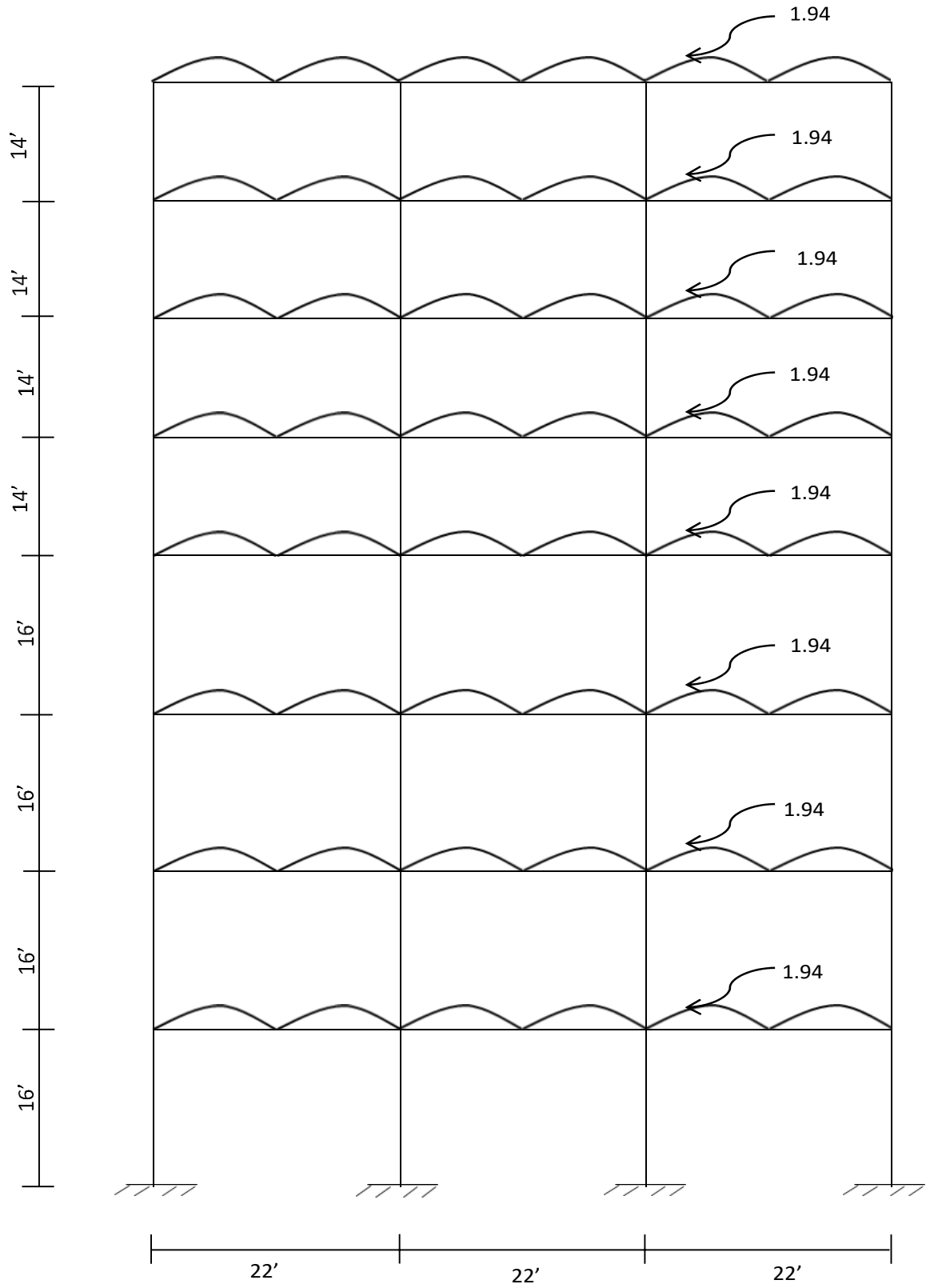
GRID 1&4

Note: All values are in kip/ft.



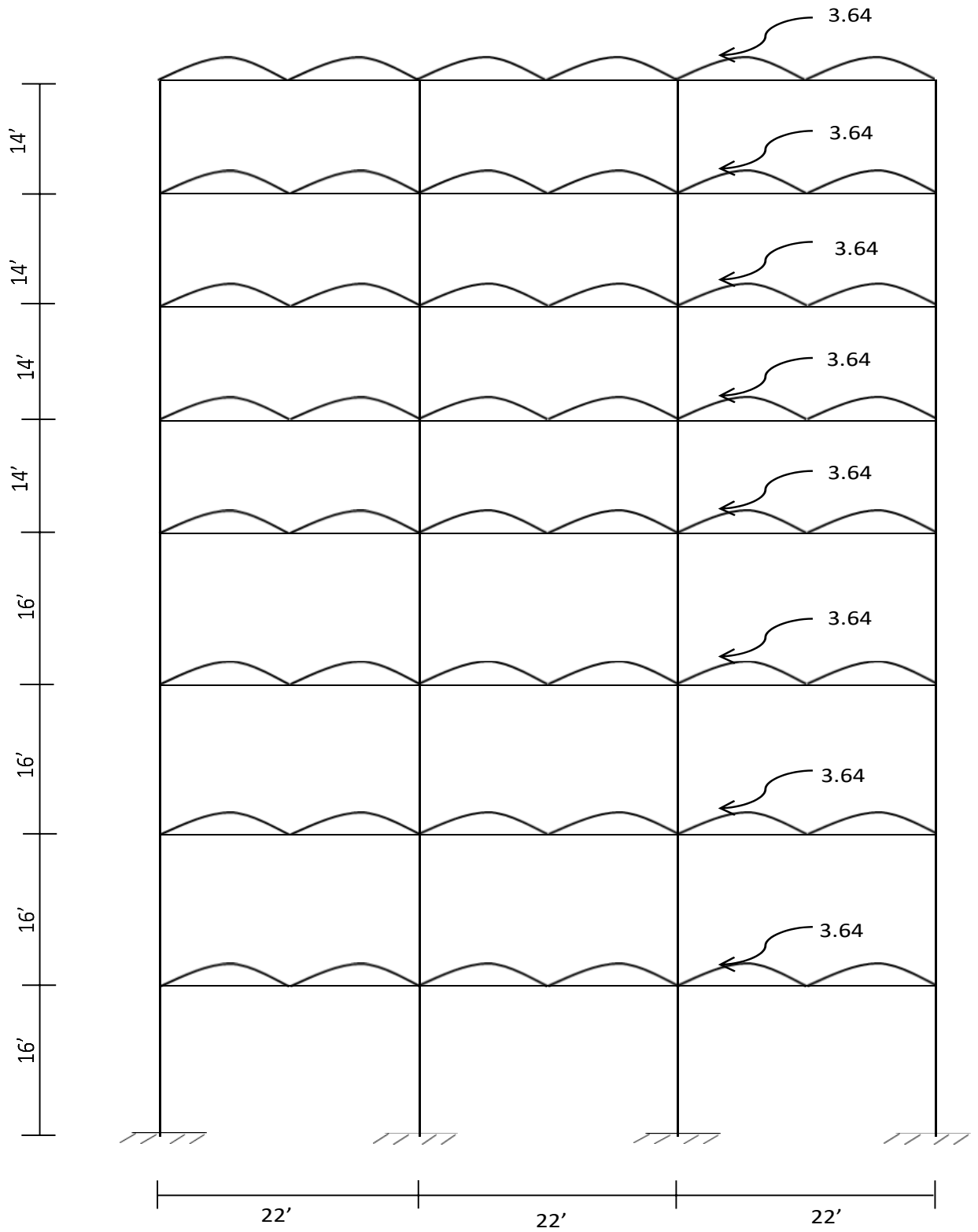
GRID 2&3

Note: All values are in kip/ft.



GRID A&D

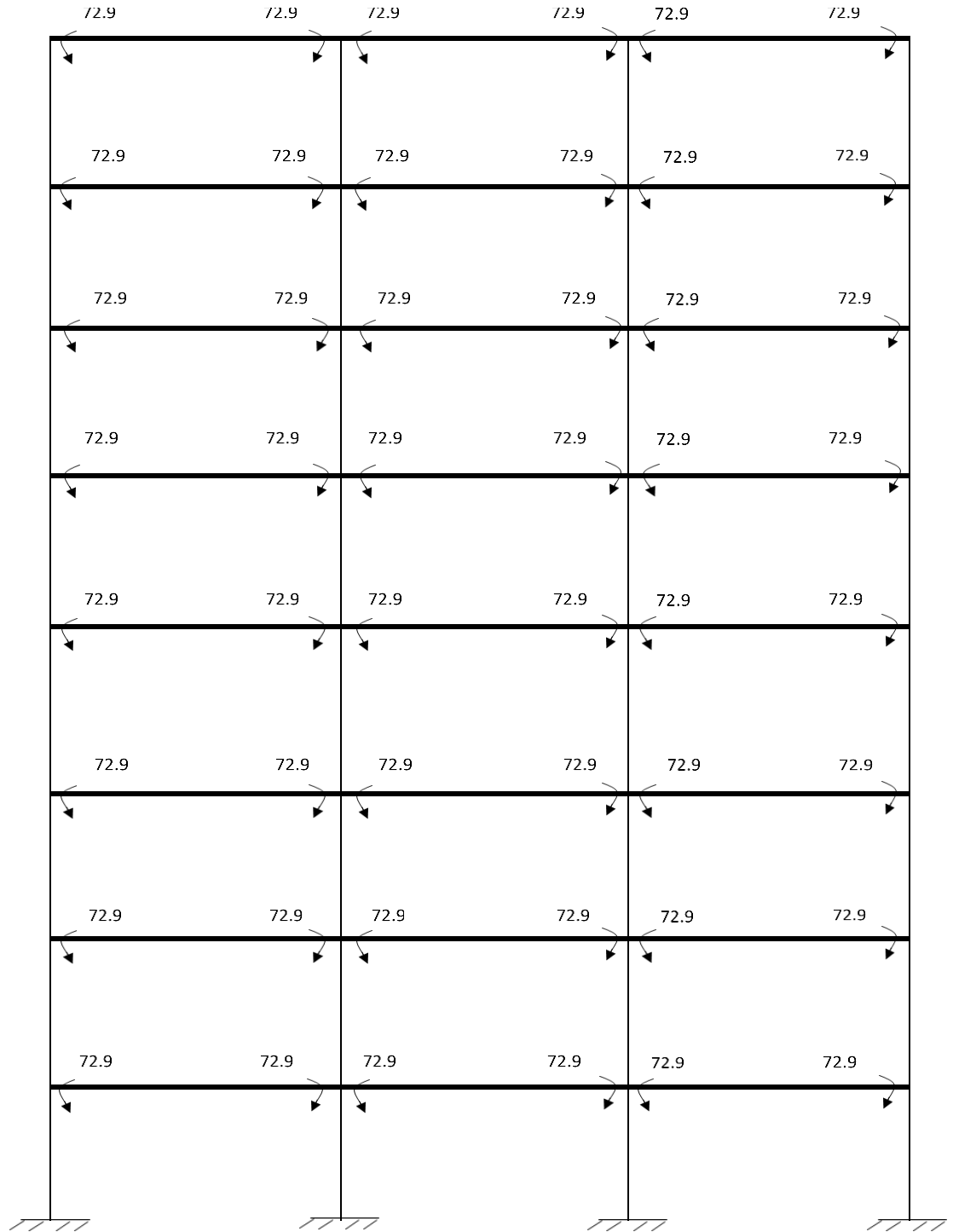
Note: All values are in kip/ft.



GRID B&C

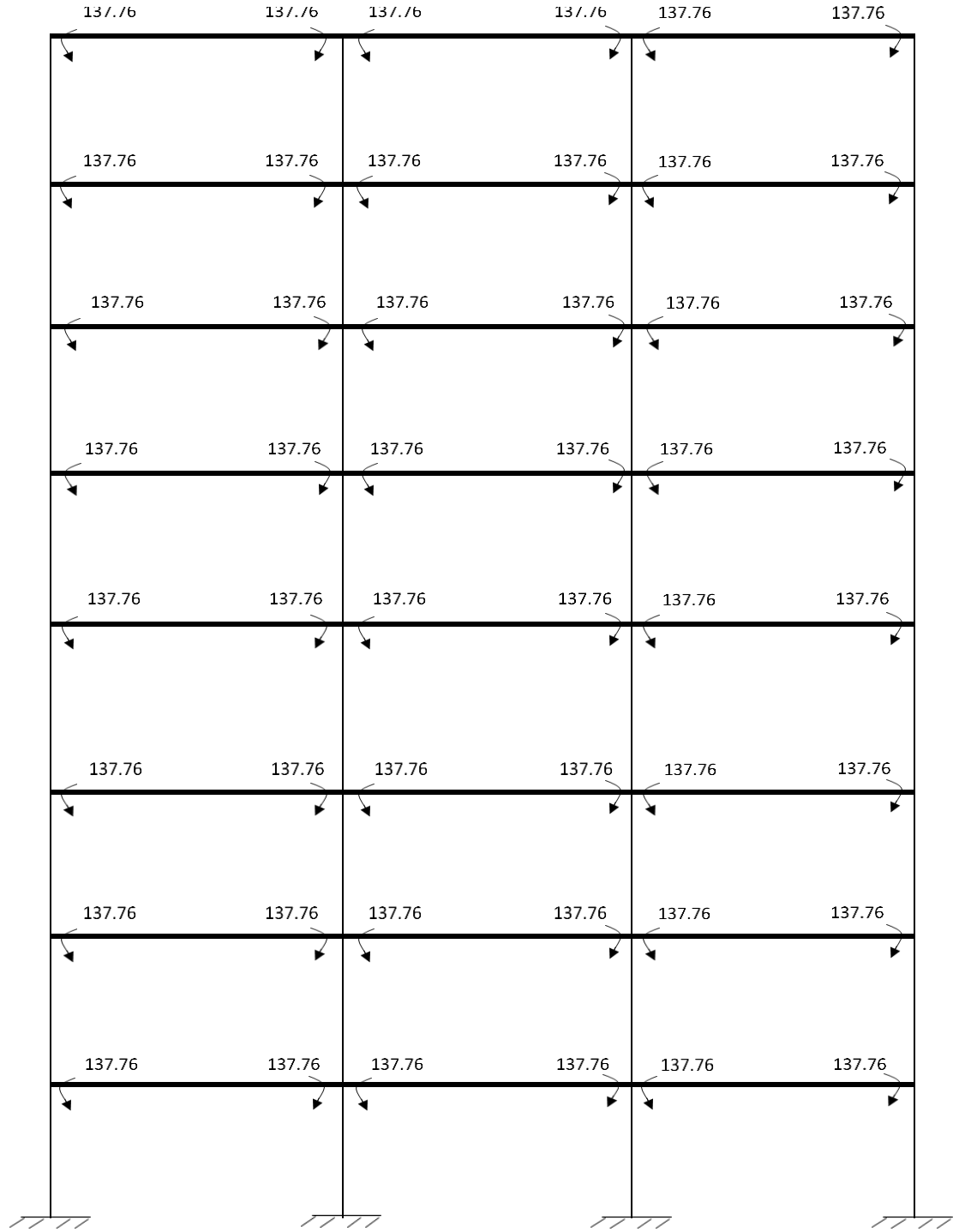
Note: All values are in kip/ft.

FIXED END MOMENTS



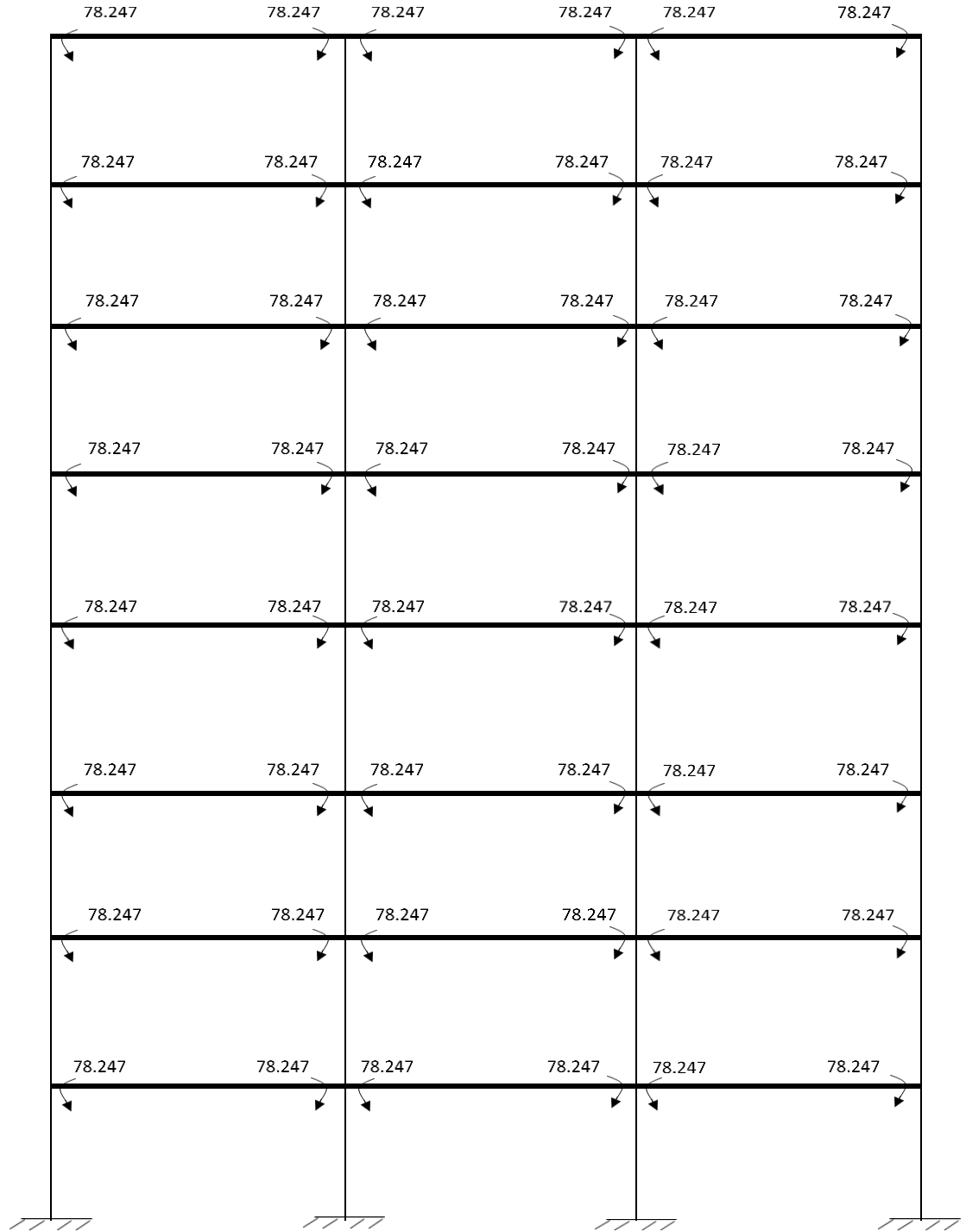
GRID 1&4

Note: All values are in kip-ft.



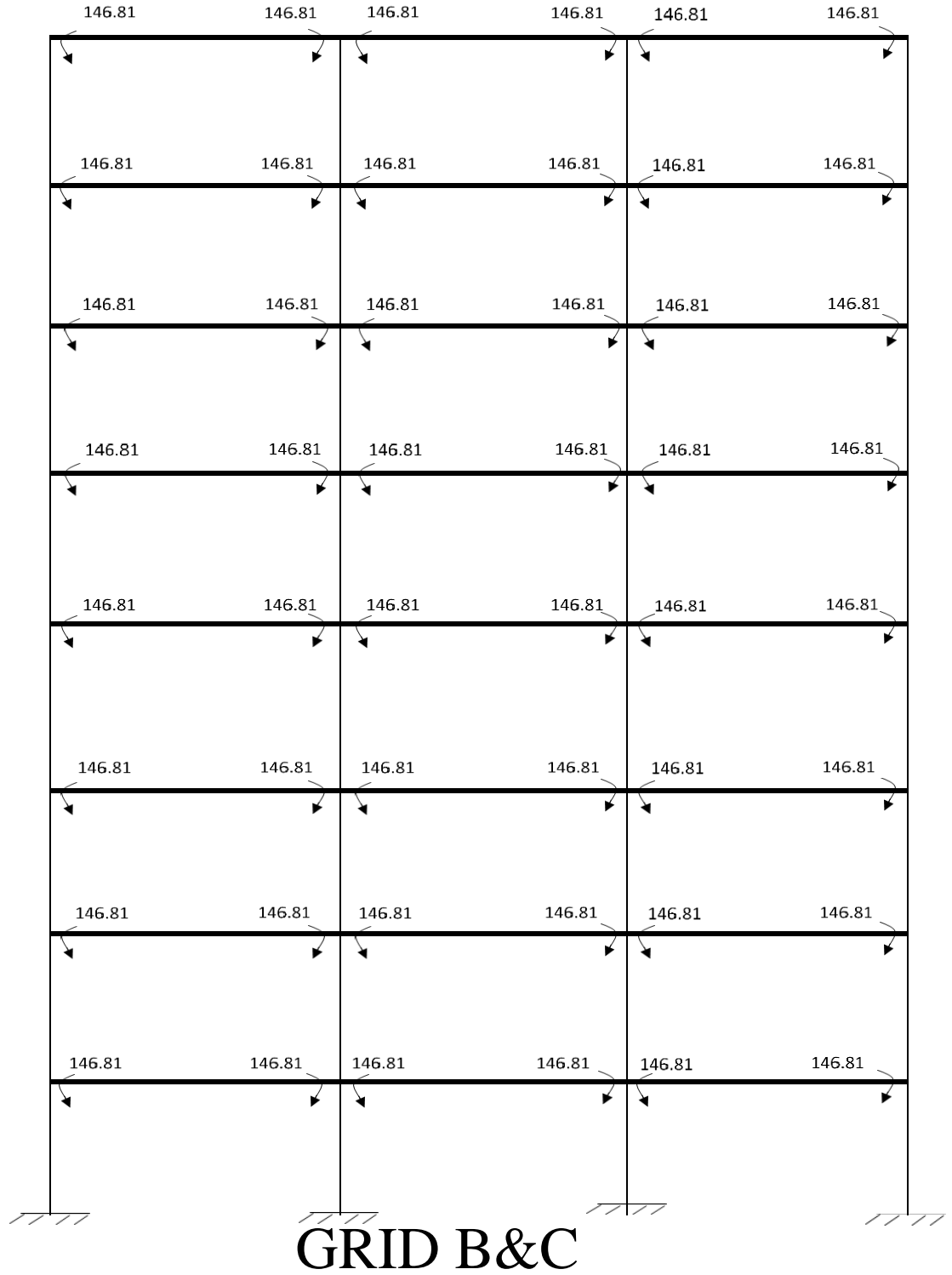
GRID 2&3

Note: All values are in kip-ft.



GRID A&D

Note: All values are in kip-ft.



Note: All values are in kip-ft.

LOAD MATRIX [P]
ELEVATION 1

P ₁	=	874.8
P ₂	=	0
P ₃	=	0
P ₄	=	-874.8
P ₅	=	874.8
P ₆	=	0
P ₇	=	0
P ₈	=	-874.8
P ₉	=	874.8
P ₁₀	=	0
P ₁₁	=	0
P ₁₂	=	-874.8
P ₁₃	=	874.8
P ₁₄	=	0
P ₁₅	=	0
P ₁₆	=	-874.8
P ₁₇	=	874.8
P ₁₈	=	0
P ₁₉	=	0
P ₂₀	=	-874.8
P ₂₁	=	874.8
P ₂₂	=	0
P ₂₃	=	0
P ₂₄	=	-874.8
P ₂₅	=	874.8
P ₂₆	=	0
P ₂₇	=	0
P ₂₈	=	-874.8
P ₂₉	=	874.8
P ₃₀	=	0
P ₃₁	=	0
P ₃₂	=	-874.8

P ₃₃	=	1653.204
P ₃₄	=	0
P ₃₅	=	0
P ₃₆	=	-1653.204
P ₃₇	=	1653.204
P ₃₈	=	0
P ₃₉	=	0
P ₄₀	=	-1653.204
P ₄₁	=	1653.204
P ₄₂	=	0
P ₄₃	=	0
P ₄₄	=	-1653.204
P ₄₅	=	1653.204
P ₄₆	=	0
P ₄₇	=	0
P ₄₈	=	-1653.204
P ₄₉	=	1653.204
P ₅₀	=	0
P ₅₁	=	0
P ₅₂	=	-1653.204
P ₅₃	=	1653.204
P ₅₄	=	0
P ₅₅	=	0
P ₅₆	=	-1653.204
P ₅₇	=	1653.204
P ₅₈	=	0
P ₅₉	=	0
P ₆₀	=	-1653.204
P ₆₁	=	1653.204
P ₆₂	=	0
P ₆₃	=	0
P ₆₄	=	-1653.204

GRID 1&4

GRID 2&3

Note: All values are in kip-in.

ELEVATION 2

P ₆₅	=	938.964
P ₆₆	=	0
P ₆₇	=	0
P ₆₈	=	-938.964
P ₆₉	=	938.964
P ₇₀	=	0
P ₇₁	=	0
P ₇₂	=	-938.964
P ₇₃	=	938.964
P ₇₄	=	0
P ₇₅	=	0
P ₇₆	=	-938.964
P ₇₇	=	938.964
P ₇₈	=	0
P ₇₉	=	0
P ₈₀	=	-938.964
P ₈₁	=	938.964
P ₈₂	=	0
P ₈₃	=	0
P ₈₄	=	-938.964
P ₈₅	=	938.964
P ₈₆	=	0
P ₈₇	=	0
P ₈₈	=	-938.964
P ₈₉	=	938.964
P ₉₀	=	0
P ₉₁	=	0
P ₉₂	=	-938.964
P ₉₃	=	938.964
P ₉₄	=	0
P ₉₅	=	0
P ₉₆	=	-938.964

P ₉₇	=	1761.76
P ₉₈	=	0
P ₉₉	=	0
P ₁₀₀	=	-1761.76
P ₁₀₁	=	1761.76
P ₁₀₂	=	0
P ₁₀₃	=	0
P ₁₀₄	=	-1761.76
P ₁₀₅	=	1761.76
P ₁₀₆	=	0
P ₁₀₇	=	0
P ₁₀₈	=	-1761.76
P ₁₀₉	=	1761.76
P ₁₁₀	=	0
P ₁₁₁	=	0
P ₁₁₂	=	-1761.76
P ₁₁₃	=	1761.76
P ₁₁₄	=	0
P ₁₁₅	=	0
P ₁₁₆	=	-1761.76
P ₁₁₇	=	1761.76
P ₁₁₈	=	0
P ₁₁₉	=	0
P ₁₂₀	=	-1761.76
P ₁₂₁	=	1761.76
P ₁₂₂	=	0
P ₁₂₃	=	0
P ₁₂₄	=	-1761.76
P ₁₂₅	=	1761.76
P ₁₂₆	=	0
P ₁₂₇	=	0
P ₁₂₈	=	-1761.76

GRID A&D

GRID B&C

Note: All values are in kip-in.

JOINT ROTATION MATRIX [X]

$$[X] = [K]^{-1} [P]$$

ELEVATION 1

X ₁	=	2.235626
X ₂	=	-0.3849
X ₃	=	0.384903
X ₄	=	-2.23563
X ₅	=	0.913685
X ₆	=	-0.02708
X ₇	=	0.027082
X ₈	=	-0.91369
X ₉	=	1.180001
X ₁₀	=	-0.12047
X ₁₁	=	0.120467
X ₁₂	=	-1.18
X ₁₃	=	1.112808
X ₁₄	=	-0.09455
X ₁₅	=	0.09455
X ₁₆	=	-1.11281
X ₁₇	=	1.195239
X ₁₈	=	-0.11262
X ₁₉	=	0.112621
X ₂₀	=	-1.19524
X ₂₁	=	1.283766
X ₂₂	=	-0.13167
X ₂₃	=	0.131674
X ₂₄	=	-1.28376
X ₂₅	=	1.214579
X ₂₆	=	-0.1095
X ₂₇	=	0.109495
X ₂₈	=	-1.21458
X ₂₉	=	1.500709
X ₃₀	=	-0.17693
X ₃₁	=	0.176929
X ₃₂	=	-1.50071

GRID 1&4

Note: All values are in radians.

X ₃₃	=	4.144840338
X ₃₄	=	-0.362677875
X ₃₅	=	0.362677875
X ₃₆	=	-4.144840338
X ₃₇	=	1.735980167
X ₃₈	=	0.011922575
X ₃₉	=	-0.011922575
X ₄₀	=	-1.735980167
X ₄₁	=	2.212649316
X ₄₂	=	-0.098524448
X ₄₃	=	0.098524448
X ₄₄	=	-2.212649316
X ₄₅	=	2.09334241
X ₄₆	=	-0.065254427
X ₄₇	=	0.065254427
X ₄₈	=	-2.09334241
X ₄₉	=	2.245303468
X ₅₀	=	-0.083337323
X ₅₁	=	0.083337323
X ₅₂	=	-2.245303468
X ₅₃	=	2.408471419
X ₅₄	=	-0.10047376
X ₅₅	=	0.10047376
X ₅₆	=	-2.408471419
X ₅₇	=	2.28383781
X ₅₈	=	-0.076787068
X ₅₉	=	0.076787068
X ₆₀	=	-2.28383781
X ₆₁	=	2.809281989
X ₆₂	=	-0.140106993
X ₆₃	=	0.140106993
X ₆₄	=	-2.809281989

GRID 2&3

ELEVATION 2

X ₆₅	=	2.5199837
X ₆₆	=	-0.56321
X ₆₇	=	0.5632672
X ₆₈	=	-2.520158
X ₆₉	=	0.9731169
X ₇₀	=	0.0066642
X ₇₁	=	-0.006797
X ₇₂	=	-0.972572
X ₇₃	=	1.2921403
X ₇₄	=	-0.128946
X ₇₅	=	0.1295023
X ₇₆	=	-1.294788
X ₇₇	=	1.2261826
X ₇₈	=	-0.097994
X ₇₉	=	0.0958128
X ₈₀	=	-1.212962
X ₈₁	=	1.2386552
X ₈₂	=	-0.102385
X ₈₃	=	0.1090016
X ₈₄	=	-1.305149
X ₈₅	=	1.4182294
X ₈₆	=	-0.138513
X ₈₇	=	0.1363515
X ₈₈	=	-1.405465
X ₈₉	=	1.3230052
X ₉₀	=	-0.109919
X ₉₁	=	0.1104502
X ₉₂	=	-1.32547
X ₉₃	=	1.6483003
X ₉₄	=	-0.183001
X ₉₅	=	0.1828879
X ₉₆	=	-1.647839

GRID A&D

Note: All values are in radians.

X ₉₇	=	4.79098
X ₉₈	=	-1.311269
X ₉₉	=	1.311485
X ₁₀₀	=	-4.791321
X ₁₀₁	=	1.786708
X ₁₀₂	=	0.233207
X ₁₀₃	=	-0.233432
X ₁₀₄	=	-1.785712
X ₁₀₅	=	2.422703
X ₁₀₆	=	-0.149048
X ₁₀₇	=	0.14976
X ₁₀₈	=	-2.427526
X ₁₀₉	=	2.286698
X ₁₁₀	=	-0.056328
X ₁₁₁	=	0.053975
X ₁₁₂	=	-2.262415
X ₁₁₃	=	2.314883
X ₁₁₄	=	-0.074465
X ₁₁₅	=	0.080511
X ₁₁₆	=	-2.438163
X ₁₁₇	=	2.642889
X ₁₁₈	=	-0.103831
X ₁₁₉	=	0.101447
X ₁₂₀	=	-2.619463
X ₁₂₁	=	2.472147
X ₁₂₂	=	-0.074959
X ₁₂₃	=	0.075658
X ₁₂₄	=	-2.476629
X ₁₂₅	=	3.066555
X ₁₂₆	=	-0.141427
X ₁₂₇	=	0.141254
X ₁₂₈	=	-3.06572

GRID B&C

MEMBER ROTATION MATRIX [e]

$$[e] = [B] [X]$$

ELEVATION 1

e ₁	=	2.235626
e ₂	=	-0.3849
e ₃	=	-0.3849
e ₄	=	0.384903
e ₅	=	0.384903
e ₆	=	-2.23563
e ₇	=	0.913685
e ₈	=	-0.02708
e ₉	=	-0.02708
e ₁₀	=	0.027082
e ₁₁	=	0.027082
e ₁₂	=	-0.91369
e ₁₃	=	1.180001
e ₁₄	=	-0.12047
e ₁₅	=	-0.12047
e ₁₆	=	0.120467
e ₁₇	=	0.120467
e ₁₈	=	-1.18
e ₁₉	=	1.112808
e ₂₀	=	-0.09455
e ₂₁	=	-0.09455
e ₂₂	=	0.09455
e ₂₃	=	0.09455
e ₂₄	=	-1.11281
e ₂₅	=	1.195239
e ₂₆	=	-0.11262
e ₂₇	=	-0.11262
e ₂₈	=	0.112621

e ₂₉	=	0.112621
e ₃₀	=	-1.19524
e ₃₁	=	1.283766
e ₃₂	=	-0.13167
e ₃₃	=	-0.13167
e ₃₄	=	0.131674
e ₃₅	=	0.131674
e ₃₆	=	-1.28376
e ₃₇	=	1.214579
e ₃₈	=	-0.1095
e ₃₉	=	-0.1095
e ₄₀	=	0.109495
e ₄₁	=	0.109495
e ₄₂	=	-1.21458
e ₄₃	=	1.500709
e ₄₄	=	-0.17693
e ₄₅	=	-0.17693
e ₄₆	=	0.176929
e ₄₇	=	0.176929
e ₄₈	=	-1.50071
e ₄₉	=	2.235626
e ₅₀	=	0.913685
e ₅₁	=	-0.3849
e ₅₂	=	-0.02708
e ₅₃	=	0.384903
e ₅₄	=	0.027082
e ₅₅	=	-2.23563
e ₅₆	=	-0.91369

e ₅₇	=	0.913685
e ₅₈	=	1.180001
e ₅₉	=	-0.02708
e ₆₀	=	-0.12047
e ₆₁	=	0.027082
e ₆₂	=	0.120467
e ₆₃	=	-0.91369
e ₆₄	=	-1.18
e ₆₅	=	1.180001
e ₆₆	=	1.112808
e ₆₇	=	-0.12047
e ₆₈	=	-0.09455
e ₆₉	=	0.120467
e ₇₀	=	0.09455
e ₇₁	=	-1.18
e ₇₂	=	-1.11281
e ₇₃	=	1.112808
e ₇₄	=	1.195239
e ₇₅	=	-0.09455
e ₇₆	=	-0.11262
e ₇₇	=	0.09455
e ₇₈	=	0.112621
e ₇₉	=	-1.11281
e ₈₀	=	-1.19524
e ₈₁	=	1.195239
e ₈₂	=	1.283766
e ₈₃	=	-0.11262
e ₈₄	=	-0.13167

e ₈₅	=	0.112621
e ₈₆	=	0.131674
e ₈₇	=	-1.19524
e ₈₈	=	-1.28376
e ₈₉	=	1.283766
e ₉₀	=	1.214579
e ₉₁	=	-0.13167
e ₉₂	=	-0.1095
e ₉₃	=	0.131674
e ₉₄	=	0.109495
e ₉₅	=	-1.28376
e ₉₆	=	-1.21458
e ₉₇	=	1.214579
e ₉₈	=	1.500709
e ₉₉	=	-0.1095
e ₁₀₀	=	-0.17693
e ₁₀₁	=	0.109495
e ₁₀₂	=	0.176929
e ₁₀₃	=	-1.21458
e ₁₀₄	=	-1.50071
e ₁₀₅	=	1.500709
e ₁₀₆	=	0
e ₁₀₇	=	-0.17693
e ₁₀₈	=	0
e ₁₀₉	=	0.176929
e ₁₁₀	=	0
e ₁₁₁	=	-1.50071
e ₁₁₂	=	0

GRID 1&4

Note: All values are in radians.

e ₁₁₃	=	4.14484
e ₁₁₄	=	-0.36268
e ₁₁₅	=	-0.36268
e ₁₁₆	=	0.362678
e ₁₁₇	=	0.362678
e ₁₁₈	=	-4.14484
e ₁₁₉	=	1.73598
e ₁₂₀	=	0.011923
e ₁₂₁	=	0.011923
e ₁₂₂	=	-0.01192
e ₁₂₃	=	-0.01192
e ₁₂₄	=	-1.73598
e ₁₂₅	=	2.212649
e ₁₂₆	=	-0.09852
e ₁₂₇	=	-0.09852
e ₁₂₈	=	0.098524
e ₁₂₉	=	0.098524
e ₁₃₀	=	-2.21265
e ₁₃₁	=	2.093342
e ₁₃₂	=	-0.06525
e ₁₃₃	=	-0.06525
e ₁₃₄	=	0.065254
e ₁₃₅	=	0.065254
e ₁₃₆	=	-2.09334
e ₁₃₇	=	2.245303
e ₁₃₈	=	-0.08334
e ₁₃₉	=	-0.08334
e ₁₄₀	=	0.083337

e ₁₄₁	=	0.083337
e ₁₄₂	=	-2.2453
e ₁₄₃	=	2.408471
e ₁₄₄	=	-0.10047
e ₁₄₅	=	-0.10047
e ₁₄₆	=	0.100474
e ₁₄₇	=	0.100474
e ₁₄₈	=	-2.40847
e ₁₄₉	=	2.283838
e ₁₅₀	=	-0.07679
e ₁₅₁	=	-0.07679
e ₁₅₂	=	0.076787
e ₁₅₃	=	0.076787
e ₁₅₄	=	-2.28384
e ₁₅₅	=	2.809282
e ₁₅₆	=	-0.14011
e ₁₅₇	=	-0.14011
e ₁₅₈	=	0.140107
e ₁₅₉	=	0.140107
e ₁₆₀	=	-2.80928
e ₁₆₁	=	4.14484
e ₁₆₂	=	1.73598
e ₁₆₃	=	-0.36268
e ₁₆₄	=	0.011923
e ₁₆₅	=	0.362678
e ₁₆₆	=	-0.01192
e ₁₆₇	=	-4.14484
e ₁₆₈	=	-1.73598

e ₁₆₉	=	1.73598
e ₁₇₀	=	2.212649
e ₁₇₁	=	0.011923
e ₁₇₂	=	-0.09852
e ₁₇₃	=	-0.01192
e ₁₇₄	=	0.098524
e ₁₇₅	=	-1.73598
e ₁₇₆	=	-2.21265
e ₁₇₇	=	2.212649
e ₁₇₈	=	2.093342
e ₁₇₉	=	-0.09852
e ₁₈₀	=	-0.06525
e ₁₈₁	=	0.098524
e ₁₈₂	=	0.065254
e ₁₈₃	=	-2.21265
e ₁₈₄	=	-2.09334
e ₁₈₅	=	2.093342
e ₁₈₆	=	2.245303
e ₁₈₇	=	-0.06525
e ₁₈₈	=	-0.08334
e ₁₈₉	=	0.065254
e ₁₉₀	=	0.083337
e ₁₉₁	=	-2.09334
e ₁₉₂	=	-2.2453
e ₁₉₃	=	2.245303
e ₁₉₄	=	2.408471
e ₁₉₅	=	-0.08334
e ₁₉₆	=	-0.10047

e ₁₉₇	=	0.083337
e ₁₉₈	=	0.100474
e ₁₉₉	=	-2.2453
e ₂₀₀	=	-2.40847
e ₂₀₁	=	2.408471
e ₂₀₂	=	2.283838
e ₂₀₃	=	-0.10047
e ₂₀₄	=	-0.07679
e ₂₀₅	=	0.100474
e ₂₀₆	=	0.076787
e ₂₀₇	=	-2.40847
e ₂₀₈	=	-2.28384
e ₂₀₉	=	2.283838
e ₂₁₀	=	2.809282
e ₂₁₁	=	-0.07679
e ₂₁₂	=	-0.14011
e ₂₁₃	=	0.076787
e ₂₁₄	=	0.140107
e ₂₁₅	=	-2.28384
e ₂₁₆	=	-2.80928
e ₂₁₇	=	2.809282
e ₂₁₈	=	0
e ₂₁₉	=	-0.14011
e ₂₂₀	=	0
e ₂₂₁	=	0.140107
e ₂₂₂	=	0
e ₂₂₃	=	-2.80928
e ₂₂₄	=	0

GRID 2&3

Note: All values are in radians.

ELEVATION 2

e ₂₂₅	=	2.519984
e ₂₂₆	=	-0.56321
e ₂₂₇	=	-0.56321
e ₂₂₈	=	0.563267
e ₂₂₉	=	0.563267
e ₂₃₀	=	-2.52016
e ₂₃₁	=	0.973117
e ₂₃₂	=	0.006664
e ₂₃₃	=	0.006664
e ₂₃₄	=	-0.0068
e ₂₃₅	=	-0.0068
e ₂₃₆	=	-0.97257
e ₂₃₇	=	1.29214
e ₂₃₈	=	-0.12895
e ₂₃₉	=	-0.12895
e ₂₄₀	=	0.129502
e ₂₄₁	=	0.129502
e ₂₄₂	=	-1.29479
e ₂₄₃	=	1.226183
e ₂₄₄	=	-0.09799
e ₂₄₅	=	-0.09799
e ₂₄₆	=	0.095813
e ₂₄₇	=	0.095813
e ₂₄₈	=	-1.21296
e ₂₄₉	=	1.238655
e ₂₅₀	=	-0.10239
e ₂₅₁	=	-0.10239
e ₂₅₂	=	0.109002

e ₂₅₃	=	0.109002
e ₂₅₄	=	-1.30515
e ₂₅₅	=	1.418229
e ₂₅₆	=	-0.13851
e ₂₅₇	=	-0.13851
e ₂₅₈	=	0.136352
e ₂₅₉	=	0.136352
e ₂₆₀	=	-1.40546
e ₂₆₁	=	1.323005
e ₂₆₂	=	-0.10992
e ₂₆₃	=	-0.10992
e ₂₆₄	=	0.11045
e ₂₆₅	=	0.11045
e ₂₆₆	=	-1.32547
e ₂₆₇	=	1.6483
e ₂₆₈	=	-0.183
e ₂₆₉	=	-0.183
e ₂₇₀	=	0.182888
e ₂₇₁	=	0.182888
e ₂₇₂	=	-1.64784
e ₂₇₃	=	2.519984
e ₂₇₄	=	0.973117
e ₂₇₅	=	-0.56321
e ₂₇₆	=	0.006664
e ₂₇₇	=	0.563267
e ₂₇₈	=	-0.0068
e ₂₇₉	=	-2.52016
e ₂₈₀	=	-0.97257

e ₂₈₁	=	0.973117
e ₂₈₂	=	1.29214
e ₂₈₃	=	0.006664
e ₂₈₄	=	-0.12895
e ₂₈₅	=	-0.0068
e ₂₈₆	=	0.129502
e ₂₈₇	=	-0.97257
e ₂₈₈	=	-1.29479
e ₂₈₉	=	1.29214
e ₂₉₀	=	1.226183
e ₂₉₁	=	-0.12895
e ₂₉₂	=	-0.09799
e ₂₉₃	=	0.129502
e ₂₉₄	=	0.095813
e ₂₉₅	=	-1.29479
e ₂₉₆	=	-1.21296
e ₂₉₇	=	1.226183
e ₂₉₈	=	1.238655
e ₂₉₉	=	-0.09799
e ₃₀₀	=	-0.10239
e ₃₀₁	=	0.095813
e ₃₀₂	=	0.109002
e ₃₀₃	=	-1.21296
e ₃₀₄	=	-1.30515
e ₃₀₅	=	1.238655
e ₃₀₆	=	1.418229
e ₃₀₇	=	-0.10239
e ₃₀₈	=	-0.13851

e ₃₀₉	=	0.109002
e ₃₁₀	=	0.136352
e ₃₁₁	=	-1.30515
e ₃₁₂	=	-1.40546
e ₃₁₃	=	1.418229
e ₃₁₄	=	1.323005
e ₃₁₅	=	-0.13851
e ₃₁₆	=	-0.10992
e ₃₁₇	=	0.136352
e ₃₁₈	=	0.11045
e ₃₁₉	=	-1.40546
e ₃₂₀	=	-1.32547
e ₃₂₁	=	1.323005
e ₃₂₂	=	1.6483
e ₃₂₃	=	-0.10992
e ₃₂₄	=	-0.183
e ₃₂₅	=	0.11045
e ₃₂₆	=	0.182888
e ₃₂₇	=	-1.32547
e ₃₂₈	=	-1.64784
e ₃₂₉	=	1.6483
e ₃₃₀	=	0
e ₃₃₁	=	-0.183
e ₃₃₂	=	0
e ₃₃₃	=	0.182888
e ₃₃₄	=	0
e ₃₃₅	=	-1.64784
e ₃₃₆	=	0

GRID A&D

Note: All values are in radians.

e ₃₃₇	=	4.79098
e ₃₃₈	=	-1.3113
e ₃₃₉	=	-1.3113
e ₃₄₀	=	1.31148
e ₃₄₁	=	1.31148
e ₃₄₂	=	-4.7913
e ₃₄₃	=	1.78671
e ₃₄₄	=	0.23321
e ₃₄₅	=	0.23321
e ₃₄₆	=	-0.2334
e ₃₄₇	=	-0.2334
e ₃₄₈	=	-1.7857
e ₃₄₉	=	2.4227
e ₃₅₀	=	-0.149
e ₃₅₁	=	-0.149
e ₃₅₂	=	0.14976
e ₃₅₃	=	0.14976
e ₃₅₄	=	-2.4275
e ₃₅₅	=	2.2867
e ₃₅₆	=	-0.0563
e ₃₅₇	=	-0.0563
e ₃₅₈	=	0.05397
e ₃₅₉	=	0.05397
e ₃₆₀	=	-2.2624
e ₃₆₁	=	2.31488
e ₃₆₂	=	-0.0745
e ₃₆₃	=	-0.0745
e ₃₆₄	=	0.08051

e ₃₆₅	=	0.08051
e ₃₆₆	=	-2.4382
e ₃₆₇	=	2.64289
e ₃₆₈	=	-0.1038
e ₃₆₉	=	-0.1038
e ₃₇₀	=	0.10145
e ₃₇₁	=	0.10145
e ₃₇₂	=	-2.6195
e ₃₇₃	=	2.47215
e ₃₇₄	=	-0.075
e ₃₇₅	=	-0.075
e ₃₇₆	=	0.07566
e ₃₇₇	=	0.07566
e ₃₇₈	=	-2.4766
e ₃₇₉	=	3.06655
e ₃₈₀	=	-0.1414
e ₃₈₁	=	-0.1414
e ₃₈₂	=	0.14125
e ₃₈₃	=	0.14125
e ₃₈₄	=	-3.0657
e ₃₈₅	=	4.79098
e ₃₈₆	=	1.78671
e ₃₈₇	=	-1.3113
e ₃₈₈	=	0.23321
e ₃₈₉	=	1.31148
e ₃₉₀	=	-0.2334
e ₃₉₁	=	-4.7913
e ₃₉₂	=	-1.7857

e ₃₉₃	=	1.78671
e ₃₉₄	=	2.4227
e ₃₉₅	=	0.23321
e ₃₉₆	=	-0.149
e ₃₉₇	=	-0.2334
e ₃₉₈	=	0.14976
e ₃₉₉	=	-1.7857
e ₄₀₀	=	-2.4275
e ₄₀₁	=	2.4227
e ₄₀₂	=	2.2867
e ₄₀₃	=	-0.149
e ₄₀₄	=	-0.0563
e ₄₀₅	=	0.14976
e ₄₀₆	=	0.05397
e ₄₀₇	=	-2.4275
e ₄₀₈	=	-2.2624
e ₄₀₉	=	2.2867
e ₄₁₀	=	2.31488
e ₄₁₁	=	-0.0563
e ₄₁₂	=	-0.0745
e ₄₁₃	=	0.05397
e ₄₁₄	=	0.08051
e ₄₁₅	=	-2.2624
e ₄₁₆	=	-2.4382
e ₄₁₇	=	2.31488
e ₄₁₈	=	2.64289
e ₄₁₉	=	-0.0745
e ₄₂₀	=	-0.1038

e ₄₂₁	=	0.08051
e ₄₂₂	=	0.10145
e ₄₂₃	=	-2.4382
e ₄₂₄	=	-2.6195
e ₄₂₅	=	2.64289
e ₄₂₆	=	2.47215
e ₄₂₇	=	-0.1038
e ₄₂₈	=	-0.075
e ₄₂₉	=	0.10145
e ₄₃₀	=	0.07566
e ₄₃₁	=	-2.6195
e ₄₃₂	=	-2.4766
e ₄₃₃	=	2.47215
e ₄₃₄	=	3.06655
e ₄₃₅	=	-0.075
e ₄₃₆	=	-0.1414
e ₄₃₇	=	0.07566
e ₄₃₈	=	0.14125
e ₄₃₉	=	-2.4766
e ₄₄₀	=	-3.0657
e ₄₄₁	=	3.06655
e ₄₄₂	=	0
e ₄₄₃	=	-0.1414
e ₄₄₄	=	0
e ₄₄₅	=	0.14125
e ₄₄₆	=	0
e ₄₄₇	=	-3.0657
e ₄₄₈	=	0

GRID B&C

Note: All values are in radians.

[F] MATRIX
ELEVATION 1

F ₁	=	313.8317
F ₂	=	112.5751
F ₃	=	-29.5605
F ₄	=	29.56052
F ₅	=	-112.575
F ₆	=	-313.832
F ₇	=	138.2622
F ₈	=	66.01122
F ₉	=	-2.07991
F ₁₀	=	2.079907
F ₁₁	=	-66.0112
F ₁₂	=	-138.262
F ₁₃	=	171.9963
F ₁₄	=	72.12039
F ₁₅	=	-9.25184
F ₁₆	=	9.251854
F ₁₇	=	-72.1204
F ₁₈	=	-171.996
F ₁₉	=	163.6659
F ₂₀	=	70.94083
F ₂₁	=	-7.26143
F ₂₂	=	7.261392
F ₂₃	=	-70.9408
F ₂₄	=	-163.666
F ₂₅	=	174.9395
F ₂₆	=	74.49594
F ₂₇	=	-8.64918
F ₂₈	=	8.649303

F ₂₉	=	-74.4963
F ₃₀	=	-174.94
F ₃₁	=	187.0738
F ₃₂	=	78.368
F ₃₃	=	-10.1126
F ₃₄	=	10.11258
F ₃₅	=	-78.368
F ₃₆	=	-187.074
F ₃₇	=	178.1501
F ₃₈	=	76.46119
F ₃₉	=	-8.40922
F ₄₀	=	8.40923
F ₄₁	=	-76.4612
F ₄₂	=	-178.15
F ₄₃	=	216.9207
F ₄₄	=	88.07819
F ₄₅	=	-13.5881
F ₄₆	=	13.58812
F ₄₇	=	-88.0782
F ₄₈	=	-216.921
F ₄₉	=	560.8028
F ₅₀	=	423.1321
F ₅₁	=	-82.9901
F ₅₂	=	-45.7257
F ₅₃	=	82.99012
F ₅₄	=	45.72567
F ₅₅	=	-560.803
F ₅₆	=	-423.132

F ₅₇	=	313.1963
F ₅₈	=	340.9312
F ₅₉	=	-18.1866
F ₆₀	=	-27.9119
F ₆₁	=	18.18658
F ₆₂	=	27.91193
F ₆₃	=	-313.196
F ₆₄	=	-340.931
F ₆₅	=	361.6684
F ₆₆	=	354.6707
F ₆₇	=	-34.9382
F ₆₈	=	-32.2391
F ₆₉	=	34.93818
F ₇₀	=	32.23908
F ₇₁	=	-361.668
F ₇₂	=	-354.671
F ₇₃	=	356.2577
F ₇₄	=	364.8423
F ₇₅	=	-31.4219
F ₇₆	=	-33.3038
F ₇₇	=	31.42195
F ₇₈	=	33.30392
F ₇₉	=	-356.258
F ₈₀	=	-364.843
F ₈₁	=	334.8155
F ₈₂	=	342.8825
F ₈₃	=	-32.5238
F ₈₄	=	-34.2602

F ₈₅	=	32.52393
F ₈₆	=	34.2602
F ₈₇	=	-334.816
F ₈₈	=	-342.883
F ₈₉	=	344.6448
F ₉₀	=	338.3401
F ₉₁	=	-33.9754
F ₉₂	=	-31.9543
F ₉₃	=	33.9754
F ₉₄	=	31.95432
F ₉₅	=	-344.645
F ₉₆	=	-338.34
F ₉₇	=	358.109
F ₉₈	=	384.1826
F ₉₉	=	-36.0781
F ₁₀₀	=	-42.223
F ₁₀₁	=	36.07811
F ₁₀₂	=	42.22299
F ₁₀₃	=	-358.109
F ₁₀₄	=	-384.183
F ₁₀₅	=	273.5042
F ₁₀₆	=	136.7521
F ₁₀₇	=	-32.2452
F ₁₀₈	=	-16.1226
F ₁₀₉	=	32.24524
F ₁₁₀	=	16.12262
F ₁₁₁	=	-273.504
F ₁₁₂	=	-136.752

GRID 1&4

Note: All values are in kip-in.

F ₁₁₃	=	608.7938
F ₁₁₄	=	262.6164
F ₁₁₅	=	-27.8537
F ₁₁₆	=	27.85366
F ₁₁₇	=	-262.616
F ₁₁₈	=	-608.794
F ₁₁₉	=	267.5622
F ₁₂₀	=	135.1546
F ₁₂₁	=	0.915654
F ₁₂₂	=	-0.91565
F ₁₂₃	=	-135.155
F ₁₂₄	=	-267.562
F ₁₂₅	=	332.2963
F ₁₂₆	=	154.7981
F ₁₂₇	=	-7.56668
F ₁₂₈	=	7.566678
F ₁₂₉	=	-154.798
F ₁₃₀	=	-332.296
F ₁₃₁	=	316.5259
F ₁₃₂	=	150.7456
F ₁₃₃	=	-5.01154
F ₁₃₄	=	5.01154
F ₁₃₅	=	-150.746
F ₁₃₆	=	-316.526
F ₁₃₇	=	338.4783
F ₁₃₈	=	159.6387
F ₁₃₉	=	-6.40031
F ₁₄₀	=	6.400306

F ₁₄₁	=	-159.639
F ₁₄₂	=	-338.478
F ₁₄₃	=	362.2248
F ₁₄₄	=	169.5378
F ₁₄₅	=	-7.71638
F ₁₄₆	=	7.716385
F ₁₄₇	=	-169.538
F ₁₄₈	=	-362.225
F ₁₄₉	=	344.9002
F ₁₅₀	=	163.6043
F ₁₅₁	=	-5.89725
F ₁₅₂	=	5.897247
F ₁₅₃	=	-163.604
F ₁₅₄	=	-344.9
F ₁₅₅	=	420.7455
F ₁₅₆	=	194.2324
F ₁₅₇	=	-10.7602
F ₁₅₈	=	10.76022
F ₁₅₉	=	-194.232
F ₁₆₀	=	-420.745
F ₁₆₁	=	1044.101
F ₁₆₂	=	793.2354
F ₁₆₃	=	-234.821
F ₁₆₄	=	-111.524
F ₁₆₅	=	234.8214
F ₁₆₆	=	111.5244
F ₁₆₇	=	-1044.1
F ₁₆₈	=	-793.235

F ₁₆₉	=	592.0115
F ₁₇₀	=	641.6532
F ₁₇₁	=	-24.5802
F ₁₇₂	=	-60.933
F ₁₇₃	=	24.58016
F ₁₇₄	=	60.93301
F ₁₇₅	=	-592.011
F ₁₇₆	=	-641.653
F ₁₇₇	=	678.8699
F ₁₇₈	=	666.4449
F ₁₇₉	=	-86.3353
F ₁₈₀	=	-75.3847
F ₁₈₁	=	86.33526
F ₁₈₂	=	75.38468
F ₁₈₃	=	-678.87
F ₁₈₄	=	-666.445
F ₁₈₅	=	669.8456
F ₁₈₆	=	685.6713
F ₁₈₇	=	-70.3859
F ₁₈₈	=	-76.3378
F ₁₈₉	=	70.38594
F ₁₉₀	=	76.3378
F ₁₉₁	=	-669.846
F ₁₉₂	=	-685.671
F ₁₉₃	=	628.6785
F ₁₉₄	=	643.5472
F ₁₉₅	=	-76.9387
F ₁₉₆	=	-81.874

F ₁₉₇	=	76.93874
F ₁₉₈	=	81.87403
F ₁₉₉	=	-628.679
F ₂₀₀	=	-643.547
F ₂₀₁	=	647.0586
F ₂₀₂	=	635.7014
F ₂₀₃	=	-79.9876
F ₂₀₄	=	-73.1658
F ₂₀₅	=	79.98756
F ₂₀₆	=	73.16579
F ₂₀₇	=	-647.059
F ₂₀₈	=	-635.701
F ₂₀₉	=	672.2253
F ₂₁₀	=	720.1064
F ₂₁₁	=	-84.5802
F ₂₁₂	=	-102.816
F ₂₁₃	=	84.58016
F ₂₁₄	=	102.8163
F ₂₁₅	=	-672.225
F ₂₁₆	=	-720.106
F ₂₁₇	=	511.9916
F ₂₁₈	=	255.9958
F ₂₁₉	=	-80.7016
F ₂₂₀	=	-40.3508
F ₂₂₁	=	80.70163
F ₂₂₂	=	40.35081
F ₂₂₃	=	-511.992
F ₂₂₄	=	-255.996

GRID 2&3

Note: All values are in kip-in.

ELEVATION 2

F ₂₂₅	=	312.559
F ₂₂₆	=	97.2961
F ₂₂₇	=	-39.3183
F ₂₂₈	=	39.3303
F ₂₂₉	=	-97.3003
F ₂₃₀	=	-312.579
F ₂₃₁	=	136.348
F ₂₃₂	=	68.8718
F ₂₃₃	=	0.45598
F ₂₃₄	=	-0.48388
F ₂₃₅	=	-68.8523
F ₂₃₆	=	-136.281
F ₂₃₇	=	171.427
F ₂₃₈	=	72.2093
F ₂₃₉	=	-8.96395
F ₂₄₀	=	9.08045
F ₂₄₁	=	-72.3165
F ₂₄₂	=	-171.758
F ₂₄₃	=	164.378
F ₂₄₄	=	71.9263
F ₂₄₅	=	-6.99404
F ₂₄₆	=	6.5372
F ₂₄₇	=	-71.3078
F ₂₄₈	=	-162.684
F ₂₄₉	=	165.813
F ₂₅₀	=	72.184
F ₂₅₁	=	-6.6864
F ₂₅₂	=	8.07224

F ₂₅₃	=	-75.9026
F ₂₅₄	=	-174.636
F ₂₅₅	=	188.366
F ₂₅₆	=	79.6767
F ₂₅₇	=	-9.82166
F ₂₅₈	=	9.36889
F ₂₅₉	=	-79.0873
F ₂₆₀	=	-186.734
F ₂₆₁	=	177.065
F ₂₆₂	=	77.0212
F ₂₆₃	=	-7.6372
F ₂₆₄	=	7.74855
F ₂₆₅	=	-77.119
F ₂₆₆	=	-177.372
F ₂₆₇	=	217.386
F ₂₆₈	=	89.5277
F ₂₆₉	=	-12.7847
F ₂₇₀	=	12.761
F ₂₇₁	=	-89.5113
F ₂₇₂	=	-217.329
F ₂₇₃	=	626.22
F ₂₇₄	=	465.125
F ₂₇₅	=	-116.615
F ₂₇₆	=	-57.2662
F ₂₇₇	=	116.613
F ₂₇₈	=	57.2445
F ₂₇₉	=	-626.199
F ₂₈₀	=	-465.029

F ₂₈₁	=	337.254
F ₂₈₂	=	370.478
F ₂₈₃	=	-12.0408
F ₂₈₄	=	-26.1636
F ₂₈₅	=	12.0709
F ₂₈₆	=	26.2656
F ₂₈₇	=	-337.416
F ₂₈₈	=	-370.972
F ₂₈₉	=	396.833
F ₂₉₀	=	389.964
F ₂₉₁	=	-37.063
F ₂₉₂	=	-33.8395
F ₂₉₃	=	36.9517
F ₂₉₄	=	33.4432
F ₂₉₅	=	-396.007
F ₂₉₆	=	-387.486
F ₂₉₇	=	384.393
F ₂₉₈	=	385.692
F ₂₉₉	=	-31.0734
F ₃₀₀	=	-31.5307
F ₃₀₁	=	31.3082
F ₃₀₂	=	32.6817
F ₃₀₃	=	-388.565
F ₃₀₄	=	-398.165
F ₃₀₅	=	354.981
F ₃₀₆	=	371.345
F ₃₀₇	=	-31.2817
F ₃₀₈	=	-34.5739

F ₃₀₉	=	32.2906
F ₃₁₀	=	34.7828
F ₃₁₁	=	-365.936
F ₃₁₂	=	-375.078
F ₃₁₃	=	379.031
F ₃₁₄	=	370.354
F ₃₁₅	=	-35.2604
F ₃₁₆	=	-32.6547
F ₃₁₇	=	34.9148
F ₃₁₈	=	32.5546
F ₃₁₉	=	-376.929
F ₃₂₀	=	-369.64
F ₃₂₁	=	391.319
F ₃₂₂	=	420.962
F ₃₂₃	=	-36.7086
F ₃₂₄	=	-43.3683
F ₃₂₅	=	36.7952
F ₃₂₆	=	43.3961
F ₃₂₇	=	-391.726
F ₃₂₈	=	-421.102
F ₃₂₉	=	300.403
F ₃₃₀	=	150.201
F ₃₃₁	=	-33.3519
F ₃₃₂	=	-16.676
F ₃₃₃	=	33.3313
F ₃₃₄	=	16.6657
F ₃₃₅	=	-300.319
F ₃₃₆	=	-150.159

GRID A&D

Note: All values are in kip-in.

F ₃₃₇	=	577.445
F ₃₃₈	=	151.397
F ₃₃₉	=	-91.536
F ₃₄₀	=	91.5853
F ₃₄₁	=	-151.39
F ₃₄₂	=	-577.48
F ₃₄₃	=	265.772
F ₃₄₄	=	157.309
F ₃₄₅	=	16.2664
F ₃₄₆	=	-16.314
F ₃₄₇	=	-157.27
F ₃₄₈	=	-265.65
F ₃₄₉	=	327.891
F ₃₅₀	=	148.336
F ₃₅₁	=	-10.357
F ₃₅₂	=	10.5056
F ₃₅₃	=	-148.57
F ₃₅₄	=	-328.51
F ₃₅₅	=	315.374
F ₃₅₆	=	151.788
F ₃₅₇	=	-4.097
F ₃₅₈	=	3.60411
F ₃₅₉	=	-150.42
F ₃₆₀	=	-312.15
F ₃₆₁	=	318.043
F ₃₆₂	=	151.223
F ₃₆₃	=	-4.777
F ₃₆₄	=	6.04321

F ₃₆₅	=	-158.99
F ₃₆₆	=	-334.84
F ₃₆₇	=	361.794
F ₃₆₈	=	170.023
F ₃₆₉	=	-7.4157
F ₃₇₀	=	6.91644
F ₃₇₁	=	-168.72
F ₃₇₂	=	-358.69
F ₃₇₃	=	339.968
F ₃₇₄	=	162.134
F ₃₇₅	=	-5.1847
F ₃₇₆	=	5.33114
F ₃₇₇	=	-162.35
F ₃₇₈	=	-340.55
F ₃₇₉	=	418.328
F ₃₈₀	=	194.353
F ₃₈₁	=	-9.8863
F ₃₈₂	=	9.85004
F ₃₈₃	=	-194.32
F ₃₈₄	=	-418.22
F ₃₈₅	=	1183.97
F ₃₈₆	=	871.092
F ₃₈₇	=	-786.43
F ₃₈₈	=	-278.08
F ₃₈₉	=	786.499
F ₃₉₀	=	278.001
F ₃₉₁	=	-1183.9
F ₃₉₂	=	-870.92

F ₃₉₃	=	624.453
F ₃₉₄	=	690.687
F ₃₉₅	=	104.459
F ₃₉₆	=	-21.358
F ₃₉₇	=	-104.37
F ₃₉₈	=	21.7521
F ₃₉₉	=	-624.75
F ₄₀₀	=	-691.59
F ₄₀₁	=	742.758
F ₄₀₂	=	728.594
F ₄₀₃	=	-116.66
F ₄₀₄	=	-86.138
F ₄₀₅	=	116.35
F ₄₀₆	=	84.823
F ₄₀₇	=	-741.23
F ₄₀₈	=	-724.04
F ₄₀₉	=	717.365
F ₄₁₀	=	720.3
F ₄₁₁	=	-61.589
F ₄₁₂	=	-67.559
F ₄₁₃	=	62.0303
F ₄₁₄	=	70.7645
F ₄₁₅	=	-725.15
F ₄₁₆	=	-743.45
F ₄₁₇	=	662.721
F ₄₁₈	=	692.61
F ₄₁₉	=	-72.795
F ₄₂₀	=	-81.253

F ₄₂₁	=	75.5911
F ₄₂₂	=	81.6207
F ₄₂₃	=	-683.05
F ₄₂₄	=	-699.57
F ₄₂₅	=	706.941
F ₄₂₆	=	691.382
F ₄₂₇	=	-81.395
F ₄₂₈	=	-73.08
F ₄₂₉	=	80.2232
F ₄₃₀	=	72.796
F ₄₃₁	=	-703.08
F ₄₃₂	=	-690.06
F ₄₃₃	=	729.989
F ₄₃₄	=	784.154
F ₄₃₅	=	-83.908
F ₄₃₆	=	-103.05
F ₄₃₇	=	84.2605
F ₄₃₈	=	103.152
F ₄₃₉	=	-730.73
F ₄₄₀	=	-784.41
F ₄₄₁	=	558.88
F ₄₄₂	=	279.44
F ₄₄₃	=	-81.462
F ₄₄₄	=	-40.731
F ₄₄₅	=	81.3624
F ₄₄₆	=	40.6812
F ₄₄₇	=	-558.73
F ₄₄₈	=	-279.36

GRID B&C

Note: All values are in kip-in.

**[F_o] MATRIX
ELEVATION 1**

F _{o1}	=	-874.8
F _{o2}	=	874.8
F _{o3}	=	-874.8
F _{o4}	=	874.8
F _{o5}	=	-874.8
F _{o6}	=	874.8
F _{o7}	=	-874.8
F _{o8}	=	874.8
F _{o9}	=	-874.8
F _{o10}	=	874.8
F _{o11}	=	-874.8
F _{o12}	=	874.8
F _{o13}	=	-874.8
F _{o14}	=	874.8
F _{o15}	=	-874.8
F _{o16}	=	874.8
F _{o17}	=	-874.8
F _{o18}	=	874.8
F _{o19}	=	-874.8
F _{o20}	=	874.8
F _{o21}	=	-874.8
F _{o22}	=	874.8
F _{o23}	=	-874.8
F _{o24}	=	874.8
F _{o25}	=	-874.8
F _{o26}	=	874.8
F _{o27}	=	-874.8
F _{o28}	=	874.8

F _{o29}	=	-874.8
F _{o30}	=	874.8
F _{o31}	=	-874.8
F _{o32}	=	874.8
F _{o33}	=	-874.8
F _{o34}	=	874.8
F _{o35}	=	-874.8
F _{o36}	=	874.8
F _{o37}	=	-874.8
F _{o38}	=	874.8
F _{o39}	=	-874.8
F _{o40}	=	874.8
F _{o41}	=	-874.8
F _{o42}	=	874.8
F _{o43}	=	-874.8
F _{o44}	=	874.8
F _{o45}	=	-874.8
F _{o46}	=	874.8
F _{o47}	=	-874.8
F _{o48}	=	874.8
F _{o49}	=	0
F _{o50}	=	0
F _{o51}	=	0
F _{o52}	=	0
F _{o53}	=	0
F _{o54}	=	0
F _{o55}	=	0
F _{o56}	=	0

F _{o57}	=	0
F _{o58}	=	0
F _{o59}	=	0
F _{o60}	=	0
F _{o61}	=	0
F _{o62}	=	0
F _{o63}	=	0
F _{o64}	=	0
F _{o65}	=	0
F _{o66}	=	0
F _{o67}	=	0
F _{o68}	=	0
F _{o69}	=	0
F _{o70}	=	0
F _{o71}	=	0
F _{o72}	=	0
F _{o73}	=	0
F _{o74}	=	0
F _{o75}	=	0
F _{o76}	=	0
F _{o77}	=	0
F _{o78}	=	0
F _{o79}	=	0
F _{o80}	=	0
F _{o81}	=	0
F _{o82}	=	0
F _{o83}	=	0
F _{o84}	=	0

F _{o85}	=	0
F _{o86}	=	0
F _{o87}	=	0
F _{o88}	=	0
F _{o89}	=	0
F _{o90}	=	0
F _{o91}	=	0
F _{o92}	=	0
F _{o93}	=	0
F _{o94}	=	0
F _{o95}	=	0
F _{o96}	=	0
F _{o97}	=	0
F _{o98}	=	0
F _{o99}	=	0
F _{o100}	=	0
F _{o101}	=	0
F _{o102}	=	0
F _{o103}	=	0
F _{o104}	=	0
F _{o105}	=	0
F _{o106}	=	0
F _{o107}	=	0
F _{o108}	=	0
F _{o109}	=	0
F _{o110}	=	0
F _{o111}	=	0
F _{o112}	=	0

GRID 1&4

Note: All values are in kip-in.

F _{o113}	=	-1653.2
F _{o114}	=	1653.204
F _{o115}	=	-1653.2
F _{o116}	=	1653.204
F _{o117}	=	-1653.2
F _{o118}	=	1653.204
F _{o119}	=	-1653.2
F _{o120}	=	1653.204
F _{o121}	=	-1653.2
F _{o122}	=	1653.204
F _{o123}	=	-1653.2
F _{o124}	=	1653.204
F _{o125}	=	-1653.2
F _{o126}	=	1653.204
F _{o127}	=	-1653.2
F _{o128}	=	1653.204
F _{o129}	=	-1653.2
F _{o130}	=	1653.204
F _{o131}	=	-1653.2
F _{o132}	=	1653.204
F _{o133}	=	-1653.2
F _{o134}	=	1653.204
F _{o135}	=	-1653.2
F _{o136}	=	1653.204
F _{o137}	=	-1653.2
F _{o138}	=	1653.204
F _{o139}	=	-1653.2
F _{o140}	=	1653.204

F _{o141}	=	-1653.2
F _{o142}	=	1653.204
F _{o143}	=	-1653.2
F _{o144}	=	1653.204
F _{o145}	=	-1653.2
F _{o146}	=	1653.204
F _{o147}	=	-1653.2
F _{o148}	=	1653.204
F _{o149}	=	-1653.2
F _{o150}	=	1653.204
F _{o151}	=	-1653.2
F _{o152}	=	1653.204
F _{o153}	=	-1653.2
F _{o154}	=	1653.204
F _{o155}	=	-1653.2
F _{o156}	=	1653.204
F _{o157}	=	-1653.2
F _{o158}	=	1653.204
F _{o159}	=	-1653.2
F _{o160}	=	1653.204
F _{o161}	=	0
F _{o162}	=	0
F _{o163}	=	0
F _{o164}	=	0
F _{o165}	=	0
F _{o166}	=	0
F _{o167}	=	0
F _{o168}	=	0

F _{o169}	=	0
F _{o170}	=	0
F _{o171}	=	0
F _{o172}	=	0
F _{o173}	=	0
F _{o174}	=	0
F _{o175}	=	0
F _{o176}	=	0
F _{o177}	=	0
F _{o178}	=	0
F _{o179}	=	0
F _{o180}	=	0
F _{o181}	=	0
F _{o182}	=	0
F _{o183}	=	0
F _{o184}	=	0
F _{o185}	=	0
F _{o186}	=	0
F _{o187}	=	0
F _{o188}	=	0
F _{o189}	=	0
F _{o190}	=	0
F _{o191}	=	0
F _{o192}	=	0
F _{o193}	=	0
F _{o194}	=	0
F _{o195}	=	0
F _{o196}	=	0

F _{o197}	=	0
F _{o198}	=	0
F _{o199}	=	0
F _{o200}	=	0
F _{o201}	=	0
F _{o202}	=	0
F _{o203}	=	0
F _{o204}	=	0
F _{o205}	=	0
F _{o206}	=	0
F _{o207}	=	0
F _{o208}	=	0
F _{o209}	=	0
F _{o210}	=	0
F _{o211}	=	0
F _{o212}	=	0
F _{o213}	=	0
F _{o214}	=	0
F _{o215}	=	0
F _{o216}	=	0
F _{o217}	=	0
F _{o218}	=	0
F _{o219}	=	0
F _{o220}	=	0
F _{o221}	=	0
F _{o222}	=	0
F _{o223}	=	0
F _{o224}	=	0

GRID 2&3

Note: All values are in kip-in.

ELEVATION 2

F _{o225}	=	-938.96
F _{o226}	=	938.964
F _{o227}	=	-938.96
F _{o228}	=	938.964
F _{o229}	=	-938.96
F _{o230}	=	938.964
F _{o231}	=	-938.96
F _{o232}	=	938.964
F _{o233}	=	-938.96
F _{o234}	=	938.964
F _{o235}	=	-938.96
F _{o236}	=	938.964
F _{o237}	=	-938.96
F _{o238}	=	938.964
F _{o239}	=	-938.96
F _{o240}	=	938.964
F _{o241}	=	-938.96
F _{o242}	=	938.964
F _{o243}	=	-938.96
F _{o244}	=	938.964
F _{o245}	=	-938.96
F _{o246}	=	938.964
F _{o247}	=	-938.96
F _{o248}	=	938.964
F _{o249}	=	-938.96
F _{o250}	=	938.964
F _{o251}	=	-938.96
F _{o252}	=	938.964

F _{o253}	=	-938.96
F _{o254}	=	938.964
F _{o255}	=	-938.96
F _{o256}	=	938.964
F _{o257}	=	-938.96
F _{o258}	=	938.964
F _{o259}	=	-938.96
F _{o260}	=	938.964
F _{o261}	=	-938.96
F _{o262}	=	938.964
F _{o263}	=	-938.96
F _{o264}	=	938.964
F _{o265}	=	-938.96
F _{o266}	=	938.964
F _{o267}	=	-938.96
F _{o268}	=	938.964
F _{o269}	=	-938.96
F _{o270}	=	938.964
F _{o271}	=	-938.96
F _{o272}	=	938.964
F _{o273}	=	0
F _{o274}	=	0
F _{o275}	=	0
F _{o276}	=	0
F _{o277}	=	0
F _{o278}	=	0
F _{o279}	=	0
F _{o280}	=	0

F _{o281}	=	0
F _{o282}	=	0
F _{o283}	=	0
F _{o284}	=	0
F _{o285}	=	0
F _{o286}	=	0
F _{o287}	=	0
F _{o288}	=	0
F _{o289}	=	0
F _{o290}	=	0
F _{o291}	=	0
F _{o292}	=	0
F _{o293}	=	0
F _{o294}	=	0
F _{o295}	=	0
F _{o296}	=	0
F _{o297}	=	0
F _{o298}	=	0
F _{o299}	=	0
F _{o300}	=	0
F _{o301}	=	0
F _{o302}	=	0
F _{o303}	=	0
F _{o304}	=	0
F _{o305}	=	0
F _{o306}	=	0
F _{o307}	=	0
F _{o308}	=	0

F _{o309}	=	0
F _{o310}	=	0
F _{o311}	=	0
F _{o312}	=	0
F _{o313}	=	0
F _{o314}	=	0
F _{o315}	=	0
F _{o316}	=	0
F _{o317}	=	0
F _{o318}	=	0
F _{o319}	=	0
F _{o320}	=	0
F _{o321}	=	0
F _{o322}	=	0
F _{o323}	=	0
F _{o324}	=	0
F _{o325}	=	0
F _{o326}	=	0
F _{o327}	=	0
F _{o328}	=	0
F _{o329}	=	0
F _{o330}	=	0
F _{o331}	=	0
F _{o332}	=	0
F _{o333}	=	0
F _{o334}	=	0
F _{o335}	=	0
F _{o336}	=	0

GRID A&D

Note: All values are in kip-in.

F _{o337}	=	-1761.76
F _{o338}	=	1761.76
F _{o339}	=	-1761.76
F _{o340}	=	1761.76
F _{o341}	=	-1761.76
F _{o342}	=	1761.76
F _{o343}	=	-1761.76
F _{o344}	=	1761.76
F _{o345}	=	-1761.76
F _{o346}	=	1761.76
F _{o347}	=	-1761.76
F _{o348}	=	1761.76
F _{o349}	=	-1761.76
F _{o350}	=	1761.76
F _{o351}	=	-1761.76
F _{o352}	=	1761.76
F _{o353}	=	-1761.76
F _{o354}	=	1761.76
F _{o355}	=	-1761.76
F _{o356}	=	1761.76
F _{o357}	=	-1761.76
F _{o358}	=	1761.76
F _{o359}	=	-1761.76
F _{o360}	=	1761.76
F _{o361}	=	-1761.76
F _{o362}	=	1761.76
F _{o363}	=	-1761.76
F _{o364}	=	1761.76

F _{o365}	=	-1761.76
F _{o366}	=	1761.76
F _{o367}	=	-1761.76
F _{o368}	=	1761.76
F _{o369}	=	-1761.76
F _{o370}	=	1761.76
F _{o371}	=	-1761.76
F _{o372}	=	1761.76
F _{o373}	=	-1761.76
F _{o374}	=	1761.76
F _{o375}	=	-1761.76
F _{o376}	=	1761.76
F _{o377}	=	-1761.76
F _{o378}	=	1761.76
F _{o379}	=	-1761.76
F _{o380}	=	1761.76
F _{o381}	=	-1761.76
F _{o382}	=	1761.76
F _{o383}	=	-1761.76
F _{o384}	=	1761.76
F _{o385}	=	0
F _{o386}	=	0
F _{o387}	=	0
F _{o388}	=	0
F _{o389}	=	0
F _{o390}	=	0
F _{o391}	=	0
F _{o392}	=	0

F _{o393}	=	0
F _{o394}	=	0
F _{o395}	=	0
F _{o396}	=	0
F _{o397}	=	0
F _{o398}	=	0
F _{o399}	=	0
F _{o400}	=	0
F _{o401}	=	0
F _{o402}	=	0
F _{o403}	=	0
F _{o404}	=	0
F _{o405}	=	0
F _{o406}	=	0
F _{o407}	=	0
F _{o408}	=	0
F _{o409}	=	0
F _{o410}	=	0
F _{o411}	=	0
F _{o412}	=	0
F _{o413}	=	0
F _{o414}	=	0
F _{o415}	=	0
F _{o416}	=	0
F _{o417}	=	0
F _{o418}	=	0
F _{o419}	=	0
F _{o420}	=	0

F _{o421}	=	0
F _{o422}	=	0
F _{o423}	=	0
F _{o424}	=	0
F _{o425}	=	0
F _{o426}	=	0
F _{o427}	=	0
F _{o428}	=	0
F _{o429}	=	0
F _{o430}	=	0
F _{o431}	=	0
F _{o432}	=	0
F _{o433}	=	0
F _{o434}	=	0
F _{o435}	=	0
F _{o436}	=	0
F _{o437}	=	0
F _{o438}	=	0
F _{o439}	=	0
F _{o440}	=	0
F _{o441}	=	0
F _{o442}	=	0
F _{o443}	=	0
F _{o444}	=	0
F _{o445}	=	0
F _{o446}	=	0
F _{o447}	=	0
F _{o448}	=	0

GRID B&C

Note: All values are in kip-in.

$[F^*]$ MATRIX
ELEVATION 1

F* ₁	=	-560.97
F* ₂	=	987.375
F* ₃	=	-904.36
F* ₄	=	904.361
F* ₅	=	-987.38
F* ₆	=	560.968
F* ₇	=	-736.54
F* ₈	=	940.811
F* ₉	=	-876.88
F* ₁₀	=	876.88
F* ₁₁	=	-940.81
F* ₁₂	=	736.538
F* ₁₃	=	-702.8
F* ₁₄	=	946.92
F* ₁₅	=	-884.05
F* ₁₆	=	884.052
F* ₁₇	=	-946.92
F* ₁₈	=	702.804
F* ₁₉	=	-711.13
F* ₂₀	=	945.741
F* ₂₁	=	-882.06
F* ₂₂	=	882.061
F* ₂₃	=	-945.74
F* ₂₄	=	711.134
F* ₂₅	=	-699.86
F* ₂₆	=	949.296
F* ₂₇	=	-883.45
F* ₂₈	=	883.449

F* ₂₉	=	-949.3
F* ₃₀	=	699.86
F* ₃₁	=	-687.73
F* ₃₂	=	953.168
F* ₃₃	=	-884.91
F* ₃₄	=	884.913
F* ₃₅	=	-953.17
F* ₃₆	=	687.726
F* ₃₇	=	-696.65
F* ₃₈	=	951.261
F* ₃₉	=	-883.21
F* ₄₀	=	883.209
F* ₄₁	=	-951.26
F* ₄₂	=	696.65
F* ₄₃	=	-657.88
F* ₄₄	=	962.878
F* ₄₅	=	-888.39
F* ₄₆	=	888.388
F* ₄₇	=	-962.88
F* ₄₈	=	657.879
F* ₄₉	=	560.803
F* ₅₀	=	423.132
F* ₅₁	=	-82.99
F* ₅₂	=	-45.726
F* ₅₃	=	82.9901
F* ₅₄	=	45.7257
F* ₅₅	=	-560.8
F* ₅₆	=	-423.13

F* ₅₇	=	313.196
F* ₅₈	=	340.931
F* ₅₉	=	-18.187
F* ₆₀	=	-27.912
F* ₆₁	=	18.1866
F* ₆₂	=	27.9119
F* ₆₃	=	-313.2
F* ₆₄	=	-340.93
F* ₆₅	=	361.668
F* ₆₆	=	354.671
F* ₆₇	=	-34.938
F* ₆₈	=	-32.239
F* ₆₉	=	34.9382
F* ₇₀	=	32.2391
F* ₇₁	=	-361.67
F* ₇₂	=	-354.67
F* ₇₃	=	356.258
F* ₇₄	=	364.842
F* ₇₅	=	-31.422
F* ₇₆	=	-33.304
F* ₇₇	=	31.4219
F* ₇₈	=	33.3039
F* ₇₉	=	-356.26
F* ₈₀	=	-364.84
F* ₈₁	=	334.816
F* ₈₂	=	342.882
F* ₈₃	=	-32.524
F* ₈₄	=	-34.26

F* ₈₅	=	32.5239
F* ₈₆	=	34.2602
F* ₈₇	=	-334.82
F* ₈₈	=	-342.88
F* ₈₉	=	344.645
F* ₉₀	=	338.34
F* ₉₁	=	-33.975
F* ₉₂	=	-31.954
F* ₉₃	=	33.9754
F* ₉₄	=	31.9543
F* ₉₅	=	-344.64
F* ₉₆	=	-338.34
F* ₉₇	=	358.109
F* ₉₈	=	384.183
F* ₉₉	=	-36.078
F* ₁₀₀	=	-42.223
F* ₁₀₁	=	36.0781
F* ₁₀₂	=	42.223
F* ₁₀₃	=	-358.11
F* ₁₀₄	=	-384.18
F* ₁₀₅	=	273.504
F* ₁₀₆	=	136.752
F* ₁₀₇	=	-32.245
F* ₁₀₈	=	-16.123
F* ₁₀₉	=	32.2452
F* ₁₁₀	=	16.1226
F* ₁₁₁	=	-273.5
F* ₁₁₂	=	-136.75

GRID 1&4

Note: All values are in kip-in.

F* ₁₁₃	=	-1044.41
F* ₁₁₄	=	1915.82
F* ₁₁₅	=	-1681.06
F* ₁₁₆	=	1681.058
F* ₁₁₇	=	-1915.82
F* ₁₁₈	=	1044.41
F* ₁₁₉	=	-1385.64
F* ₁₂₀	=	1788.359
F* ₁₂₁	=	-1652.29
F* ₁₂₂	=	1652.288
F* ₁₂₃	=	-1788.36
F* ₁₂₄	=	1385.642
F* ₁₂₅	=	-1320.91
F* ₁₂₆	=	1808.002
F* ₁₂₇	=	-1660.77
F* ₁₂₈	=	1660.771
F* ₁₂₉	=	-1808
F* ₁₃₀	=	1320.908
F* ₁₃₁	=	-1336.68
F* ₁₃₂	=	1803.95
F* ₁₃₃	=	-1658.22
F* ₁₃₄	=	1658.216
F* ₁₃₅	=	-1803.95
F* ₁₃₆	=	1336.678
F* ₁₃₇	=	-1314.73
F* ₁₃₈	=	1812.843
F* ₁₃₉	=	-1659.6
F* ₁₄₀	=	1659.604

F* ₁₄₁	=	-1812.84
F* ₁₄₂	=	1314.726
F* ₁₄₃	=	-1290.98
F* ₁₄₄	=	1822.742
F* ₁₄₅	=	-1660.92
F* ₁₄₆	=	1660.92
F* ₁₄₇	=	-1822.74
F* ₁₄₈	=	1290.979
F* ₁₄₉	=	-1308.3
F* ₁₅₀	=	1816.808
F* ₁₅₁	=	-1659.1
F* ₁₅₂	=	1659.101
F* ₁₅₃	=	-1816.81
F* ₁₅₄	=	1308.304
F* ₁₅₅	=	-1232.46
F* ₁₅₆	=	1847.436
F* ₁₅₇	=	-1663.96
F* ₁₅₈	=	1663.964
F* ₁₅₉	=	-1847.44
F* ₁₆₀	=	1232.459
F* ₁₆₁	=	1044.101
F* ₁₆₂	=	793.2354
F* ₁₆₃	=	-234.821
F* ₁₆₄	=	-111.524
F* ₁₆₅	=	234.8214
F* ₁₆₆	=	111.5244
F* ₁₆₇	=	-1044.1
F* ₁₆₈	=	-793.235

F* ₁₆₉	=	592.0115
F* ₁₇₀	=	641.6532
F* ₁₇₁	=	-24.5802
F* ₁₇₂	=	-60.933
F* ₁₇₃	=	24.58016
F* ₁₇₄	=	60.93301
F* ₁₇₅	=	-592.011
F* ₁₇₆	=	-641.653
F* ₁₇₇	=	678.8699
F* ₁₇₈	=	666.4449
F* ₁₇₉	=	-86.3353
F* ₁₈₀	=	-75.3847
F* ₁₈₁	=	86.33526
F* ₁₈₂	=	75.38468
F* ₁₈₃	=	-678.87
F* ₁₈₄	=	-666.445
F* ₁₈₅	=	669.8456
F* ₁₈₆	=	685.6713
F* ₁₈₇	=	-70.3859
F* ₁₈₈	=	-76.3378
F* ₁₈₉	=	70.38594
F* ₁₉₀	=	76.3378
F* ₁₉₁	=	-669.846
F* ₁₉₂	=	-685.671
F* ₁₉₃	=	628.6785
F* ₁₉₄	=	643.5472
F* ₁₉₅	=	-76.9387
F* ₁₉₆	=	-81.874

F* ₁₉₇	=	76.93874
F* ₁₉₈	=	81.87403
F* ₁₉₉	=	-628.679
F* ₂₀₀	=	-643.547
F* ₂₀₁	=	647.0586
F* ₂₀₂	=	635.7014
F* ₂₀₃	=	-79.9876
F* ₂₀₄	=	-73.1658
F* ₂₀₅	=	79.98756
F* ₂₀₆	=	73.16579
F* ₂₀₇	=	-647.059
F* ₂₀₈	=	-635.701
F* ₂₀₉	=	672.2253
F* ₂₁₀	=	720.1064
F* ₂₁₁	=	-84.5802
F* ₂₁₂	=	-102.816
F* ₂₁₃	=	84.58016
F* ₂₁₄	=	102.8163
F* ₂₁₅	=	-672.225
F* ₂₁₆	=	-720.106
F* ₂₁₇	=	511.9916
F* ₂₁₈	=	255.9958
F* ₂₁₉	=	-80.7016
F* ₂₂₀	=	-40.3508
F* ₂₂₁	=	80.70163
F* ₂₂₂	=	40.35081
F* ₂₂₃	=	-511.992
F* ₂₂₄	=	-255.996

GRID 2&3

Note: All values are in kip-in.

ELEVATION 2

F* ₂₂₅	=	-626.4
F* ₂₂₆	=	1036.3
F* ₂₂₇	=	-978.28
F* ₂₂₈	=	978.29
F* ₂₂₉	=	-1036.3
F* ₂₃₀	=	626.38
F* ₂₃₁	=	-802.62
F* ₂₃₂	=	1007.8
F* ₂₃₃	=	-938.51
F* ₂₃₄	=	938.48
F* ₂₃₅	=	-1007.8
F* ₂₃₆	=	802.68
F* ₂₃₇	=	-767.54
F* ₂₃₈	=	1011.2
F* ₂₃₉	=	-947.93
F* ₂₄₀	=	948.04
F* ₂₄₁	=	-1011.3
F* ₂₄₂	=	767.21
F* ₂₄₃	=	-774.59
F* ₂₄₄	=	1010.9
F* ₂₄₅	=	-945.96
F* ₂₄₆	=	945.5
F* ₂₄₇	=	-1010.3
F* ₂₄₈	=	776.28
F* ₂₄₉	=	-773.15
F* ₂₅₀	=	1011.1
F* ₂₅₁	=	-945.65
F* ₂₅₂	=	947.04

F* ₂₅₃	=	-1014.9
F* ₂₅₄	=	764.33
F* ₂₅₅	=	-750.6
F* ₂₅₆	=	1018.6
F* ₂₅₇	=	-948.79
F* ₂₅₈	=	948.33
F* ₂₅₉	=	-1018.1
F* ₂₆₀	=	752.23
F* ₂₆₁	=	-761.9
F* ₂₆₂	=	1016
F* ₂₆₃	=	-946.6
F* ₂₆₄	=	946.71
F* ₂₆₅	=	-1016.1
F* ₂₆₆	=	761.59
F* ₂₆₇	=	-721.58
F* ₂₆₈	=	1028.5
F* ₂₆₉	=	-951.75
F* ₂₇₀	=	951.73
F* ₂₇₁	=	-1028.5
F* ₂₇₂	=	721.63
F* ₂₇₃	=	626.22
F* ₂₇₄	=	465.12
F* ₂₇₅	=	-116.61
F* ₂₇₆	=	-57.266
F* ₂₇₇	=	116.61
F* ₂₇₈	=	57.244
F* ₂₇₉	=	-626.2
F* ₂₈₀	=	-465.03

F* ₂₈₁	=	337.25
F* ₂₈₂	=	370.48
F* ₂₈₃	=	-12.041
F* ₂₈₄	=	-26.164
F* ₂₈₅	=	12.071
F* ₂₈₆	=	26.266
F* ₂₈₇	=	-337.42
F* ₂₈₈	=	-370.97
F* ₂₈₉	=	396.83
F* ₂₉₀	=	389.96
F* ₂₉₁	=	-37.063
F* ₂₉₂	=	-33.84
F* ₂₉₃	=	36.952
F* ₂₉₄	=	33.443
F* ₂₉₅	=	-396.01
F* ₂₉₆	=	-387.49
F* ₂₉₇	=	384.39
F* ₂₉₈	=	385.69
F* ₂₉₉	=	-31.073
F* ₃₀₀	=	-31.531
F* ₃₀₁	=	31.308
F* ₃₀₂	=	32.682
F* ₃₀₃	=	-388.56
F* ₃₀₄	=	-398.17
F* ₃₀₅	=	354.98
F* ₃₀₆	=	371.34
F* ₃₀₇	=	-31.282
F* ₃₀₈	=	-34.574

F* ₃₀₉	=	32.291
F* ₃₁₀	=	34.783
F* ₃₁₁	=	-365.94
F* ₃₁₂	=	-375.08
F* ₃₁₃	=	379.03
F* ₃₁₄	=	370.35
F* ₃₁₅	=	-35.26
F* ₃₁₆	=	-32.655
F* ₃₁₇	=	34.915
F* ₃₁₈	=	32.555
F* ₃₁₉	=	-376.93
F* ₃₂₀	=	-369.64
F* ₃₂₁	=	391.32
F* ₃₂₂	=	420.96
F* ₃₂₃	=	-36.709
F* ₃₂₄	=	-43.368
F* ₃₂₅	=	36.795
F* ₃₂₆	=	43.396
F* ₃₂₇	=	-391.73
F* ₃₂₈	=	-421.1
F* ₃₂₉	=	300.4
F* ₃₃₀	=	150.2
F* ₃₃₁	=	-33.352
F* ₃₃₂	=	-16.676
F* ₃₃₃	=	33.331
F* ₃₃₄	=	16.666
F* ₃₃₅	=	-300.32
F* ₃₃₆	=	-150.16

GRID A&D

Note: All values are in kip-in.

F* ₃₃₇	=	-1184.3
F* ₃₃₈	=	1913.16
F* ₃₃₉	=	-1853.3
F* ₃₄₀	=	1853.35
F* ₃₄₁	=	-1913.2
F* ₃₄₂	=	1184.28
F* ₃₄₃	=	-1496
F* ₃₄₄	=	1919.07
F* ₃₄₅	=	-1745.5
F* ₃₄₆	=	1745.45
F* ₃₄₇	=	-1919
F* ₃₄₈	=	1496.11
F* ₃₄₉	=	-1433.9
F* ₃₅₀	=	1910.1
F* ₃₅₁	=	-1772.1
F* ₃₅₂	=	1772.27
F* ₃₅₃	=	-1910.3
F* ₃₅₄	=	1433.25
F* ₃₅₅	=	-1446.4
F* ₃₅₆	=	1913.55
F* ₃₅₇	=	-1765.9
F* ₃₅₈	=	1765.36
F* ₃₅₉	=	-1912.2
F* ₃₆₀	=	1449.61
F* ₃₆₁	=	-1443.7
F* ₃₆₂	=	1912.98
F* ₃₆₃	=	-1766.5
F* ₃₆₄	=	1767.8

F* ₃₆₅	=	-1920.7
F* ₃₆₆	=	1426.92
F* ₃₆₇	=	-1400
F* ₃₆₈	=	1931.78
F* ₃₆₉	=	-1769.2
F* ₃₇₀	=	1768.68
F* ₃₇₁	=	-1930.5
F* ₃₇₂	=	1403.07
F* ₃₇₃	=	-1421.8
F* ₃₇₄	=	1923.89
F* ₃₇₅	=	-1766.9
F* ₃₇₆	=	1767.09
F* ₃₇₇	=	-1924.1
F* ₃₇₈	=	1421.21
F* ₃₇₉	=	-1343.4
F* ₃₈₀	=	1956.11
F* ₃₈₁	=	-1771.6
F* ₃₈₂	=	1771.61
F* ₃₈₃	=	-1956.1
F* ₃₈₄	=	1343.54
F* ₃₈₅	=	1183.97
F* ₃₈₆	=	871.092
F* ₃₈₇	=	-786.43
F* ₃₈₈	=	-278.08
F* ₃₈₉	=	786.499
F* ₃₉₀	=	278.001
F* ₃₉₁	=	-1183.9
F* ₃₉₂	=	-870.92

F* ₃₉₃	=	624.453
F* ₃₉₄	=	690.687
F* ₃₉₅	=	104.459
F* ₃₉₆	=	-21.358
F* ₃₉₇	=	-104.37
F* ₃₉₈	=	21.7521
F* ₃₉₉	=	-624.75
F* ₄₀₀	=	-691.59
F* ₄₀₁	=	742.758
F* ₄₀₂	=	728.594
F* ₄₀₃	=	-116.66
F* ₄₀₄	=	-86.138
F* ₄₀₅	=	116.35
F* ₄₀₆	=	84.823
F* ₄₀₇	=	-741.23
F* ₄₀₈	=	-724.04
F* ₄₀₉	=	717.365
F* ₄₁₀	=	720.3
F* ₄₁₁	=	-61.589
F* ₄₁₂	=	-67.559
F* ₄₁₃	=	62.0303
F* ₄₁₄	=	70.7645
F* ₄₁₅	=	-725.15
F* ₄₁₆	=	-743.45
F* ₄₁₇	=	662.721
F* ₄₁₈	=	692.61
F* ₄₁₉	=	-72.795
F* ₄₂₀	=	-81.253

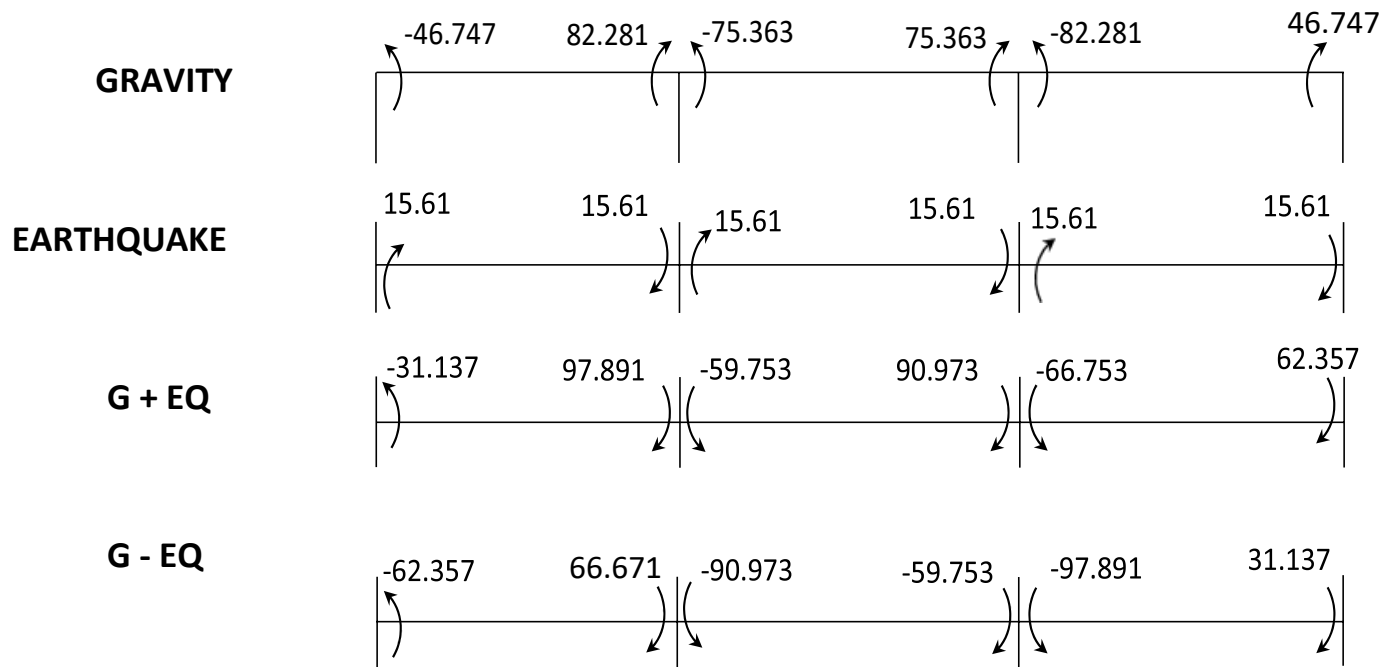
F* ₄₂₁	=	75.5911
F* ₄₂₂	=	81.6207
F* ₄₂₃	=	-683.05
F* ₄₂₄	=	-699.57
F* ₄₂₅	=	706.941
F* ₄₂₆	=	691.382
F* ₄₂₇	=	-81.395
F* ₄₂₈	=	-73.08
F* ₄₂₉	=	80.2232
F* ₄₃₀	=	72.796
F* ₄₃₁	=	-703.08
F* ₄₃₂	=	-690.06
F* ₄₃₃	=	729.989
F* ₄₃₄	=	784.154
F* ₄₃₅	=	-83.908
F* ₄₃₆	=	-103.05
F* ₄₃₇	=	84.2605
F* ₄₃₈	=	103.152
F* ₄₃₉	=	-730.73
F* ₄₄₀	=	-784.41
F* ₄₄₁	=	558.88
F* ₄₄₂	=	279.44
F* ₄₄₃	=	-81.462
F* ₄₄₄	=	-40.731
F* ₄₄₅	=	81.3624
F* ₄₄₆	=	40.6812
F* ₄₄₇	=	-558.73
F* ₄₄₈	=	-279.36

GRID B&C

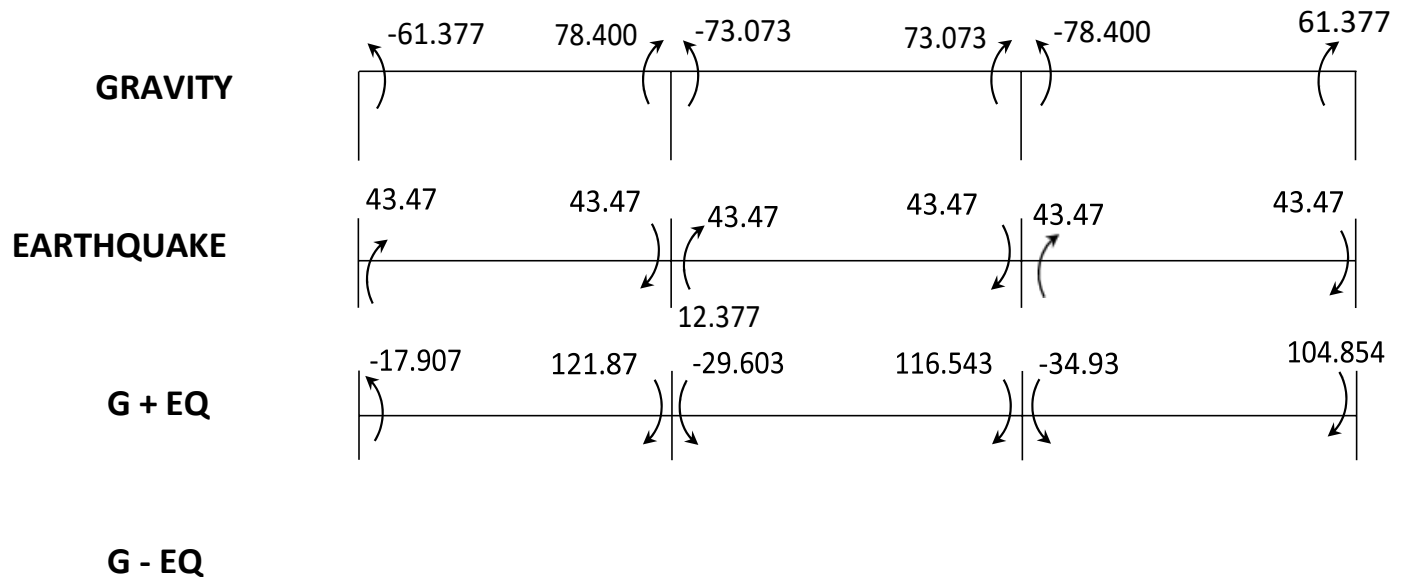
Note: All values are in kip-in.

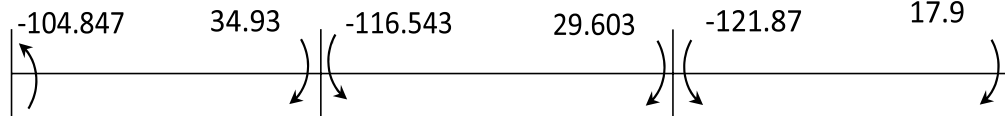
SUPERPOSITION

FRAME ON GRID 1 AND 4 (SUPERPOSITION)

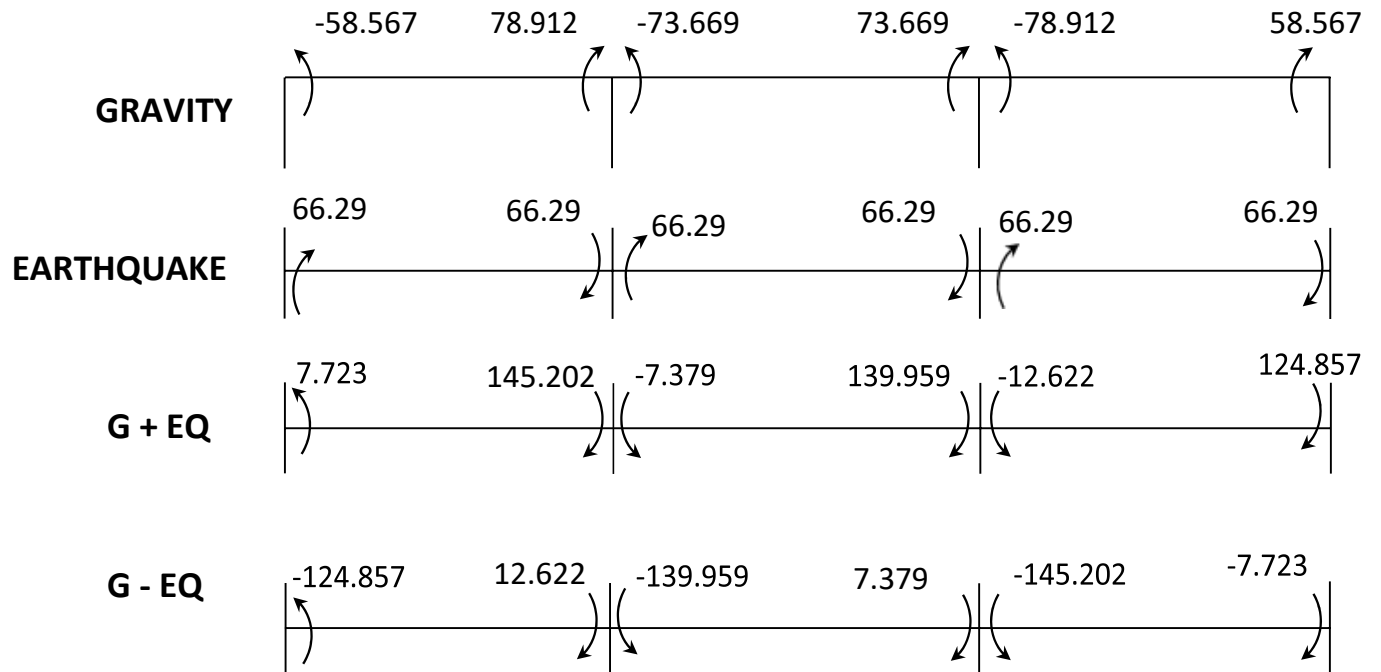


BEAM ON FLOOR 8

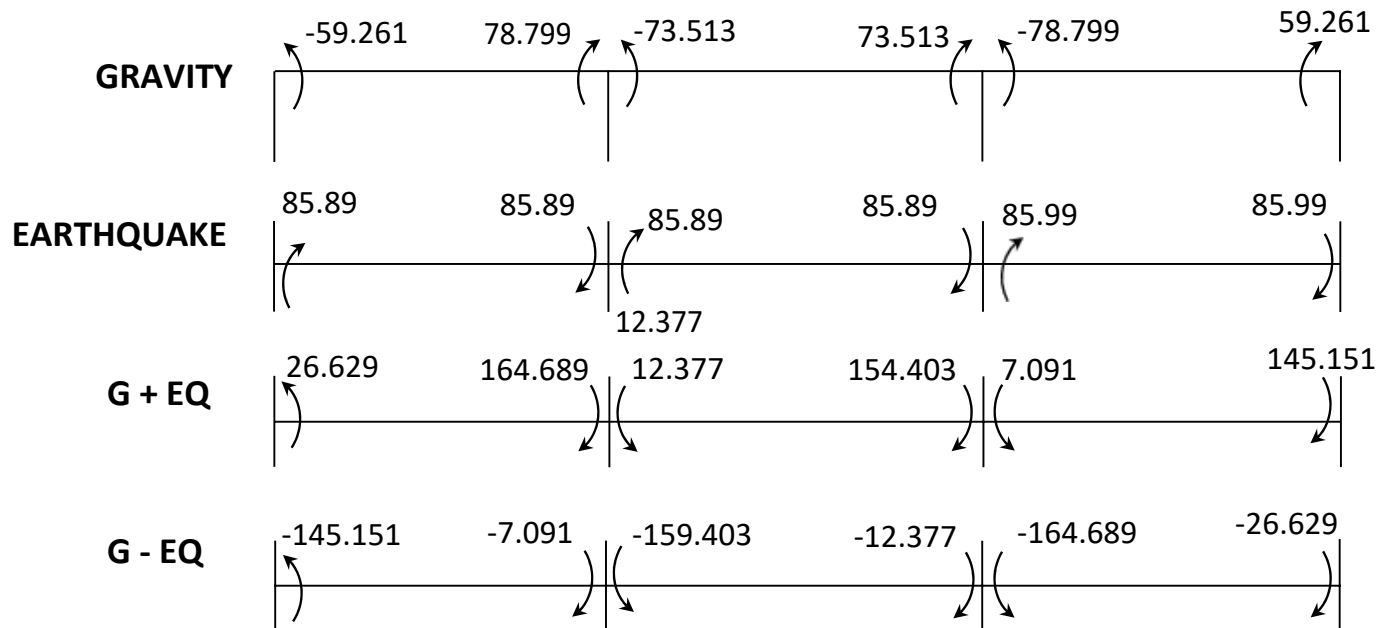




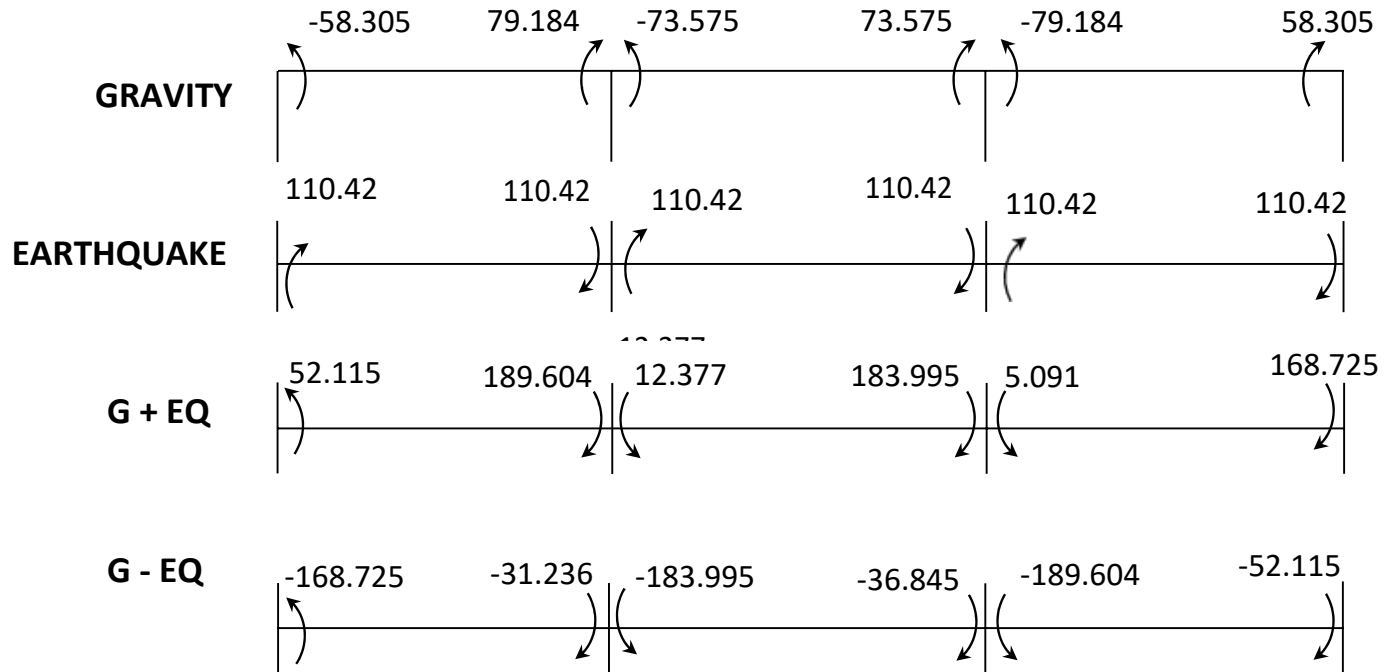
BEAM ON FLOOR 7



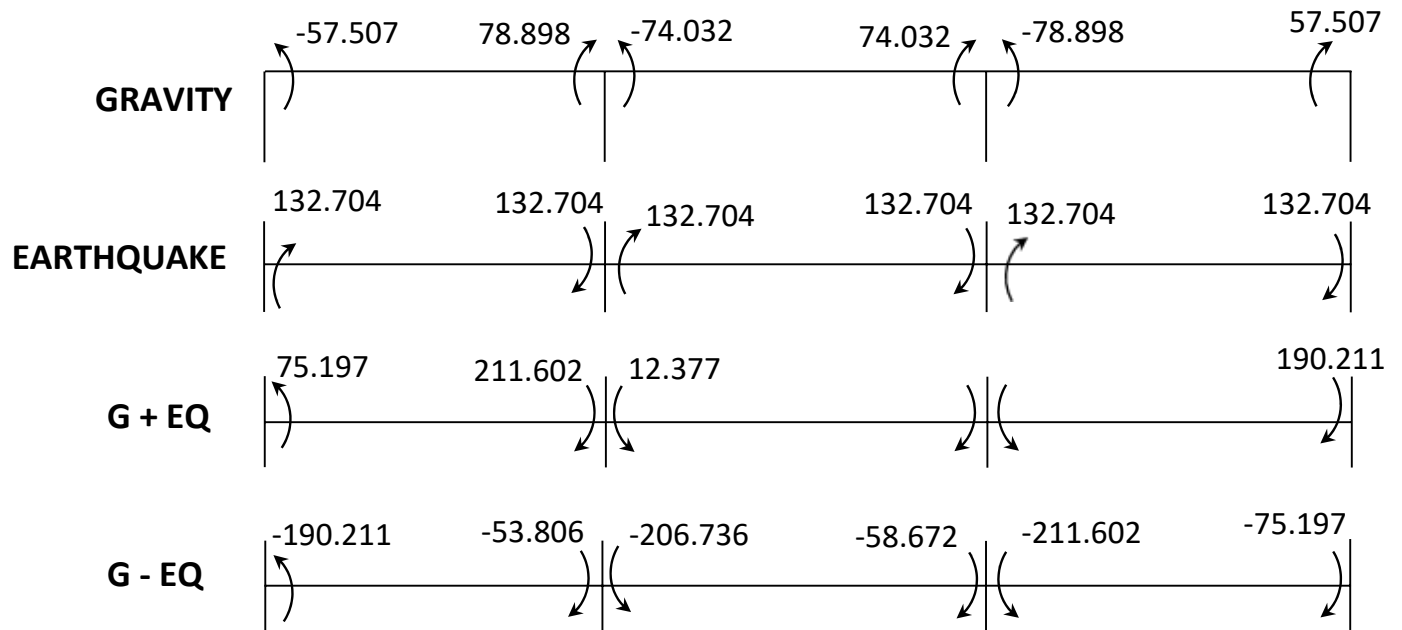
BEAM ON FLOOR 6



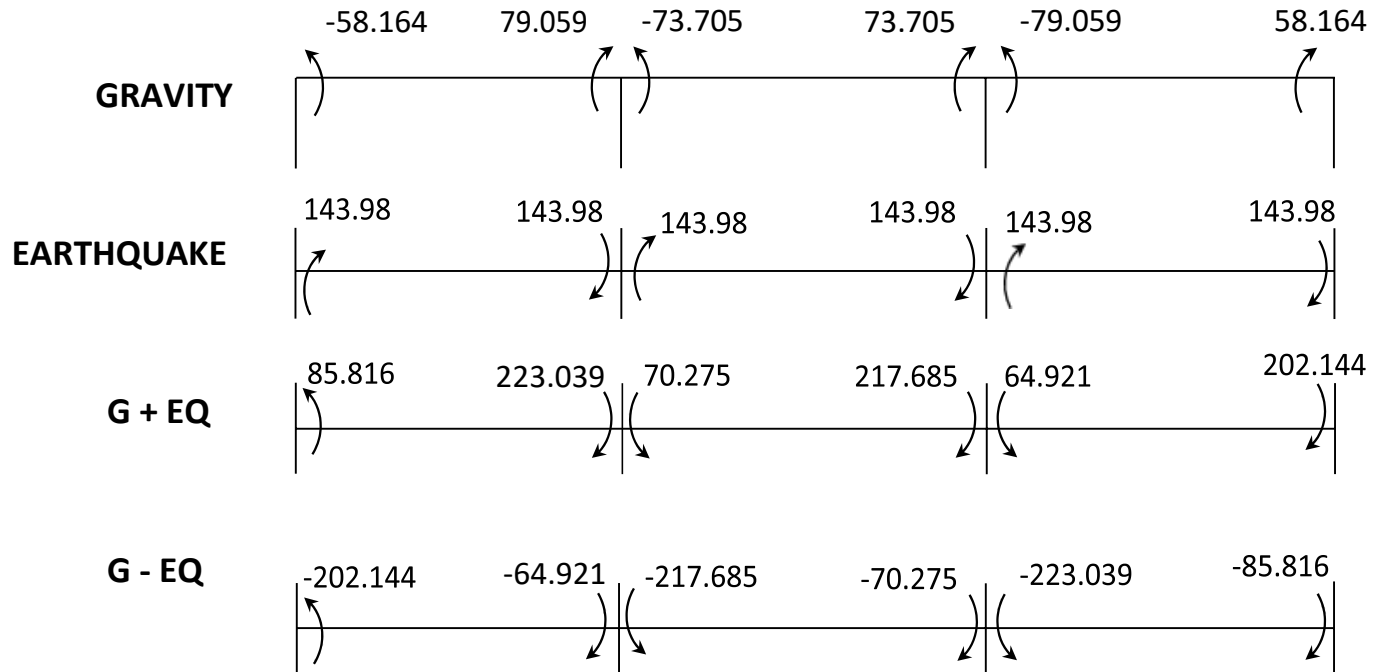
BEAM ON FLOOR 5



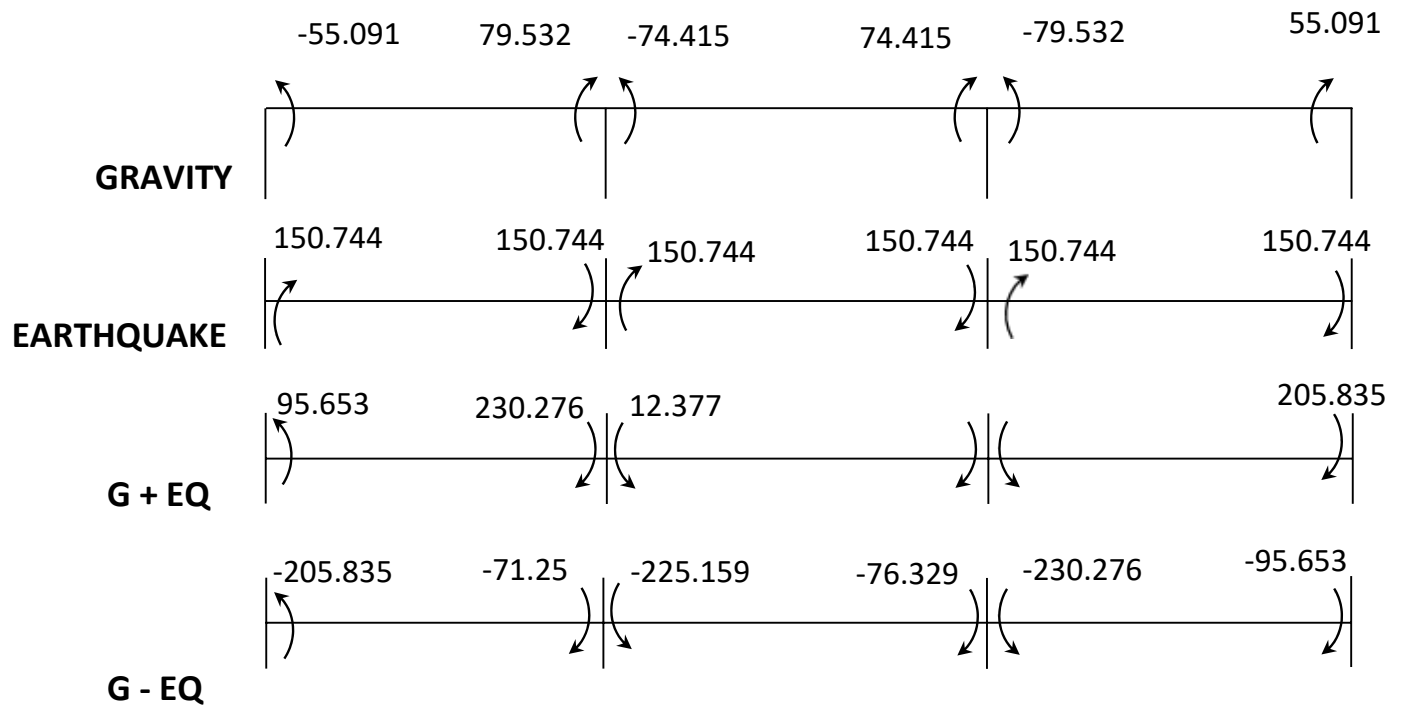
BEAM ON FLOOR 4



BEAM ON FLOOR 3



BEAM ON FLOOR 2



BEAM ON FLOOR 1

FINITE ELEMENT MODELLING

LOAD MATRIX

F1x	13.407
F1y	-21.87
M1	-874.8
F2x	0
F2y	-43.74
M2	0
F3x	0
F3y	-43.74
M3	0
F4x	0
F4y	-21.87
M4	874.8
F5x	10.47
F5y	-21.87
M5	-874.8
F6x	0
F6y	-43.74
M6	0
F7x	0
F7y	-43.74
M7	0
F8x	0
F8y	-21.87
M8	874.8
F9x	9.09
F9y	-21.87
M9	-874.8
F10x	0
F10y	-43.74
M10	0
F11x	0
F11y	-43.74

M11	0
F12x	0
F12y	-21.87
M12	874.8
F13x	7.7
F13y	-21.87
M13	-874.8
F14x	0
F14y	-43.74
M14	0
F15x	0
F15y	-43.74
M15	0
F16x	0
F16y	-21.87
M16	874.8
F17x	6.561
F17y	-21.87
M17	-874.8
F18x	0
F18y	-43.74
M18	0
F19x	0
F19y	-43.74
M19	0
F20x	0
F20y	-21.87
M20	874.8
F21x	5.08
F21y	-21.87
M21	-874.8
F22x	0

F22y	-43.74
M22	0
F23x	0
F23y	-43.74
M23	0
F24x	0
F24y	-21.87
M24	874.8
F25x	3.38
F25y	-21.87
M25	-874.8
F26x	0
F26y	-43.74
M26	0
F27x	0
F27y	-43.74
M27	0
F28x	0
F28y	-21.87
M28	874.8
F29x	1.69
F29y	-21.87
M29	-874.8
F30x	0
F30y	-43.74
M30	0
F31x	0
F31y	-43.74
M31	0
F32x	0
F32y	-21.87
M32	874.8

GRID 1&4

Note: All 'F' values are in kip and 'M' values are in kip-in.

F1x	27.97
F1y	-41.332
M1	-1653.28
F2x	0
F2y	-82.664
M2	0
F3x	0
F3y	-82.664
M3	0
F4x	0
F4y	-41.332
M4	1653.28
F5x	21.86
F5y	-41.332
M5	-1653.28
F6x	0
F6y	-82.664
M6	0
F7x	0
F7y	-82.664
M7	0
F8x	0
F8y	-41.332
M8	1653.28
F9x	18.97
F9y	-41.332
M9	-1653.28
F10x	0
F10y	-82.664
M10	0
F11x	0
F11y	-82.664

M11	0
F12x	0
F12y	-41.332
M12	1653.28
F13x	16.088
F13y	-41.332
M13	-1653.28
F14x	0
F14y	-82.664
M14	0
F15x	0
F15y	-82.664
M15	0
F16x	0
F16y	-41.332
M16	1653.28
F17x	13.689
F17y	-41.332
M17	-1653.28
F18x	0
F18y	-82.664
M18	0
F19x	0
F19y	-82.664
M19	0
F20x	0
F20y	-41.332
M20	1653.28
F21x	10.59
F21y	-41.332
M21	-1653.28
F22x	0

F22y	-82.664
M22	0
F23x	0
F23y	-82.664
M23	0
F24x	0
F24y	-41.332
M24	1653.28
F25x	7.06
F25y	-41.332
M25	-1653.28
F26x	0
F26y	-82.664
M26	0
F27x	0
F27y	-82.664
M27	0
F28x	0
F28y	-41.332
M28	1653.28
F29x	3.53
F29y	-41.332
M29	-1653.28
F30x	0
F30y	-82.664
M30	0
F31x	0
F31y	-82.664
M31	0
F32x	0
F32y	-41.332
M32	1653.28

GRID 2&3

Note: All 'F' values are in kip and 'M' values are in kip-in.

F1x	13.407
F1y	-21.34
M1	-938.96
F2x	0
F2y	-42.68
M2	0
F3x	0
F3y	-42.68
M3	0
F4x	0
F4y	-21.34
M4	938.96
F5x	10.47
F5y	-21.34
M5	-938.96
F6x	0
F6y	-42.68
M6	0
F7x	0
F7y	-42.68
M7	0
F8x	0
F8y	-21.34
M8	938.96
F9x	9.09
F9y	-21.34
M9	-938.96
F10x	0
F10y	-42.68
M10	0
F11x	0
F11y	-42.68

M11	0
F12x	0
F12y	-21.34
M12	938.96
F13x	7.7
F13y	-21.34
M13	-938.96
F14x	0
F14y	-42.68
M14	0
F15x	0
F15y	-42.68
M15	0
F16x	0
F16y	-21.34
M16	938.96
F17x	6.561
F17y	-21.34
M17	-938.96
F18x	0
F18y	-42.68
M18	0
F19x	0
F19y	-42.68
M19	0
F20x	0
F20y	-21.34
M20	938.96
F21x	5.08
F21y	-21.34
M21	-938.96
F22x	0

F22y	-42.68
M22	0
F23x	0
F23y	-42.68
M23	0
F24x	0
F24y	-21.34
M24	938.96
F25x	3.38
F25y	-21.34
M25	-938.96
F26x	0
F26y	-42.68
M26	0
F27x	0
F27y	-42.68
M27	0
F28x	0
F28y	-21.34
M28	938.96
F29x	1.69
F29y	-21.34
M29	-938.96
F30x	0
F30y	-42.68
M30	0
F31x	0
F31y	-42.68
M31	0
F32x	0
F32y	-21.34
M32	938.96

GRID A&D

Note: All 'F' values are in kip and 'M' values are in kip-in.

F1x	27.97
F1y	-40.04
M1	-1761.72
F2x	0
F2y	-80.08
M2	0
F3x	0
F3y	-80.08
M3	0
F4x	0
F4y	-40.04
M4	1761.72
F5x	21.86
F5y	-40.04
M5	-1761.72
F6x	0
F6y	-80.08
M6	0
F7x	0
F7y	-80.08
M7	0
F8x	0
F8y	-40.04
M8	1761.72
F9x	18.97
F9y	-40.04
M9	-1761.72
F10x	0
F10y	-80.08
M10	0
F11x	0
F11y	-80.08

M11	0
F12x	0
F12y	-40.04
M12	1761.72
F13x	16.088
F13y	-40.04
M13	-1761.72
F14x	0
F14y	-80.08
M14	0
F15x	0
F15y	-80.08
M15	0
F16x	0
F16y	-40.04
M16	1761.72
F17x	13.689
F17y	-40.04
M17	-1761.72
F18x	0
F18y	-80.08
M18	0
F19x	0
F19y	-80.08
M19	0
F20x	0
F20y	-40.04
M20	1761.72
F21x	10.59
F21y	-40.04
M21	-1761.72
F22x	0

F22y	-80.08
M22	0
F23x	0
F23y	-80.08
M23	0
F24x	0
F24y	-40.04
M24	1761.72
F25x	7.06
F25y	-40.04
M25	-1761.72
F26x	0
F26y	-80.08
M26	0
F27x	0
F27y	-80.08
M27	0
F28x	0
F28y	-40.04
M28	1761.72
F29x	3.53
F29y	-40.04
M29	-1761.72
F30x	0
F30y	-80.08
M30	0
F31x	0
F31y	-80.08
M31	0
F32x	0
F32y	-40.04
M32	1761.72

GRID B&C

Note: All 'F' values are in kip and 'M' values are in kip-in.

DISPLACEMENT MATRIX

d1x	2.55580345
d1y	-0.090748312
φ1	-0.001145881
d2x	2.55052029
d2y	-0.243499063
φ2	-0.000307817
d3x	2.546076335
d3y	-0.242953435
φ3	-6.24532E-05
d4x	2.54335797
d4y	-0.172541151
φ4	0.000420574
d5x	2.446478491
d5y	-0.087778377
φ5	-0.000996537
d6x	2.444672981
d6y	-0.237396348
φ6	-0.000501019
d7x	2.443684912
d7y	-0.236519973
φ7	-0.000228631
d8x	2.443564058
d8y	-0.169173183
φ8	-0.000146919
d9x	2.278195429
d9y	-0.081906528
φ9	-0.00125685
d10x	2.276154726
d10y	-0.225474961
φ10	-0.000614354
d11x	2.274950112
d11y	-0.223989412

φ11	-0.000385947
d12x	2.274458414
d12y	-0.16174882
φ12	-0.000339576
d13x	2.052429957
d13y	-0.073545029
φ13	-0.001422247
d14x	2.050714475
d14y	-0.207590696
φ14	-0.000729091
d15x	2.049742262
d15y	-0.205392566
φ15	-0.000517587
d16x	2.049413325
d16y	-0.149969192
φ16	-0.000548472
d17x	1.77340523
d17y	-0.063043369
φ17	-0.001664749
d18x	1.772435426
d18y	-0.18363936
φ18	-0.000843725
d19x	1.772034175
d19y	-0.180759971
φ19	-0.000665055
d20x	1.771926464
d20y	-0.133558464
φ20	-0.000787008
d21x	1.34672618
d21y	-0.049112641
φ21	-0.001875808
d22x	1.3456614

d22y	-0.149098219
φ22	-0.000929022
d23x	1.345116225
d23y	-0.145754946
φ23	-0.000801502
d24x	1.344937588
d24y	-0.109150436
φ24	-0.001013964
d25x	0.873555927
d25y	-0.033777018
φ25	-0.001907044
d26x	0.872870361
d26y	-0.107127761
φ26	-0.000958032
d27x	0.872581589
d27y	-0.103960055
φ27	-0.000882724
d28x	0.872460136
d28y	-0.078789591
φ28	-0.001135348
d29x	0.381172883
d29y	-0.017350141
φ29	-0.001898854
d30x	0.38176968
d30y	-0.057535232
φ30	-0.000840991
d31x	0.382109085
d31y	-0.055373689
φ31	-0.000870808
d32x	0.38209825
d32y	-0.042356625
φ32	-0.001114936

GRID 1&4

Note: All 'd' values are in inches and 'φ' values are in radians.

d1x	3.640832
d1y	-0.14571
φ1	-0.00152
d2x	3.631405
d2y	-0.26117
φ2	-0.00047
d3x	3.625074
d3y	-0.284
φ3	-0.00057
d4x	3.621244
d4y	-0.3017
φ4	0.000496
d5x	3.473981
d5y	-0.14076
φ5	-0.00136
d6x	3.469485
d6y	-0.25438
φ6	-0.00093
d7x	3.466703
d7y	-0.2768
φ7	-0.00089
d8x	3.466395
d8y	-0.29583
φ8	-0.00028
d9x	3.220196
d9y	-0.13118
φ9	-0.00171
d10x	3.215699
d10y	-0.24106
φ10	-0.00127
d11x	3.21315
d11y	-0.26258

φ11	-0.00128
d12x	3.212281
d12y	-0.28302
φ12	-0.00052
d13x	2.881694
d13y	-0.11767
φ13	-0.00196
d14x	2.877987
d14y	-0.22123
φ14	-0.0016
d15x	2.875791
d15y	-0.24127
φ15	-0.0016
d16x	2.875049
d16y	-0.26268
φ16	-0.00081
d17x	2.463313
d17y	-0.10085
φ17	-0.00226
d18x	2.460449
d18y	-0.19489
φ18	-0.00197
d19x	2.459022
d19y	-0.21282
φ19	-0.00198
d20x	2.458957
d20y	-0.23423
φ20	-0.00106
d21x	1.847698
d21y	-0.07865
φ21	-0.00251
d22x	1.845294

d22y	-0.15736
φ22	-0.00229
d23x	1.843903
d23y	-0.17209
φ23	-0.00233
d24x	1.843428
d24y	-0.19174
φ24	-0.00128
d25x	1.166654
d25y	-0.05426
φ25	-0.00257
d26x	1.164985
d26y	-0.11241
φ26	-0.00242
d27x	1.164098
d27y	-0.12305
φ27	-0.00245
d28x	1.163733
d28y	-0.13862
φ28	-0.0014
d29x	0.474668
d29y	-0.02809
φ29	-0.00242
d30x	0.474132
d30y	-0.05999
φ30	-0.00223
d31x	0.474336
d31y	-0.0657
φ31	-0.00232
d32x	0.475492
d32y	-0.07457
φ32	-0.00111

GRID 2&3

Note: All 'd' values are in inches and 'φ' values are in radians.

d1x	2.64298
d1y	-0.08881
ϑ1	-0.00117
d1x	2.637113
d1y	-0.24509
ϑ2	-0.00028
d1x	2.63224
d1y	-0.2424
ϑ3	-8.5E-05
d1x	2.629171
d1y	-0.16426
ϑ4	0.000464
d1x	2.532248
d1y	-0.08596
ϑ5	-0.00101
d1x	2.530292
d1y	-0.23904
ϑ6	-0.0005
d1x	2.529218
d1y	-0.23612
ϑ7	-0.00026
d1x	2.529126
d1y	-0.16102
ϑ8	-0.00016
d1x	2.360027
d1y	-0.08033
ϑ9	-0.0013
d1x	2.357766
d1y	-0.22702
ϑ10	-0.00063
d1x	2.356431
d1y	-0.22369

ϑ11	-0.00043
d1x	2.355885
d1y	-0.15392
ϑ12	-0.00036
d1x	2.127096
d1y	-0.07228
ϑ13	-0.00148
d1x	2.125197
d1y	-0.20892
ϑ14	-0.00076
d1x	2.124117
d1y	-0.20514
ϑ15	-0.00058
d1x	2.123755
	-0.14268
ϑ16	-0.00059
d1x	1.83765
d1y	-0.06214
ϑ17	-0.00175
d1x	1.836572
d1y	-0.18464
ϑ18	-0.0009
d1x	1.836111
d1y	-0.18051
ϑ19	-0.00074
d1x	1.835999
d1y	-0.12707
ϑ20	-0.00084
d1x	1.395208
d1y	-0.04857
ϑ21	-0.00199
d1x	1.394022

d1y	-0.1497
ϑ22	-0.001
d1x	1.393406
d1y	-0.14551
ϑ23	-0.0009
d1x	1.393206
d1y	-0.10378
ϑ24	-0.00109
d1x	0.903251
d1y	-0.03353
ϑ25	-0.00203
d1x	0.902473
d1y	-0.10739
ϑ26	-0.00104
d1x	0.902129
d1y	-0.10374
ϑ27	-0.00099
d1x	0.901981
d1y	-0.07487
ϑ28	-0.00122
d1x	0.391056
d1y	-0.0173
ϑ29	-0.00204
d1x	0.391749
d1y	-0.05756
ϑ30	-0.00092
d1x	0.392135
d1y	-0.05523
ϑ31	-0.00097
d1x	0.392142
d1y	-0.04023
ϑ32	-0.00119

GRID A&D

Note: All 'd' values are in inches and 'ϑ' values are in radians.

d1x	3.81983082
d1y	-0.144146394
φ1	-0.001597147
d2x	3.809292339
d2y	-0.255266852
φ2	-0.000461792
d3x	3.802242376
d3y	-0.273597155
φ3	-0.000590537
d4x	3.797786262
d4y	-0.28795769
φ4	0.000590832
d5x	3.648795975
d5y	-0.139365258
φ5	-0.00141854
d6x	3.643918277
d6y	-0.248650646
φ6	-0.000967334
d7x	3.640866107
d7y	-0.266656036
φ7	-0.000929377
d8x	3.640607202
d8y	-0.28228626
φ8	-0.000283647
d9x	3.385916571
d9y	-0.130076844
φ9	-0.001814272
d10x	3.380961765
d10y	-0.23564693
φ10	-0.001341109
d11x	3.378157157
d11y	-0.252935084

φ11	-0.001364816
d12x	3.377179068
d12y	-0.269976241
φ12	-0.000547446
d13x	3.0319732
d13y	-0.116922059
φ13	-0.00209514
d14x	3.02789555
d14y	-0.216263386
φ14	-0.001707473
d15x	3.025467101
d15y	-0.232377307
φ15	-0.00171805
d16x	3.024639891
d16y	-0.250474389
φ16	-0.000866341
d17x	2.591724574
d17y	-0.100458861
φ17	-0.002435314
d18x	2.588584878
d18y	-0.190515412
φ18	-0.002112724
d19x	2.587015515
d19y	-0.204953616
φ19	-0.002138101
d20x	2.586967624
d20y	-0.223247085
φ20	-0.00115654
d21x	1.943480323
d21y	-0.078611801
φ21	-0.002726008
d22x	1.940825452

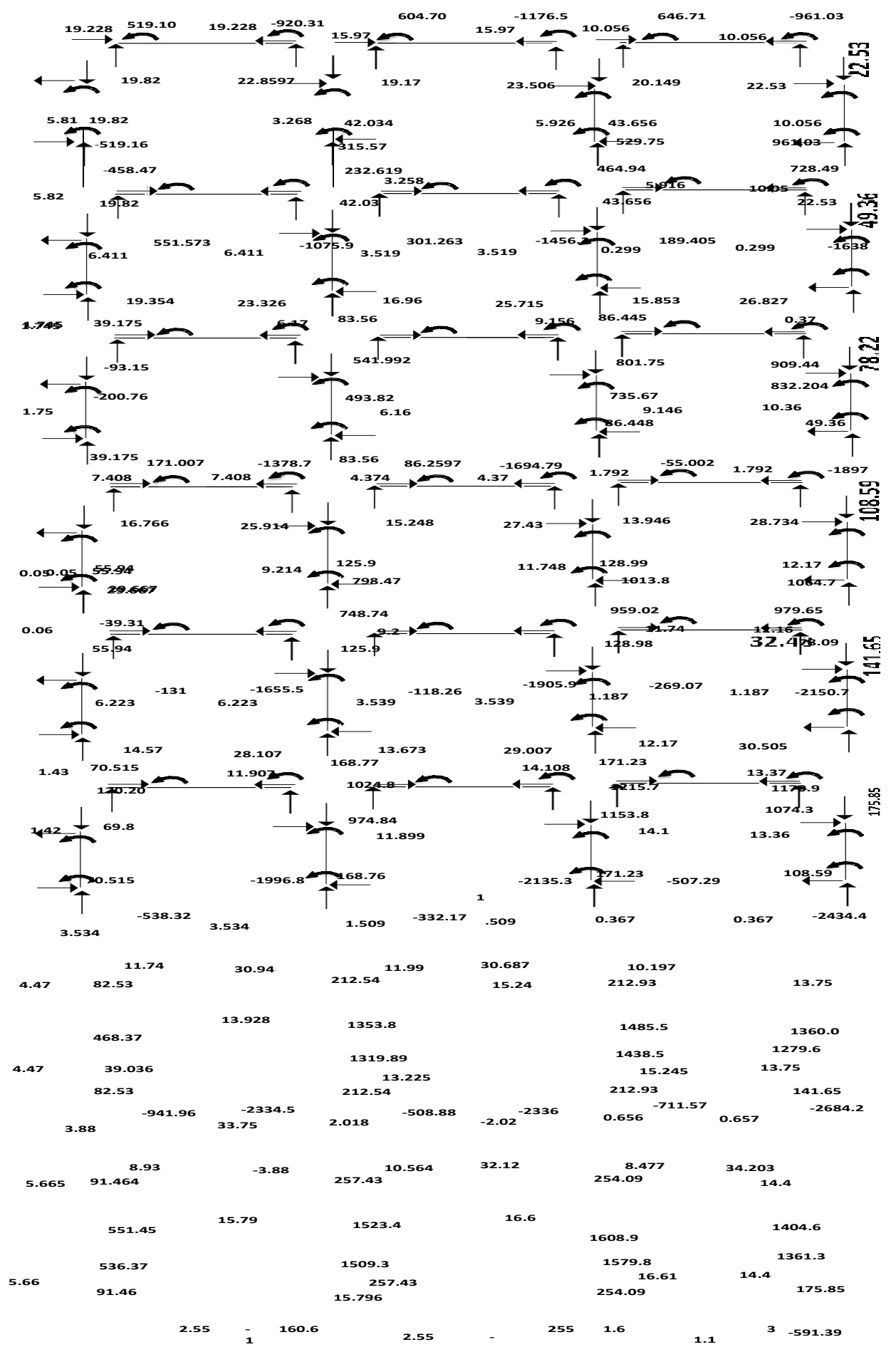
d22y	-0.153827008
φ22	-0.002476258
d23x	1.939279148
d23y	-0.165698741
φ23	-0.00252083
d24x	1.938751962
d24y	-0.182650189
φ24	-0.001401042
d25x	1.223962702
d25y	-0.054436796
φ25	-0.002809566
d26x	1.222095923
d26y	-0.10987596
φ26	-0.002628024
d27x	1.221094714
d27y	-0.118464077
φ27	-0.002666033
d28x	1.220681607
d28y	-0.131988049
φ28	-0.001547489
d29x	0.493375298
d29y	-0.028287511
φ29	-0.002657768
d30x	0.49282907
d30y	-0.058629575
φ30	-0.002411157
d31x	0.493100555
d31y	-0.063247441
φ31	-0.002504203
d32x	0.494457518
d32y	-0.070969006
φ32	-0.001222202

GRID B&C

Note: All 'd' values are in inches and 'φ' values are in radians.

FREE BODY DIAGRAM

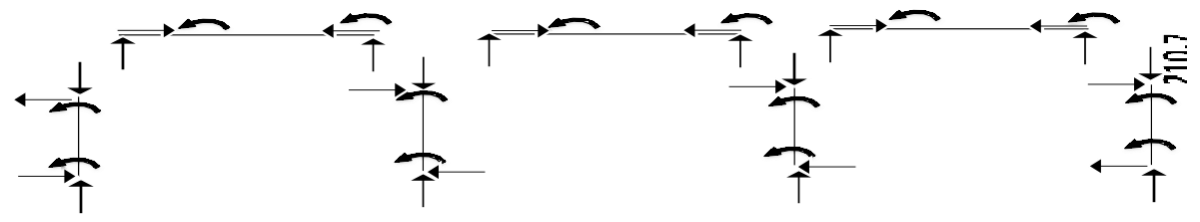
Note: All 'F' values are in kips and 'M' values are in kip-in.



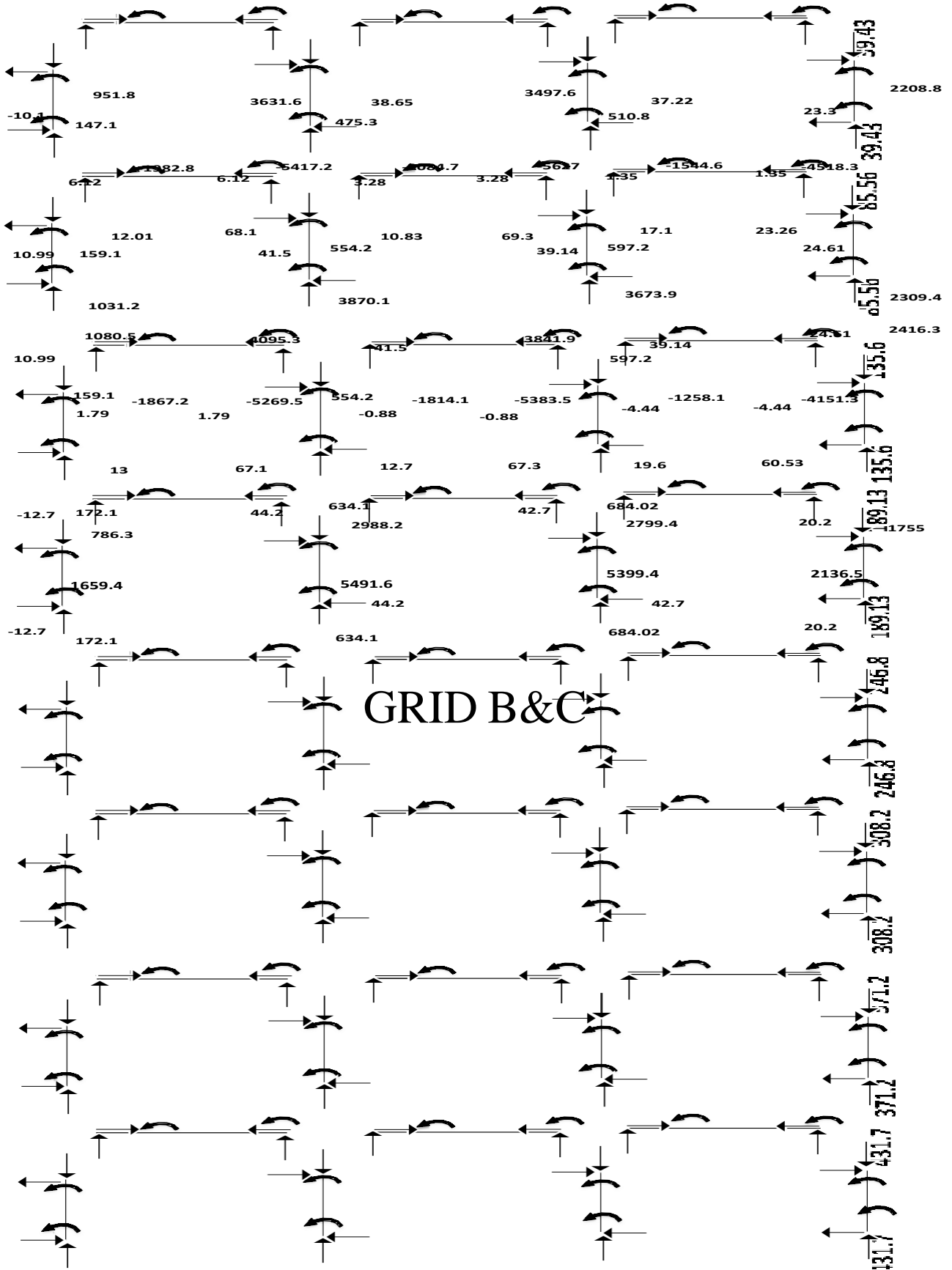
1.13

	-2441		-791.62	0.48		-	278	
		0					5.5	
		4						
		9						
	7.3		35.40		9.85		32.83	7.79
								34.88
-6.5	98.7		17.2		303.1		17.3	295.11
								14.9
	624.1				1633.5			1652.8
								1424.3
								1658.8
-6.5	622.9				1673.2			1658.8
								17.3
					17.2			14.9
	98.7				303.1			295.1
								210.7
	2.27		-1292.2		-2622.1		-456.24	1.26
								1.26
			2.27				-2356.3	-680.1
							0.023	0.023
								-2666.9
	6.51		36.17		10.68		31.99	8.66
								34.02
-10.5	105.3		16.2		350.2		16	335.98
								14.9
	669.1				1405.1			1377.5
								1232
								1695.2
	1338.3				1708			16
								14.9
-10.5					16.2			335.98
	105.3				350.2			244.8

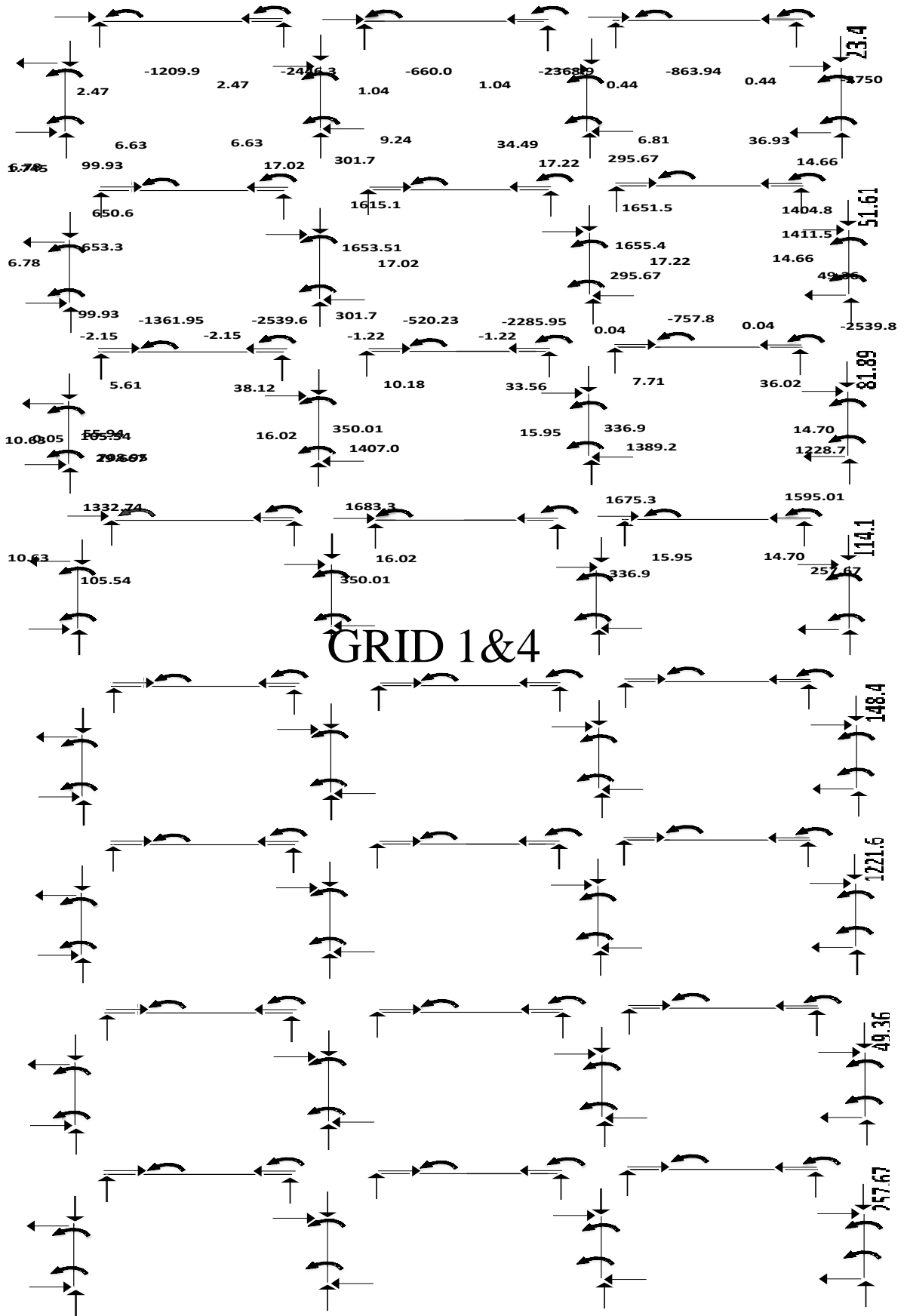
GRID A&D

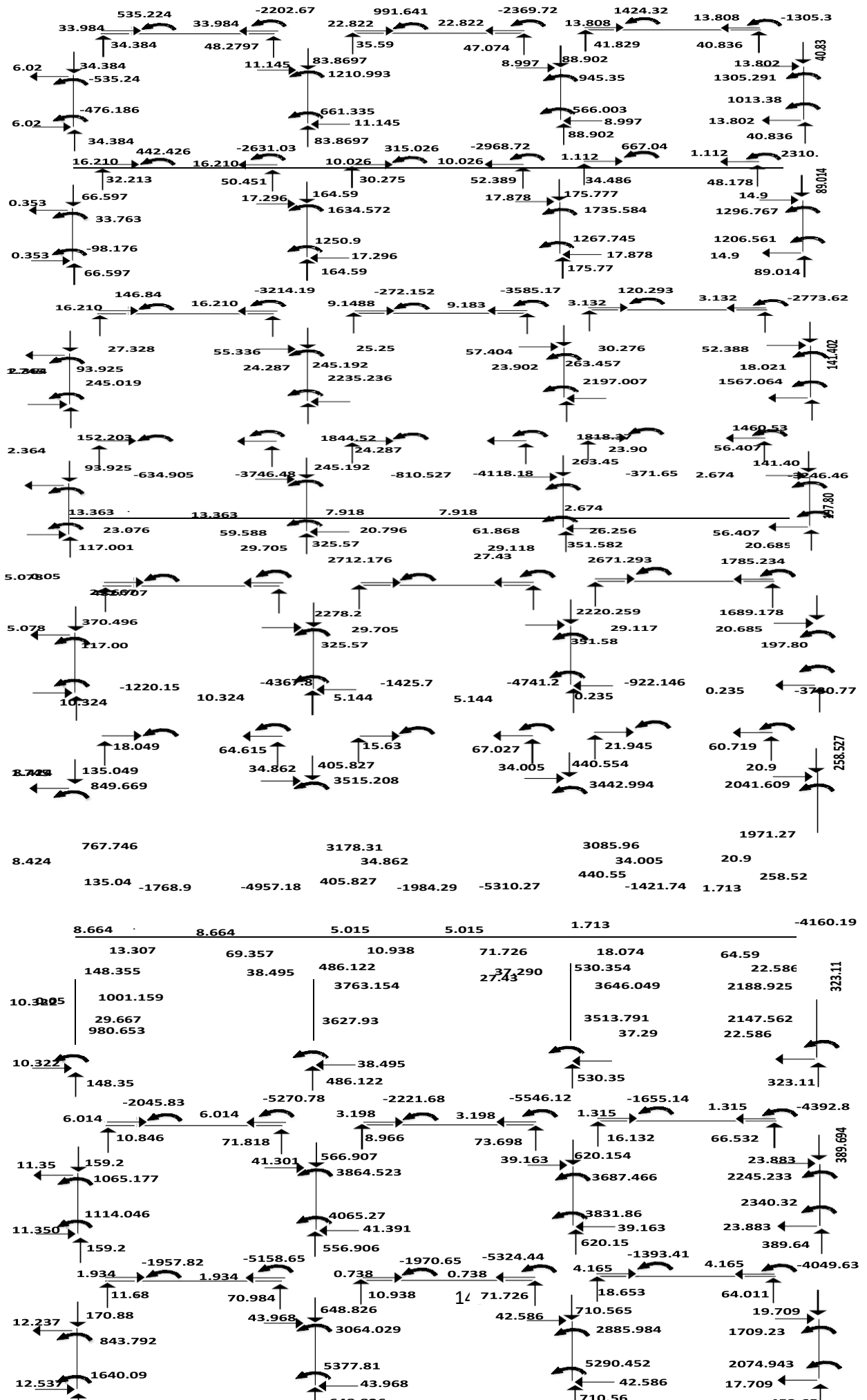


	34.5	585.2	34.5	-2380.1	1119.8	23.10	-2466.8	1551.8	-1390.7	
		33.24	46.84		34.94	45.14		40.65	39.43	
6.51	33.24		11.43	81.78		8.50	85.79		14.6	
		-585.4			1260.1			915.12		1390.6
		-518.1	660.5		11.43	513.1		8.50	14.6	1062.6
6.51							85.79			
	33.24	502.1	-2779.6	81.78	454.4	-3050.4	0.85	745.85	0.85	-2410.1
	15.99		15.99	10		10				
	31.34		48.7		30.21	49.8		33.93		46.15
0.69	64.56		17.42	160.73		17.66	169.6			
	15.86			1407.0			1389.2		15.45	1228.7
		-132.5	1241.2		17.42		1224.7	17.66		1248.5
0.69	64.56			160.73			169.6		15.45	
	16.24	-91.6	16.24	-3382.4	9.19	-131.2	9.19	-3666.3	3.21	245.9
									3.21	-2875.6
	26.88		53.2		25.66	54.42		30.08	50	
2.04	91.46		24.5	239.6		23.64	254.1		18.66	
		223.6			2272.6			2195.5		1626.9
	118.6		1837.5		24.5	1776.3		23.64	18.66	1507.4
2.04							254.1			
	91.46	-582.6	-3915.5	239.6	-671.6	-4200.3	0.85	-252.2	0.85	-3356.9
	15.99		15.99	10		10				
	31.34		48.7		30.21	49.8		33.93		46.15
4.76	114.5		29.87	318.24		28.89	338.96			
	463.82			2749.4			2675.9		21.37	1849.3
		336.32		2268.5	29.87		2177.2	28.89		1740.6
4.76	114.5			318.24			338.96		21.37	
		-1168.2	10.29	-4533.1	5.14	-1285.9	5.14	-4821.9	0.16	-806.7
									0.16	3847.7
	18.44		61.64		16.9	63.2		22.4	57.67	
8.16	132.9		35.02	396.8		33.88	424.5		21.53	
		831.8			3550.3			3450.5		2107.1
	736.3		3172.9		35.02	3053.6		33.88	21.53	2026.8
8.16							424.5			
	132.9	-1715.6	-5116.4	396.8	-1845.8	-5319.3	1.73	-1310.7	1.73	-4283.8
	8.70		8.70	5.06		5.06				
	14.2		65.92		12.62	67.45		18.85		61.24
-10.1	147.1		38.65	475.3		37.22	510.8			
	979.2			3789.2			3648.3		23.3	2256.9



	19.04	501.58	19.04	-794.84	504.44	-1112.5	9.79	558.6	9.79	-929.67
				16.02		16.02				
		20.64		23.09		19.34		24.40		20.32
										23.41
5.64	20.65		3.02	42.43		6.22	44.72		9.79	
	--501.61			290.4			553.72		929.6	
	-445.54			217.86			491.33		1062.6	
5.64	20.65			3.02			6.22		9.79	
				42.43			44.72		23.4	
	6.51	537.44	6.51	-944.21	203.4	3.56	-1398.96	0.43	92.86	0.43
				3.56						-1612.5
		20.17		23.56		16.88		26.85		15.53
1.67	40.82		5.97	82.88			9.34	87.12		28.20
										10.23
		-91.93				522.92		814.66		895.91
										823.5
1.67	-189.66			480.38			755.6		10.23	
				5.97			9.34		51.61	
							87.12			
	40.82	153.73		-1248.4	82.88	-8.36	-1634.46	1.73	-146.9	1.73
	7.34		7.34		4.34		4.31			-1871.4
		17.30		26.43		15.08		28.71		13.46
										30.48
0.09	0.05	55.94		8.98	124.34		11.91	129.3		12.02
		25.867			776.4			1025.7		1047.8
0.05	26.21				733.2			976.3		969.92
					8.98			11.91		12.02
	58.13				124.34			129.3		81.89
6.18	-151.55	6.18	-1526.3	3.50	-208.4	3.50	-1843.6	1.18	-356.2	1.18
										-2122.5
		14.87		28.86		13.32		30.42		11.54
1.57	73.01		11.66	166.5			14.23	171.25		32.19
	127.71			1001.4				1223.5		13.19
										1153
	86.66				217.869			1168.1		1063.5
1.57	73.01				11.66			14.23		13.19
					166.5			171.25		114.1
3.49	-566.72	3.49	-1879.4	1.44	-416.78	1.44	-2069.76	0.39	-589.08	0.39
										-2404.6
		11.70		32.03		11.5		32.3		9.39
1.67	84.7		13.7	210.1			18.3	212.75		34.34
										13.88
	480.13				1331.1			1491.1		1341.8
										1266.9
4.63	410.1				1303			1446.2		13.88
					13.7			18.3		
								212.75		148.4
	84.7	-980.41	3.84	-2218.1	210.1	-585.95	-2266.6	0.64	-787.8	0.64
	3.84				1.96		1.96			-2652.2
	8.54		35.19		9.98		33.75		7.54	7.54
5.87	0.05	23.24		15.6	255.4		16.62	254.25		14.66
		252.87			1501.7			1608.9		1386.2
5.87	559.6				1492.2			1582.2		1346.2
					15.6			16.62		14.66
	43.84				255.4			254.25		1221.6





0.05

29.667

27.43

453.65

GRID 2&3

APPENDIX D
CHARTS AND TABLES

Table 1:

Zone	1	2A	2B	3	4
Z	0.075	0.15	0.2	0.3	0.4

(From Table 16-I, UBC 1997.)

Table 2: Structural Systems^a

Basic structural system ^b	Lateral-force-resisting system description	R	Ω_o	Height limit for seismic zones 3 and 4
1. Bearing wall System	1. Shear walls			
	a. Concrete	4.5	2.8	160
	b. Masonry	4.5	2.8	160
	2. Braced frames where bracing carries gravity load			
	a. Steel	4.4	2.2	160
	b. Concrete ^e	2.8	2.2	N.P.
2. Building frame system	1. Steel eccentrically braced frame (EBF)	7.0	2.8	240
	2. Shear walls			
	a. Concrete	5.5	2.8	240
	b. Masonry	5.5	2.8	160
	3. Ordinary braced frames			
	a. Steel	5.6	2.2	160
	b. Concrete ^c	5.6	2.2	N.P.
	4. Special concentrically braced frames			
a. Steel	6.4	2.2	240	
3. Moment-resisting frame system	1. Special moment-resisting frame (SMRF)			
	a. Steel	8.5	2.8	N.L.
	b. Concrete ^d	8.5	2.8	N.L.
	2. Masonry moment-resisting wall frame (MMRWF)	6.5	2.8	160
	3. Concrete intermediate moment-resisting frame (IMRF) ^e	5.5	2.8	N.P.
	4. Ordinary moment-resisting frame (OMRF)			
	a. Steel ^f	4.5	2.8	160

	b. Concrete ^h	3.5	2.8	N.P.
	5. Special truss moment frames of steel (STMF)	6.5	2.8	240
4. Dual systems (frame resists at least 25% of seismic shear)	1. Shear walls			
	a. Concrete with SMRF	8.5	2.8	N.L.
	b. Concrete with steel OMRF	4.2	2.8	160
	c. Concrete with concrete IMRF ^e	6.5	2.8	160
	d. Masonry with SMRF	5.5	2.8	160
	e. Masonry with steel OMRF	4.2	2.8	160
	f. Masonry with concrete IMRF ^c	4.2	2.8	N.P.
	g. Masonry with masonry MMRWF	6.0	2.8	160
	2. Steel EBF			
	a. With steel SMRF	8.5	2.8	N.L.
	b. With steel OMRF	4.2	2.8	160
	3. Ordinary braced frames			
	a. Steel with steel SMRF	6.5	2.8	N.L.
	b. Steel with steel OMRF	4.2	2.8	160
	c. Concrete with concrete SMRF ^c	6.5	2.8	N.P.
	d. Concrete with concrete IMRF ^e	4.2	2.8	N.P.
	4. Special concentrically braced frames			
	a. Steel with steel SMRF	7.5	2.8	N.L.
	b. Steel with steel OMRF	4.2	2.8	160
5. Cantilevered column building systems	1. Cantilevered column elements ^g	2.2	2.0	357
6. Shear wall-frame interaction systems	1. Concrete ^h	5.5	2.8	160
7. Undefined systems	See Sections 1629.6.7 and 1629.9.2 (UBC 1997)	—	—	—

N.L.—no limit

N.P.—not permitted.

^a See Section 1630.4 for combination of structural systems.

^b Basic structural systems are defined in Section 1629.6, 1997 UBC.

^c Prohibited in seismic zones 3 and 4.

^d Includes precast concrete conforming to Section 1921.2.7, 1997 UBC.

^e Prohibited in seismic zones 3 and 4, except as permitted in Section 1634.2, 1997 UBC.

^f Ordinary moment-resisting frames in seismic zone 1 meeting the requirements of Section 2211.6 may use an *R* value of 8. See UBC 1997.

^g Total height of the building including cantilevered columns.

^h Prohibited in seismic zones 2A, 2B, 3, and 4. See Section 1633.2.7, 1997 UBC. (From UBC 1997, Table 16-N.)

Table 3: Seismic Coefficient C_v

Soil profile type	Seismic zone factor, Z				
	$Z = 0.075$	$Z = 0.15$	$Z = 0.2$	$Z = 0.3$	$Z = 0.4$
S_A	0.06	0.12	0.16	0.24	$0.32N_v$
S_B	0.08	0.15	0.20	0.30	$0.40N_v$
S_C	0.13	0.25	0.32	0.45	$0.56N_v$
S_D	0.18	0.32	0.40	0.54	$0.64N_v$
S_E	0.26	0.50	0.64	0.84	$0.96N_v$
S_F	Site-specific geotechnical investigation and dynamic site response analysis Shall be performed for soil type S_F .				

Table 4: Soil Profile Types

Soil profile type	Soil profile name/generic description	Average soil properties for top 100 feet (30,480 mm) of soil profile		
		Shear wave velocity, fsseet/second (m/s)	Standard penetration test (blows/foot)	Undrained shear strength, psf (kPa)
S_A	Hard rock	>5,000 (1,500)	—	—
S_B	Rock	2,500 to 5,000 (760 to 1,500)	—	—
S_C	Very dense soil and soft rock	1,200 to 2,500 (360 to 760)	>50	>2,000 (100)
S_D	Stiff soil profile	600 to 1,200 (180 to 360)	15 to 50	1,000 to 2,000 (50 to 100)
S_E	Soft soil profile	<600 (180)	<15	<1,000 (50)
S_F	Soil requiring site-specific evaluation.			

USE OR OCCUPANCY		UNIFORM LOAD ¹ (psf)	CONCENTRATED LOAD (pounds)
Category	Description	× 0.0479 for kN/m ²	× 0.004 48 for kN
1. Access floor systems	Office use	50	2,000 ²
	Computer use	100	2,000 ²
2. Armories		150	0
3. Assembly areas ³ and auditoriums and balconies therewith	Fixed seating areas	50	0
	Movable seating and other areas	100	0
	Stage areas and enclosed platforms	125	0
4. Cornices and marquees		60 ⁴	0
5. Exit facilities ⁵		100	0 ⁶
6. Garages	General storage and/or repair	100	7
	Private or pleasure-type motor vehicle storage	50	7
7. Hospitals	Wards and rooms	40	1,000 ²
8. Libraries	Reading rooms	60	1,000 ²
	Stack rooms	125	1,500 ²
9. Manufacturing	Light	75	2,000 ²
	Heavy	125	3,000 ²
10. Offices		50	2,000 ²
11. Printing plants	Press rooms	150	2,500 ²
	Composing and linotype rooms	100	2,000 ²
12. Residential ⁸	Basic floor area	40	0 ⁶
	Exterior balconies	60 ⁴	0
	Decks	40 ⁴	0
	Storage	40	0
13. Restrooms ⁹			
14. Reviewing stands, grandstands, bleachers, and folding and telescoping seating		100	0
15. Roof decks	Same as area served or for the type of occupancy accommodated		
16. Schools	Classrooms	40	1,000 ²
17. Sidewalks and driveways	Public access	250	7
18. Storage	Light	125	
	Heavy	250	
19. Stores		100	3,000 ²
20. Pedestrian bridges and walkways		100	

Table 1: Uniform and Concentrated Loads

APPENDIX E
WEIGHT OF BUILDING

LOAD OF EIGHTH FLOOR																			
Column No.	Tributry Area	Slab Load				Beam Load		Masonry Load		Column Load		Total Load For Floor 8				Commulative Load			
		D.L		L.L		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	D.L		L.L		D.L		L.L	
		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)							Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)		
1-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	8.13	9.75	1.603	1.924	32.873	39.442	8.84	14.144	32.873	39.454	8.84	14.14
1-B	235	35.25	42.3	16.45	26.32	6.2	7.44	11.94	14.32	1.603	1.924	54.993	65.984	16.45	26.32	54.993	65.984	16.45	26.32
1-C	235	35.25	42.3	16.45	26.32	6.2	7.44	11.94	14.32	1.603	1.924	54.993	65.984	16.45	26.32	54.993	65.984	16.45	26.32
1-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	8.13	9.75	1.603	1.924	32.873	39.442	8.84	14.144	32.873	39.454	8.84	14.14
2-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	12.35	14.82	1.603	1.924	55.853	67.024	16.56	26.496	55.853	66.994	16.56	26.49
2-B	440	66	79.2	30.8	49.28	8.4	10.08	16.37	19.63	2.85	3.42	93.62	112.33	30.8	49.28	93.62	112.33	30.8	49.28
2-C	440	66	79.2	30.8	49.28	8.4	10.08	16.37	19.63	2.85	3.42	93.62	112.33	30.8	49.28	93.62	112.33	30.8	49.28
2-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	12.35	14.82	1.603	1.924	55.853	67.024	16.56	26.496	55.853	66.994	16.56	26.49
3-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	12.35	14.82	1.603	1.924	55.853	67.024	16.56	26.496	55.853	66.994	16.56	26.49
3-B	440	66	79.2	30.8	49.28	8.4	10.08	16.37	19.63	2.85	3.42	93.62	112.33	30.8	49.28	93.62	112.33	30.8	49.28
3-C	440	66	79.2	30.8	49.28	8.4	10.08	16.37	19.63	2.85	3.42	93.62	112.33	30.8	49.28	93.62	112.33	30.8	49.28
3-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	12.35	14.82	1.603	1.924	55.853	67.024	16.56	26.496	55.853	66.994	16.56	26.49
4-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	8.13	9.75	1.603	1.924	32.873	39.442	8.84	14.144	32.873	39.454	8.84	14.14
4-B	235	35.25	42.3	16.45	26.32	6.2	7.4	11.94	14.32	1.603	1.924	54.993	65.944	16.45	26.32	54.993	65.944	16.45	26.32
4-C	235	35.25	42.3	16.45	26.32	6.2	7.4	11.94	14.32	1.603	1.924	54.993	65.944	16.45	26.32	54.993	65.944	16.45	26.32
4-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	8.13	9.75	1.603	1.924	32.873	39.442	8.84	14.144	32.873	39.454	8.84	14.14
Σ		622.76	747.312	290.6	464.96	100.8	120.88	195.16	234.08	30.636	36.768	949.356	1139.04	290.6	464.96	949.356	1138.968	290.6	464.92

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LOAD OF SEVENTH FLOOR																			
Column No.	Tributry Area	Slab Load				Beam Load		Masonry Load		Column Load		Total Load For Floor 7				Commulative Load			
		D.L		L.L		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	D.L		L.L		D.L		L.L	
		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)							Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)				
1-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	16.37	19.51	3.91	4.66	43.42	51.938	8.84	14.14	76.293	91.392	17.68	28.28
1-B	235	35.25	42.3	16.45	26.32	6.2	7.44	23.87	28.64	3.91	4.66	69.23	83.04	16.45	26.32	124.223	149.024	32.9	52.64
1-C	235	35.25	42.3	16.45	26.32	6.2	7.44	23.87	28.64	3.91	4.66	69.23	83.04	16.45	26.32	124.223	149.024	32.9	52.64
1-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	16.37	19.51	3.91	4.66	43.42	51.938	8.84	14.14	76.293	91.392	17.68	28.28
2-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	24.71	29.64	3.91	4.66	70.52	84.58	16.56	26.49	126.373	151.574	33.12	52.98
2-B	440	66	79.2	30.8	49.28	8.4	10.08	32.73	39.27	6.9	8.28	114.03	136.83	30.8	49.28	207.65	249.16	61.6	98.56
2-C	440	66	79.2	30.8	49.28	8.4	10.08	32.73	39.27	6.9	8.28	114.03	136.83	30.8	49.28	207.65	249.16	61.6	98.56
2-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	24.71	29.64	3.91	4.66	70.52	84.58	16.56	26.49	126.373	151.574	33.12	52.98
3-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	24.71	29.64	3.91	4.66	70.52	84.58	16.56	26.49	126.373	151.574	33.12	52.98
3-B	440	66	79.2	30.8	49.28	8.4	10.08	32.73	39.27	6.9	8.28	114.03	136.83	30.8	49.28	207.65	249.16	61.6	98.56
3-C	440	66	79.2	30.8	49.28	8.4	10.08	32.73	39.27	6.9	8.28	114.03	136.83	30.8	49.28	207.65	249.16	61.6	98.56
3-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	24.71	29.64	3.91	4.66	70.52	84.58	16.56	26.49	126.373	151.574	33.12	52.98
4-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	16.37	19.51	3.91	4.66	43.42	51.938	8.84	14.14	76.293	91.392	17.68	28.28
4-B	235	35.25	42.3	16.45	26.32	6.2	7.44	23.87	28.64	3.91	4.66	69.23	83.04	16.45	26.32	124.223	148.984	32.9	52.64
4-C	235	35.25	42.3	16.45	26.32	6.2	7.44	23.87	28.64	3.91	4.66	69.23	83.04	16.45	26.32	124.223	148.984	32.9	52.64
4-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	16.37	19.51	3.91	4.66	43.42	51.938	8.84	14.14	76.293	91.392	17.68	28.28
Σ		622.76	747.312	290.6	464.96	100.8	120.96	390.72	468.24	74.52	89.04	1188.8	1425.552	290.6	464.92	2138.156	2564.52	581.2	929.84

LOAD OF SIXTH FLOOR																			
Column No.	Tributry Area	Slab Load				Beam Load		Masonry Load		Column Load		Total Load For Floor 6				Commulative Load			
		D.L		L.L		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	D.L		L.L		D.L		L.L	
		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)							Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)
1-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	16.37	19.51	3.91	4.66	43.42	51.938	8.84	14.14	119.713	143.33	26.52	42.42
1-B	235	35.25	42.3	16.45	26.32	6.2	7.44	23.87	28.64	3.91	4.66	69.23	83.04	16.45	26.32	193.453	232.064	49.35	78.96
1-C	235	35.25	42.3	16.45	26.32	6.2	7.44	23.87	28.64	3.91	4.66	69.23	83.04	16.45	26.32	193.453	232.064	49.35	78.96
1-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	16.37	19.51	3.91	4.66	43.42	51.938	8.84	14.14	119.713	143.33	26.52	42.42
2-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	24.71	29.64	3.91	4.66	70.52	84.58	16.56	26.49	196.893	236.154	49.68	79.47
2-B	440	66	79.2	30.8	49.28	8.4	10.08	32.73	39.27	6.9	8.28	114.03	136.83	30.8	49.28	321.68	385.99	92.4	147.84
2-C	440	66	79.2	30.8	49.28	8.4	10.08	32.73	39.27	6.9	8.28	114.03	136.83	30.8	49.28	321.68	385.99	92.4	147.84
2-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	24.71	29.64	3.91	4.66	70.52	84.58	16.56	26.49	196.893	236.154	49.68	79.47
3-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	24.71	29.64	3.91	4.66	70.52	84.58	16.56	26.49	196.893	236.154	49.68	79.47
3-B	440	66	79.2	30.8	49.28	8.4	10.08	32.73	39.27	6.9	8.28	114.03	136.83	30.8	49.28	321.68	385.99	92.4	147.84
3-C	440	66	79.2	30.8	49.28	8.4	10.08	32.73	39.27	6.9	8.28	114.03	136.83	30.8	49.28	321.68	385.99	92.4	147.84
3-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	24.71	29.64	3.91	4.66	70.52	84.58	16.56	26.49	196.893	236.154	49.68	79.47
4-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	16.37	19.51	3.91	4.66	43.42	51.938	8.84	14.14	119.713	143.33	26.52	42.42
4-B	235	35.25	42.3	16.45	26.32	6.2	7.44	23.87	28.64	3.91	4.66	69.23	83.04	16.45	26.32	193.453	232.024	49.35	78.96
4-C	235	35.25	42.3	16.45	26.32	6.2	7.44	23.87	28.64	3.91	4.66	69.23	83.04	16.45	26.32	193.453	232.024	49.35	78.96
4-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	16.37	19.51	3.91	4.66	43.42	51.938	8.84	14.14	119.713	143.33	26.52	42.42
Σ		622.76	747.312	290.6	464.96	100.8	120.96	390.72	468.24	74.52	89.04	1188.8	1425.552	290.6	464.92	3326.956	3990.072	871.8	1394.76

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LOAD OF FIFTH FLOOR																			
Column No.	Tributry Area	Slab Load				Beam Load		Masonry Load		Column Load		Total Load For Floor 5				Commulative Load			
		D.L		L.L		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	D.L		L.L		D.L		L.L	
		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)							Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)
1-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	16.37	19.51	3.91	4.66	43.42	51.938	8.84	14.14	163.133	195.268	35.36	56.56
1-B	235	35.25	42.3	16.45	26.32	6.2	7.44	23.87	28.64	3.91	4.66	69.23	83.04	16.45	26.32	262.683	315.104	65.8	105.28
1-C	235	35.25	42.3	16.45	26.32	6.2	7.44	23.87	28.64	3.91	4.66	69.23	83.04	16.45	26.32	262.683	315.104	65.8	105.28
1-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	16.37	19.51	3.91	4.66	43.42	51.938	8.84	14.14	163.133	195.268	35.36	56.56
2-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	24.71	29.64	3.91	4.66	70.52	84.58	16.56	26.49	267.413	320.734	66.24	105.96
2-B	440	66	79.2	30.8	49.28	8.4	10.08	32.73	39.27	6.9	8.28	114.03	136.83	30.8	49.28	435.71	522.82	123.2	197.12
2-C	440	66	79.2	30.8	49.28	8.4	10.08	32.73	39.27	6.9	8.28	114.03	136.83	30.8	49.28	435.71	522.82	123.2	197.12
2-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	24.71	29.64	3.91	4.66	70.52	84.58	16.56	26.49	267.413	320.734	66.24	105.96
3-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	24.71	29.64	3.91	4.66	70.52	84.58	16.56	26.49	267.413	320.734	66.24	105.96
3-B	440	66	79.2	30.8	49.28	8.4	10.08	32.73	39.27	6.9	8.28	114.03	136.83	30.8	49.28	435.71	522.82	123.2	197.12
3-C	440	66	79.2	30.8	49.28	8.4	10.08	32.73	39.27	6.9	8.28	114.03	136.83	30.8	49.28	435.71	522.82	123.2	197.12
3-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	24.71	29.64	3.91	4.66	70.52	84.58	16.56	26.49	267.413	320.734	66.24	105.96
4-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	16.37	19.51	3.91	4.66	43.42	51.938	8.84	14.14	163.133	195.268	35.36	56.56
4-B	235	35.25	42.3	16.45	26.32	6.2	7.44	23.87	28.64	3.91	4.66	69.23	83.04	16.45	26.32	262.683	315.064	65.8	105.28
4-C	235	35.25	42.3	16.45	26.32	6.2	7.44	23.87	28.64	3.91	4.66	69.23	83.04	16.45	26.32	262.683	315.064	65.8	105.28
4-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	16.37	19.51	3.91	4.66	43.42	51.938	8.84	14.14	163.133	195.268	35.36	56.56
Σ		622.76	747.312	290.6	464.96	100.8	120.96	390.72	468.24	74.52	89.04	1188.8	1425.552	290.6	464.92	4515.756	5415.624	1162.4	1859.68

LOAD OF FOURTH FLOOR																			
Column No.	Tributry Area	Slab Load				Beam Load		Masonry Load		Column Load		Total Load For Floor 4				Commulative Load			
		D.L		L.L		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	D.L		L.L		D.L		L.L	
		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)							Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)
1-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	17.79	21.35	4.215	5.061	45.145	54.179	8.84	14.14	208.278	249.447	44.2	70.7
1-B	235	35.25	42.3	16.45	26.32	6.2	7.44	26.12	31.34	4.215	5.061	71.785	86.141	16.45	26.32	334.468	401.245	82.25	131.6
1-C	235	35.25	42.3	16.45	26.32	6.2	7.44	26.12	31.34	4.215	5.061	71.785	86.141	16.45	26.32	334.468	401.245	82.25	131.6
1-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	17.79	21.35	4.215	5.061	45.145	54.179	8.84	14.14	208.278	249.447	44.2	70.7
2-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	27.03	32.44	4.215	5.061	73.145	87.781	16.56	26.49	340.558	408.515	82.8	132.45
2-B	440	66	79.2	30.8	49.28	8.4	10.08	35.82	42.97	7.5	9	117.72	141.25	30.8	49.28	553.43	664.07	154	246.4
2-C	440	66	79.2	30.8	49.28	8.4	10.08	35.82	42.97	7.5	9	117.72	141.25	30.8	49.28	553.43	664.07	154	246.4
2-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	27.03	32.44	4.215	5.061	73.145	87.781	16.56	26.49	340.558	408.515	82.8	132.45
3-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	27.03	32.44	4.215	5.061	73.145	87.781	16.56	26.49	340.558	408.515	82.8	132.45
3-B	440	66	79.2	30.8	49.28	8.4	10.08	35.82	42.97	7.5	9	117.72	141.25	30.8	49.28	553.43	664.07	154	246.4
3-C	440	66	79.2	30.8	49.28	8.4	10.08	35.82	42.97	7.5	9	117.72	141.25	30.8	49.28	553.43	664.07	154	246.4
3-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	27.03	32.44	4.215	5.061	73.145	87.781	16.56	26.49	340.558	408.515	82.8	132.45
4-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	17.79	21.35	4.215	5.061	45.145	54.179	8.84	14.14	208.278	249.447	44.2	70.7
4-B	235	35.25	42.3	16.45	26.32	6.2	7.44	26.12	31.34	4.215	5.061	71.785	86.141	16.45	26.32	334.468	401.205	82.25	131.6
4-C	235	35.25	42.3	16.45	26.32	6.2	7.44	26.12	31.34	4.215	5.061	71.785	86.141	16.45	26.32	334.468	401.205	82.25	131.6
4-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	17.79	21.35	4.215	5.061	45.145	54.179	8.84	14.14	208.278	249.447	44.2	70.7
Σ		622.76	747.312	290.6	464.96	100.8	120.96	427.04	512.4	80.58	96.732	1231.18	1477.404	290.6	464.92	5746.936	6893.028	1453	2324.6

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LOAD OF THIRD FLOOR																			
Column No.	Tributry Area	Slab Load				Beam Load		Masonry Load		Column Load		Total Load For Floor 3				Commulative Load			
		D.L		L.L		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	D.L		L.L		D.L		L.L	
		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)							Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)
1-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	19.227	23.0724	4.56	5.472	46.927	56.3124	8.84	14.144	255.205	305.7594	53.04	84.844
1-B	235	35.25	42.3	16.45	26.32	6.2	7.44	28.22	33.864	4.56	5.472	74.23	89.076	16.45	26.32	408.698	490.321	98.7	157.92
1-C	235	35.25	42.3	16.45	26.32	6.2	7.44	28.22	33.864	4.56	5.472	74.23	89.076	16.45	26.32	408.698	490.321	98.7	157.92
1-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	19.227	23.0724	4.56	5.472	46.927	56.3124	8.84	14.144	255.205	305.7594	53.04	84.844
2-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	29.21	35.052	4.56	5.472	75.67	90.804	16.56	26.496	416.228	499.319	99.36	158.946
2-B	440	66	79.2	30.8	49.28	8.4	10.08	38.7	46.44	8.1	9.72	121.2	145.44	30.8	49.28	674.63	809.51	184.8	295.68
2-C	440	66	79.2	30.8	49.28	8.4	10.08	38.7	46.44	8.1	9.72	121.2	145.44	30.8	49.28	674.63	809.51	184.8	295.68
2-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	29.21	35.052	4.56	5.472	75.67	90.804	16.56	26.496	416.228	499.319	99.36	158.946
3-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	29.21	35.052	4.56	5.472	75.67	90.804	16.56	26.496	416.228	499.319	99.36	158.946
3-B	440	66	79.2	30.8	49.28	8.4	10.08	38.7	46.44	8.1	9.72	121.2	145.44	30.8	49.28	674.63	809.51	184.8	295.68
3-C	440	66	79.2	30.8	49.28	8.4	10.08	38.7	46.44	8.1	9.72	121.2	145.44	30.8	49.28	674.63	809.51	184.8	295.68
3-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	29.21	35.052	4.56	5.472	75.67	90.804	16.56	26.496	416.228	499.319	99.36	158.946
4-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	19.227	23.0724	4.56	5.472	46.927	56.3124	8.84	14.144	255.205	305.7594	53.04	84.844
4-B	235	35.25	42.3	16.45	26.32	6.2	7.44	28.22	33.864	4.56	5.472	74.23	89.076	16.45	26.32	408.698	490.281	98.7	157.92
4-C	235	35.25	42.3	16.45	26.32	6.2	7.44	28.22	33.864	4.56	5.472	74.23	89.076	16.45	26.32	408.698	490.281	98.7	157.92
4-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	19.227	23.0724	4.56	5.472	46.927	56.3124	8.84	14.144	255.205	305.7594	53.04	84.844
Σ		622.76	747.312	290.6	464.96	100.8	120.96	461.428	553.7136	87.12	104.544	1272.108	1526.5296	290.6	464.96	7019.044	8419.5576	1743.6	2789.56

LOAD OF SECOND FLOOR																			
Column No.	Tributry Area	Slab Load				Beam Load		Masonry Load		Column Load		Total Load For Floor 2				Commulative Load			
		D.L		L.L		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	D.L		L.L		D.L		L.L	
		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)							Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)		
1-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	19.227	23.0724	4.56	5.472	46.927	56.3124	8.84	14.144	302.132	362.0718	61.88	98.988
1-B	235	35.25	42.3	16.45	26.32	6.2	7.44	28.22	33.864	4.56	5.472	74.23	89.076	16.45	26.32	482.928	579.397	115.15	184.24
1-C	235	35.25	42.3	16.45	26.32	6.2	7.44	28.22	33.864	4.56	5.472	74.23	89.076	16.45	26.32	482.928	579.397	115.15	184.24
1-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	19.227	23.0724	4.56	5.472	46.927	56.3124	8.84	14.144	302.132	362.0718	61.88	98.988
2-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	29.21	35.052	4.56	5.472	75.67	90.804	16.56	26.496	491.898	590.123	115.92	185.442
2-B	440	66	79.2	30.8	49.28	8.4	10.08	38.7	46.44	8.1	9.72	121.2	145.44	30.8	49.28	795.83	954.95	215.6	344.96
2-C	440	66	79.2	30.8	49.28	8.4	10.08	38.7	46.44	8.1	9.72	121.2	145.44	30.8	49.28	795.83	954.95	215.6	344.96
2-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	29.21	35.052	4.56	5.472	75.67	90.804	16.56	26.496	491.898	590.123	115.92	185.442
3-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	29.21	35.052	4.56	5.472	75.67	90.804	16.56	26.496	491.898	590.123	115.92	185.442
3-B	440	66	79.2	30.8	49.28	8.4	10.08	38.7	46.44	8.1	9.72	121.2	145.44	30.8	49.28	795.83	954.95	215.6	344.96
3-C	440	66	79.2	30.8	49.28	8.4	10.08	38.7	46.44	8.1	9.72	121.2	145.44	30.8	49.28	795.83	954.95	215.6	344.96
3-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	29.21	35.052	4.56	5.472	75.67	90.804	16.56	26.496	491.898	590.123	115.92	185.442
4-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	19.227	23.0724	4.56	5.472	46.927	56.3124	8.84	14.144	302.132	362.0718	61.88	98.988
4-B	235	35.25	42.3	16.45	26.32	6.2	7.44	28.22	33.864	4.56	5.472	74.23	89.076	16.45	26.32	482.928	579.357	115.15	184.24
4-C	235	35.25	42.3	16.45	26.32	6.2	7.44	28.22	33.864	4.56	5.472	74.23	89.076	16.45	26.32	482.928	579.357	115.15	184.24
4-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	19.227	23.0724	4.56	5.472	46.927	56.3124	8.84	14.144	302.132	362.0718	61.88	98.988
Σ		622.76	747.312	290.6	464.96	100.8	120.96	461.428	553.7136	87.12	104.544	1272.108	1526.5296	290.6	464.96	8291.152	9946.0872	2034.2	3254.52

LOAD OF FIRST FLOOR																			
Column No.	Tributry Area	Slab Load				Beam Load		Masonry Load		Column Load		Total Load For Floor 1				Commulative Load			
		D.L		L.L		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	D.L		L.L		D.L		L.L	
		Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)							Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)	Service (Kips)	Factored (kips)		
1-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	19.227	23.0724	4.56	5.472	46.927	56.3124	8.84	14.144	349.059	418.3842	70.72	113.132
1-B	235	35.25	42.3	16.45	26.32	6.2	7.44	28.22	33.864	4.56	5.472	74.23	89.076	16.45	26.32	557.158	668.473	131.6	210.56
1-C	235	35.25	42.3	16.45	26.32	6.2	7.44	28.22	33.864	4.56	5.472	74.23	89.076	16.45	26.32	557.158	668.473	131.6	210.56
1-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	19.227	23.0724	4.56	5.472	46.927	56.3124	8.84	14.144	349.059	418.3842	70.72	113.132
2-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	29.21	35.052	4.56	5.472	75.67	90.804	16.56	26.496	567.568	680.927	132.48	211.938
2-B	440	66	79.2	30.8	49.28	8.4	10.08	38.7	46.44	8.1	9.72	121.2	145.44	30.8	49.28	917.03	1100.39	246.4	394.24
2-C	440	66	79.2	30.8	49.28	8.4	10.08	38.7	46.44	8.1	9.72	121.2	145.44	30.8	49.28	917.03	1100.39	246.4	394.24
2-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	29.21	35.052	4.56	5.472	75.67	90.804	16.56	26.496	567.568	680.927	132.48	211.938
3-A	236.5	35.5	42.6	16.56	26.496	6.4	7.68	29.21	35.052	4.56	5.472	75.67	90.804	16.56	26.496	567.568	680.927	132.48	211.938
3-B	440	66	79.2	30.8	49.28	8.4	10.08	38.7	46.44	8.1	9.72	121.2	145.44	30.8	49.28	917.03	1100.39	246.4	394.24
3-C	440	66	79.2	30.8	49.28	8.4	10.08	38.7	46.44	8.1	9.72	121.2	145.44	30.8	49.28	917.03	1100.39	246.4	394.24
3-D	236.5	35.5	42.6	16.56	26.496	6.4	7.68	29.21	35.052	4.56	5.472	75.67	90.804	16.56	26.496	567.568	680.927	132.48	211.938
4-A	126.31	18.94	22.728	8.84	14.144	4.2	5.04	19.227	23.0724	4.56	5.472	46.927	56.3124	8.84	14.144	349.059	418.3842	70.72	113.132
4-B	235	35.25	42.3	16.45	26.32	6.2	7.44	28.22	33.864	4.56	5.472	74.23	89.076	16.45	26.32	557.158	668.433	131.6	210.56
4-C	235	35.25	42.3	16.45	26.32	6.2	7.44	28.22	33.864	4.56	5.472	74.23	89.076	16.45	26.32	557.158	668.433	131.6	210.56
4-D	126.31	18.94	22.728	8.84	14.144	4.2	5.04	19.227	23.0724	4.56	5.472	46.927	56.3124	8.84	14.144	349.059	418.3842	70.72	113.132
Σ		622.76	747.312	290.6	464.96	100.8	120.96	461.428	553.7136	87.12	104.544	1272.108	1526.5296	290.6	464.96	9563.26	11472.6168	2324.8	3719.48

REFERENCES

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- A First Course in the Finite Element Method by Daryl L. Logan
- Uniform Building Code-1997 (UBC 97)
- ACI (318-05)
- ANSI